

The Performance of **Jet** Reconstruction and Distinguishment among Multi-jet Events at CEPC



Pei-Zhu Lai



NCU (Taiwan)

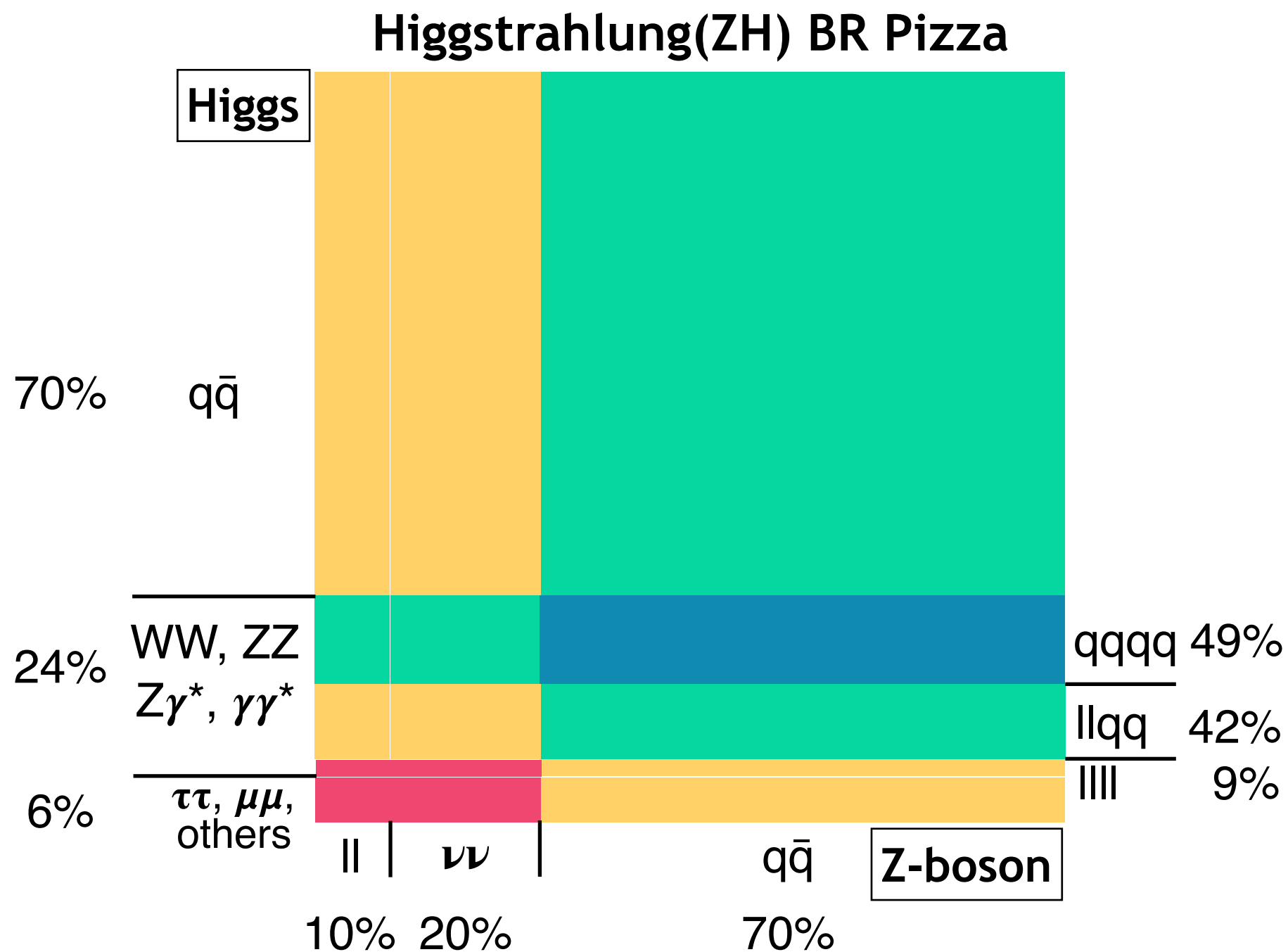
On the behalf of the CEPC Collaboration

(pei-zhu.lai@cern.ch)

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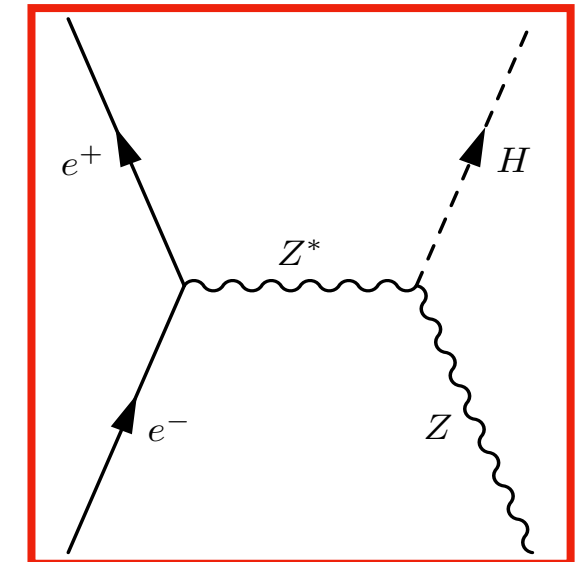
Feb 05 - Feb 07, 2020

Jets at the Higgs Signal



| # of jets | Probability |
|-----------|-------------|
| 0 | 2.44% |
| 2 | 29.73% |
| 4 | 59.58% |
| 6 | 8.23% |

~ 97% with Jets



- Circular Electron Positron Collider (CEPC) is a future collider aims to precisely measure the properties of the Higgs boson.
- Up to **97%** of Higgstrahlung(ZH) final-states associates to jets.
- Jets are also critical for many EW precision measurements.

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- 67% (4 + 6 jets) needs **dedicated color-singlet identification**: grouping the hadronic final-state particles into color-singlets (Z, W, H, γ^*). Can be done via jet clustering and pairing.
- **Jet clustering**, $ee-k_t$, is also essential for **differential** Higgs & EW precision measurements (e.g. TGCs).

BMI: Massive bosons
invariant mass resolutions

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BM2: Jet energy and angular differential response

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1/3 of ZH events

- Major SM Higgs decay modes.
- 1 color singlet could be identified.
(Single Z or Higgs boson)

BMI: Massive bosons

invariant mass resolutions

2/3 of ZH events

- Dominance statistic of $ZH \rightarrow q\bar{q}q\bar{q}$.
- Major uncertainty is on wrong jet pairing. (Potential huge impact)

BM3: # of jet identification & thrust based algorithm for 2-jet

BM4: Separation of WW , ZZ , and ZH decay to $qqqq$ final state

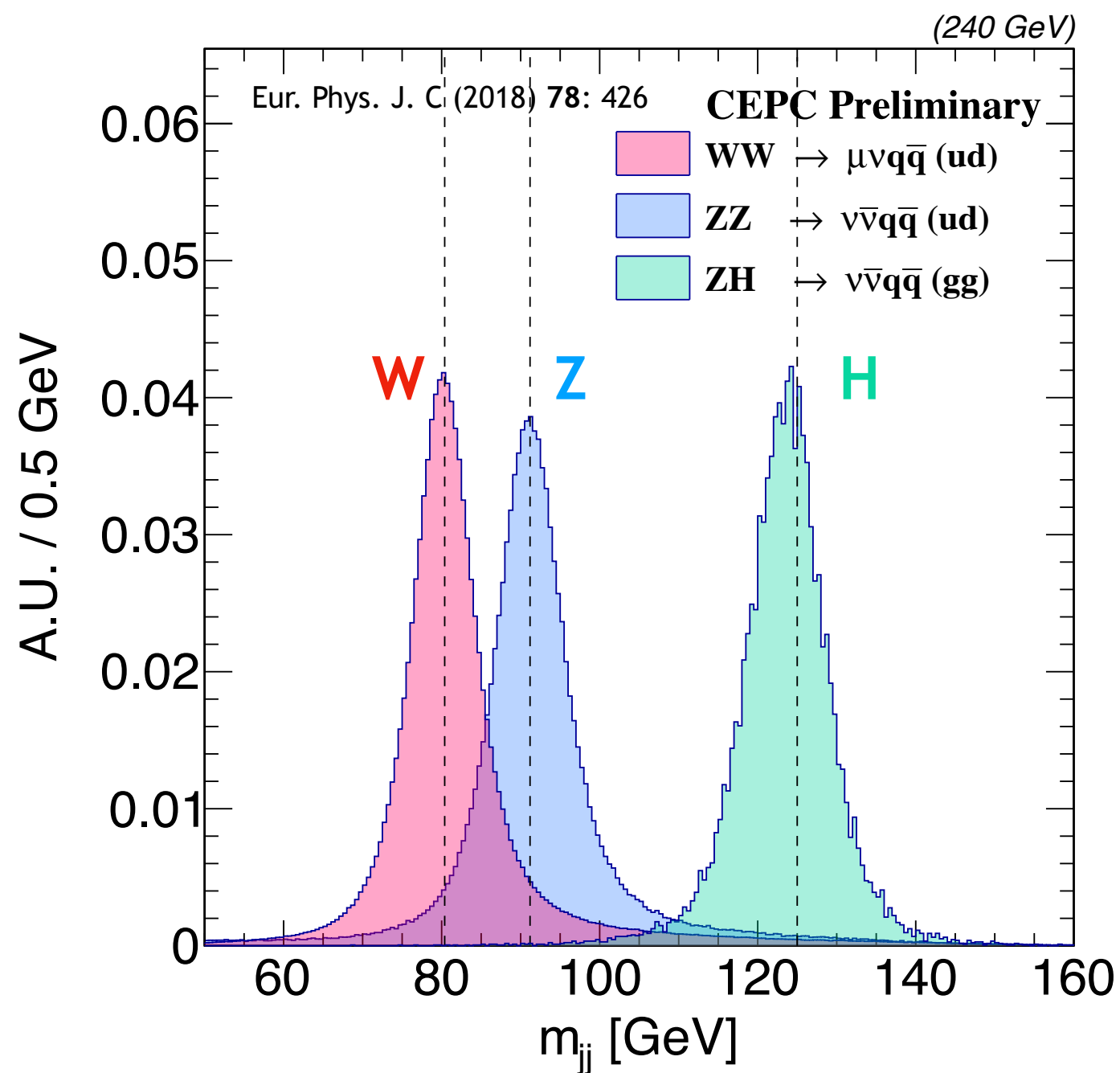
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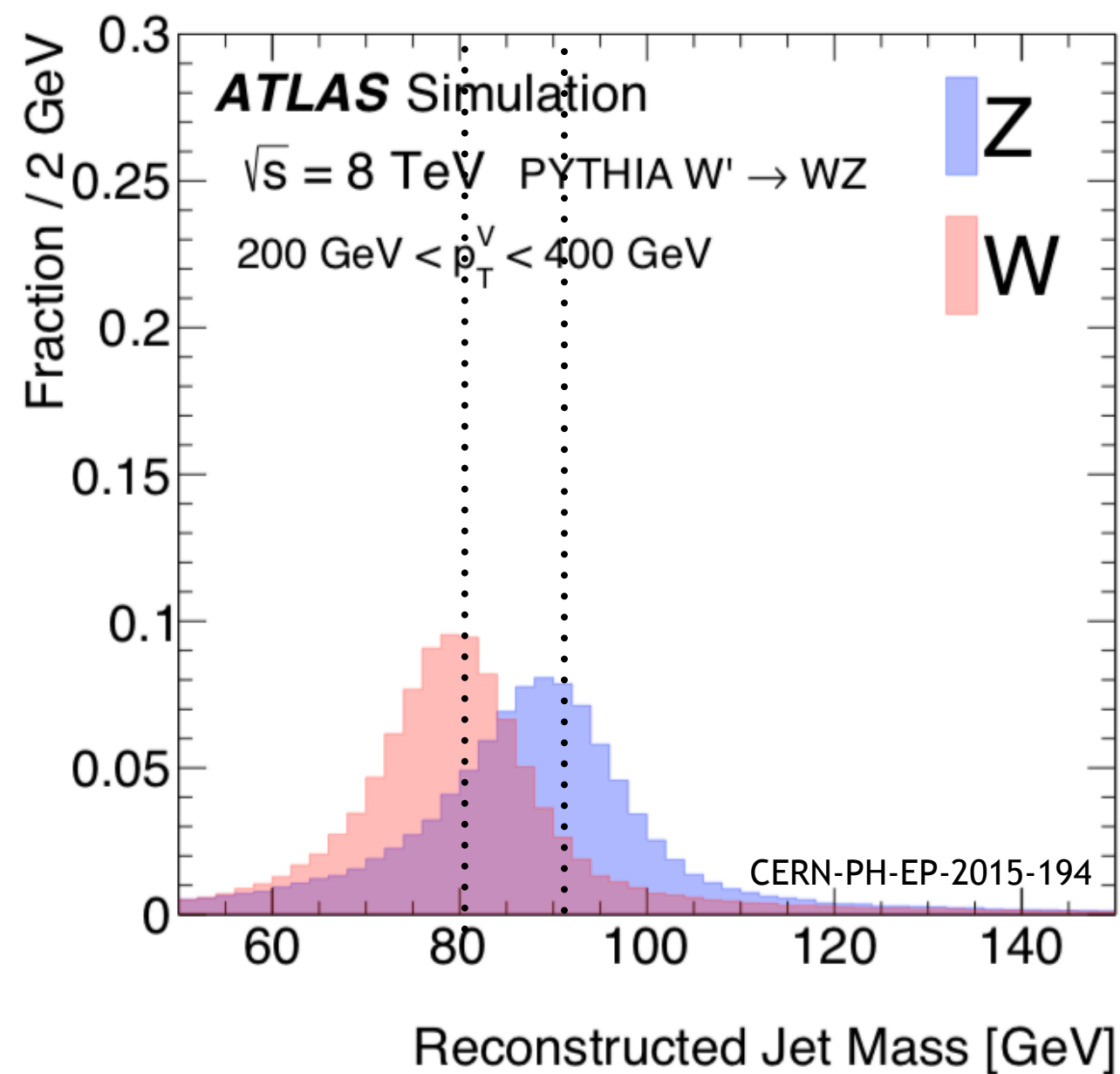
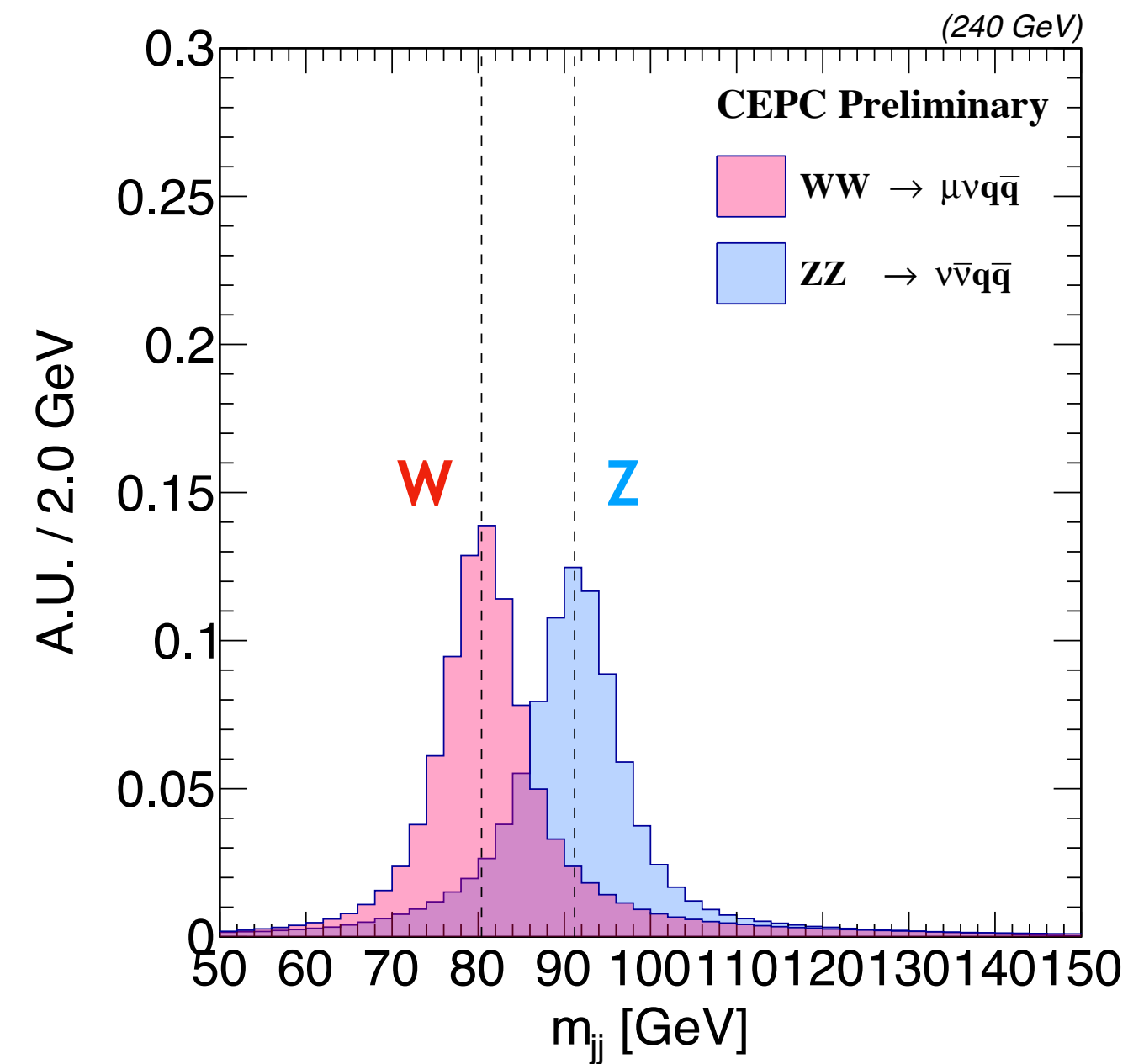
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BM1: Massive Boson Mass Resolution



- W-, Z-, and Higgs-boson masses in dijet final state can be well separated at CEPC.
- Z- and W-boson could be separated $\approx 2\sigma$, and the Higgs Boson Mass Resolution = 3.8% achieving the CEPC baseline.

BM1: Massive Boson Mass Resolution

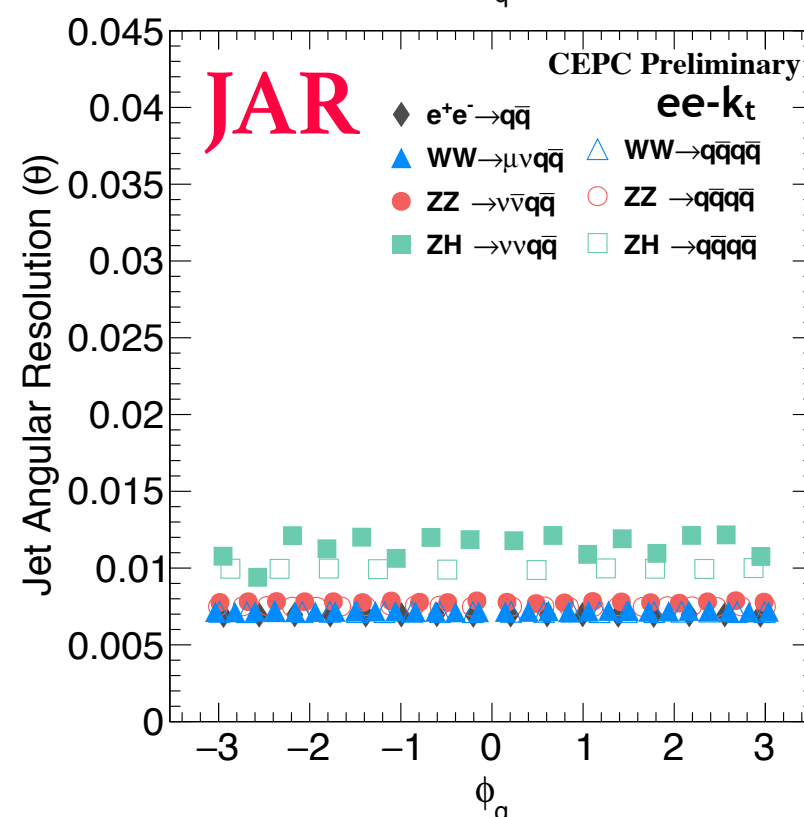
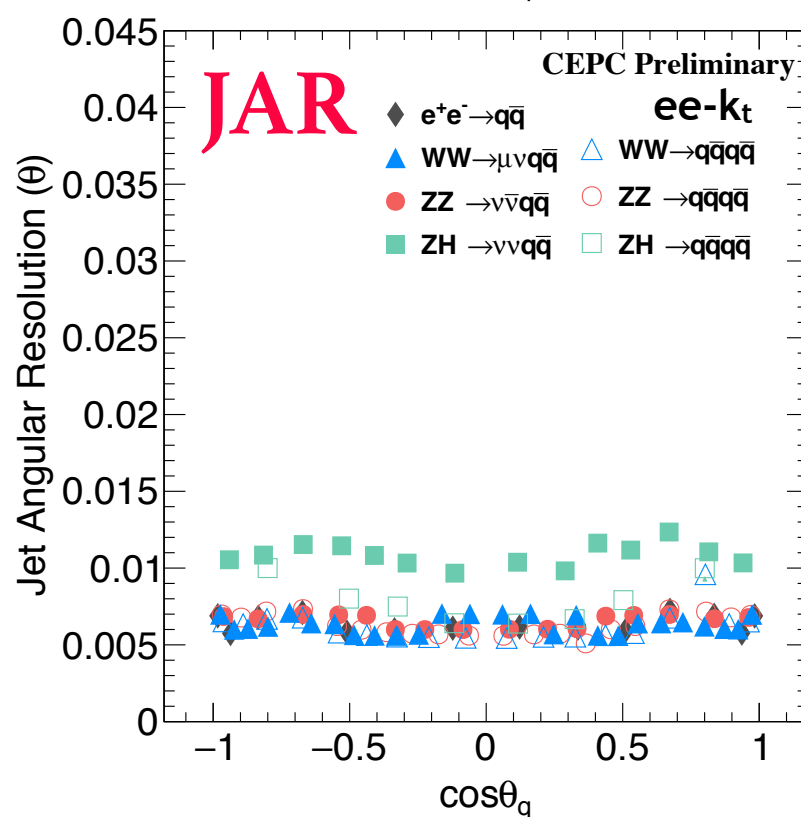
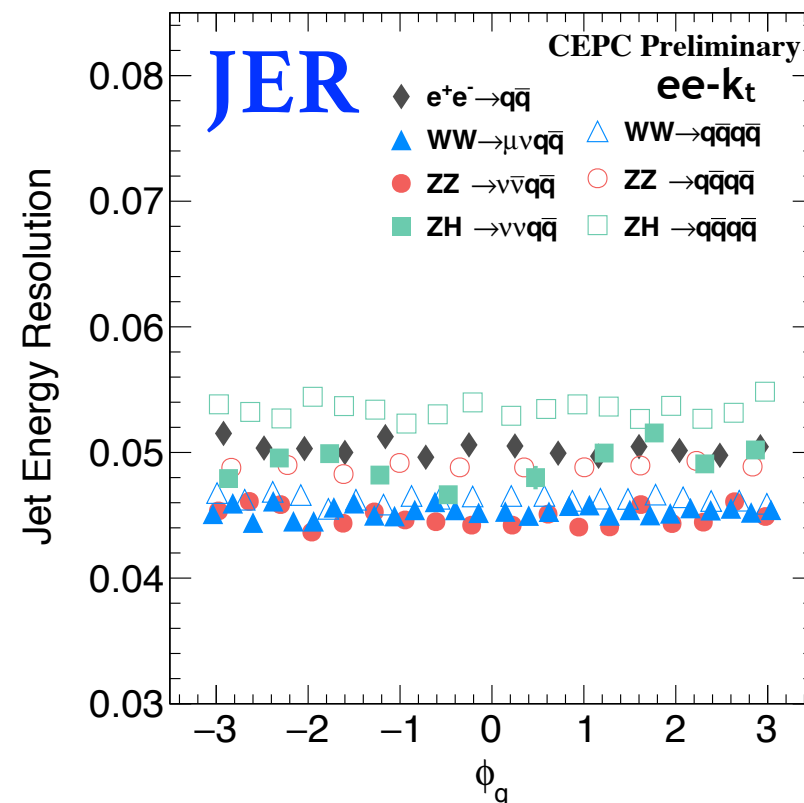
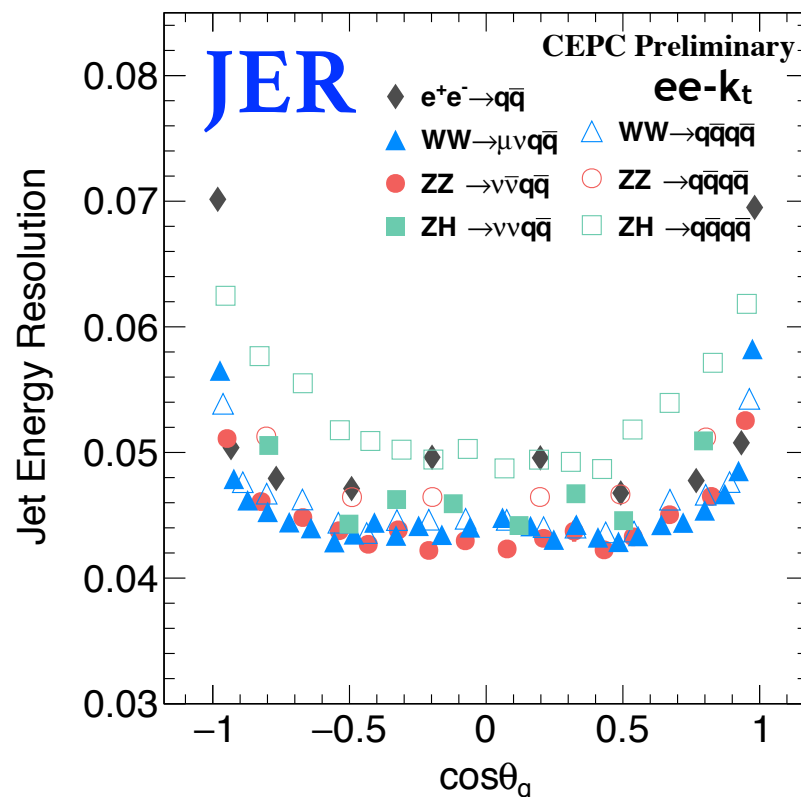


- The separation of Z- and W-boson at CEPC is much better than ATLAS as it should be, because of the better collision environment and detector response.

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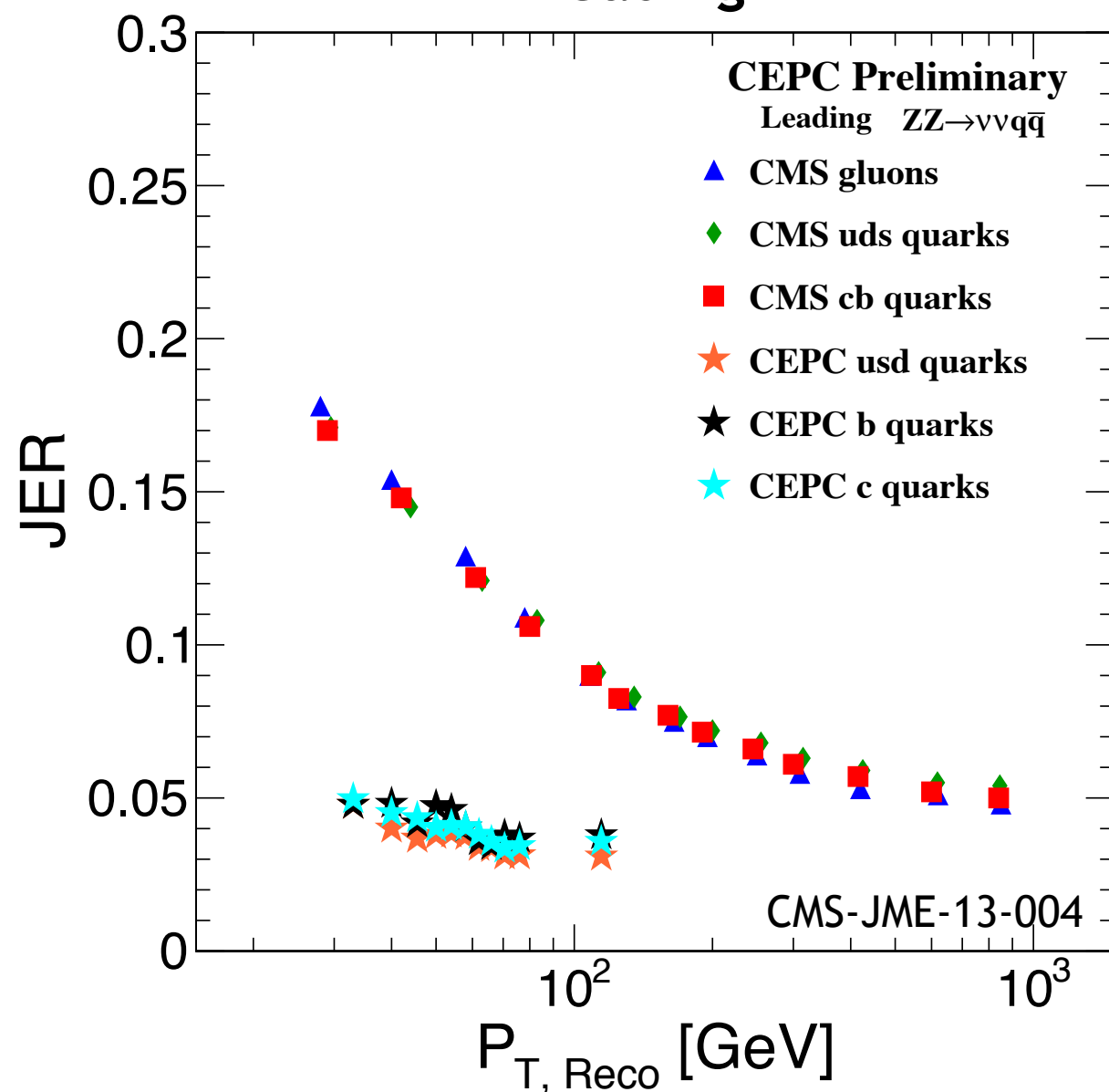
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BM2: Jet energy and angular differential response

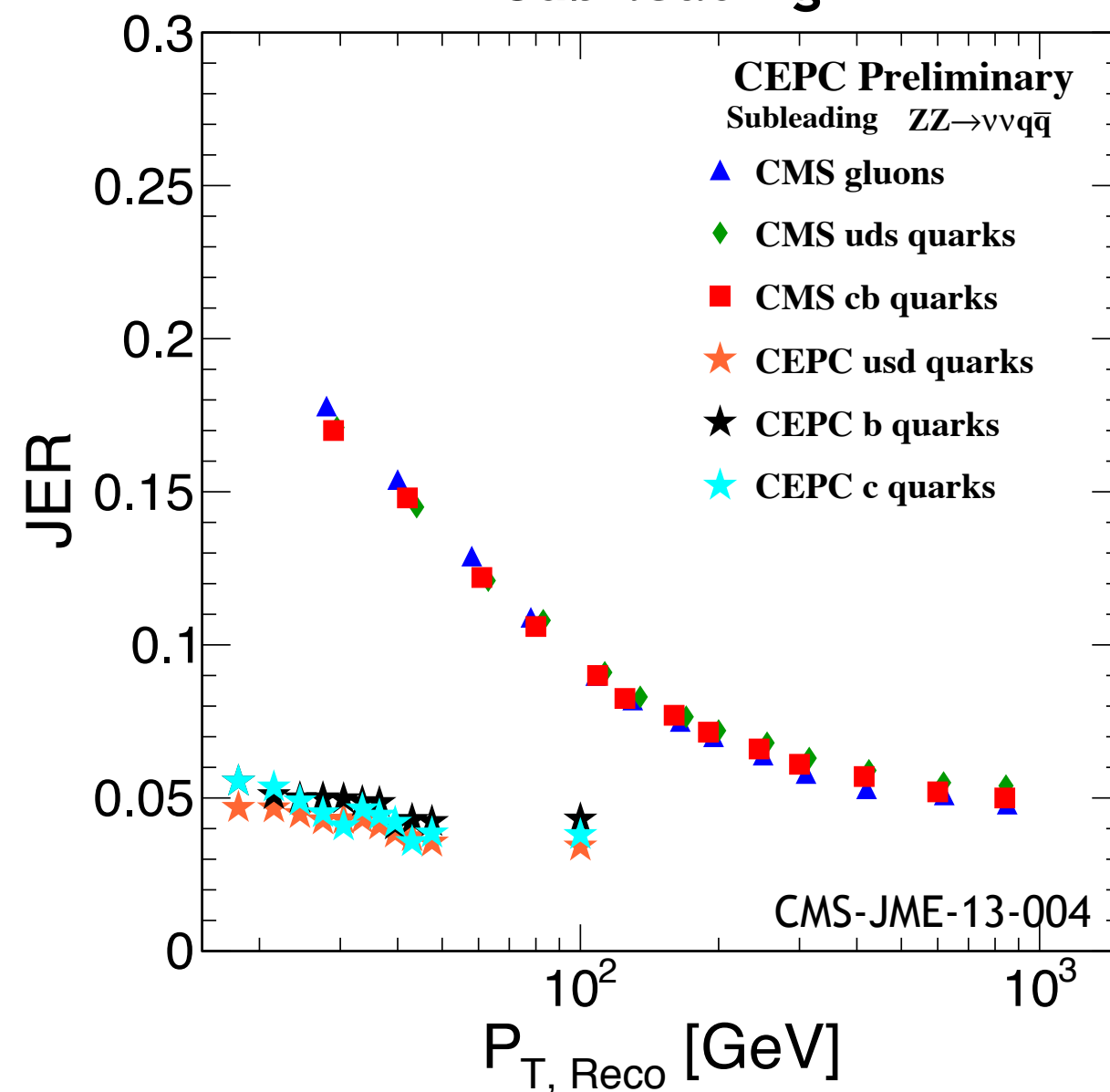


- JER is around **4.5%**, and JAR is around **1%** in barrel region;
- The difference between 2 and 4 jets final-state is controlled within **1%** level.

Leading



Sub-leading



- JER at CEPC is better than CMS as it should be; **2-4 times** better in the same energy regions.

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BM3: # of jet identification & thrust based algorithm for 2-jet

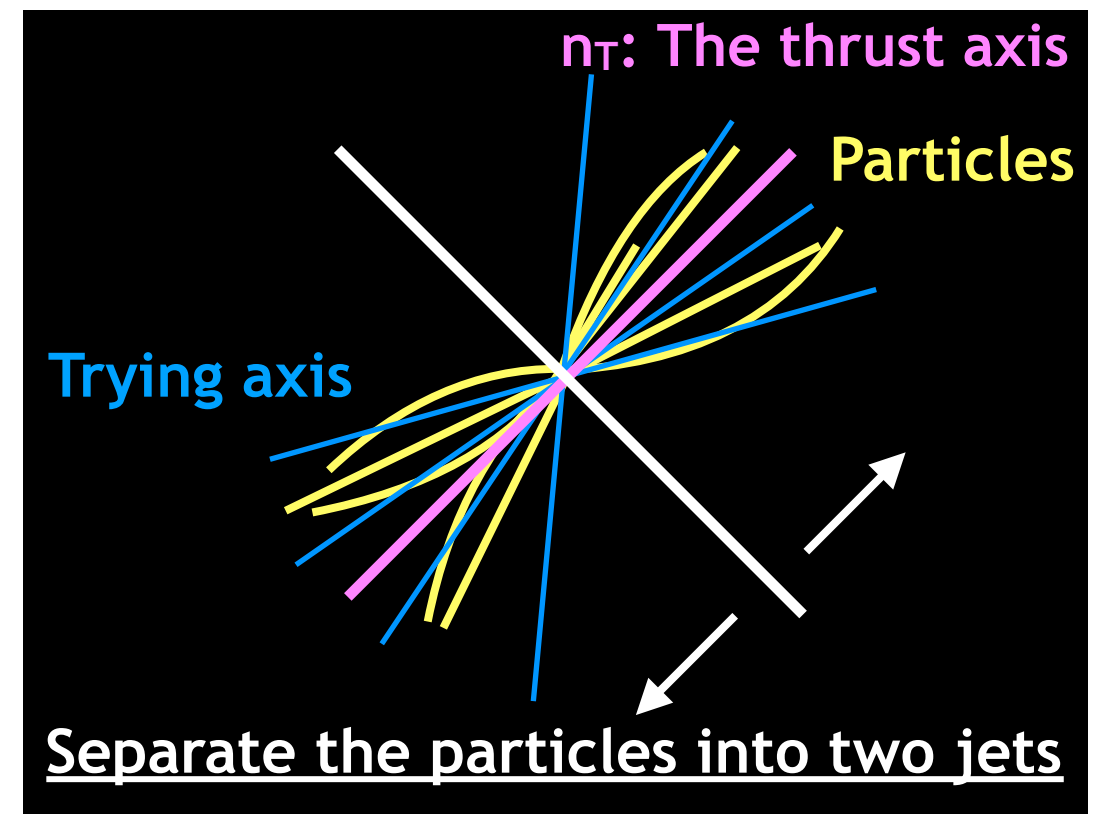
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BM3: Thrust Based Algorithm

$$T \equiv \max \frac{\sum_j^N |\underline{P_j} \cdot \underline{n_T}|}{\sum_i^N |\underline{P_i}|}$$

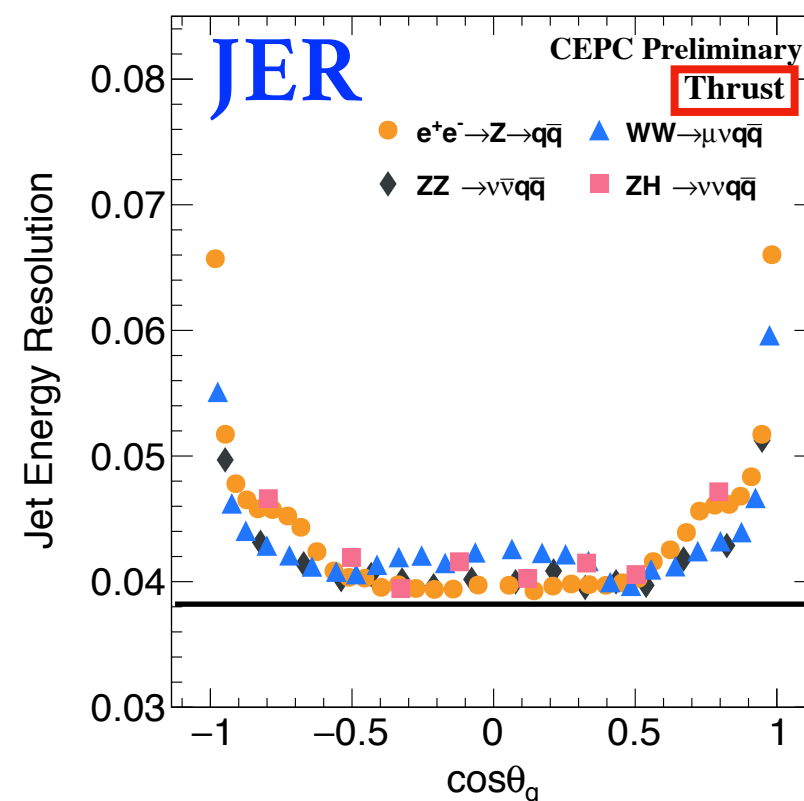
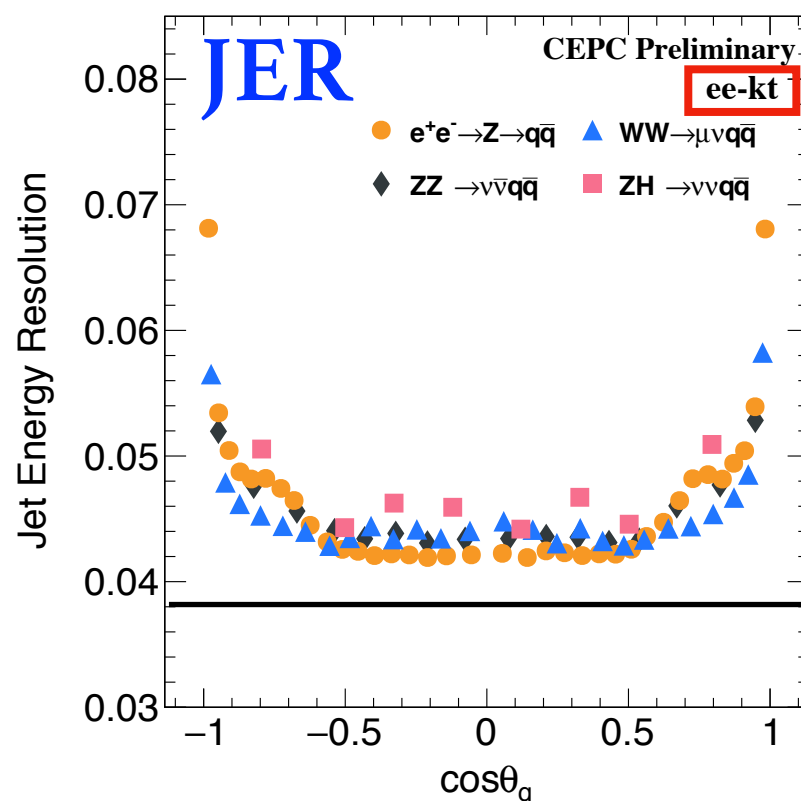
$\underline{P_i}$ or $\underline{P_j}$: Momentum of each particle

$\underline{n_T}$: A unit vector ($\sin \theta \times \cos \phi$, $\sin \theta \times \sin \phi$, $\cos \theta$)

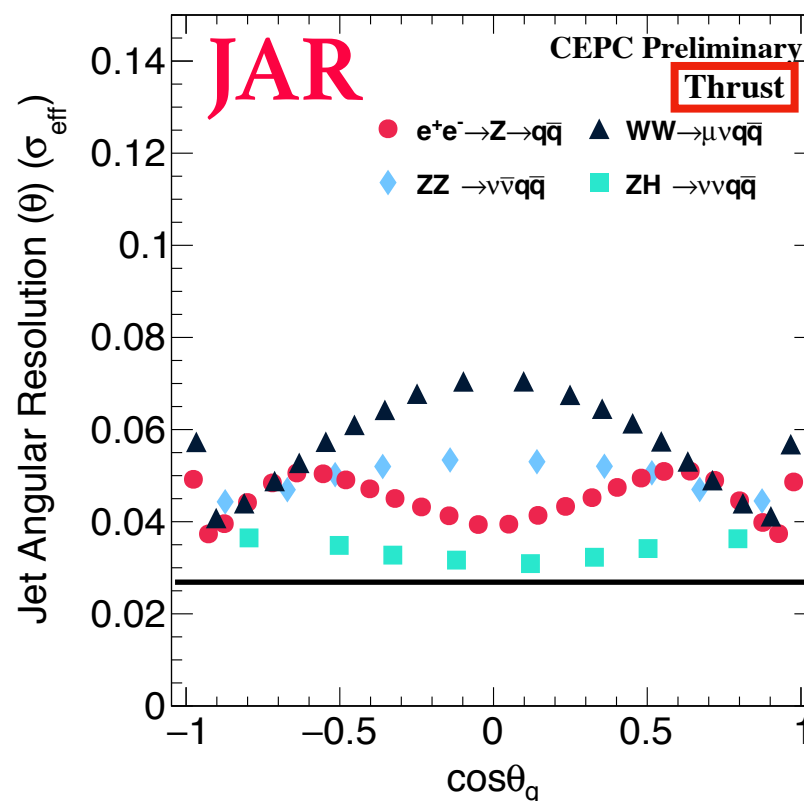
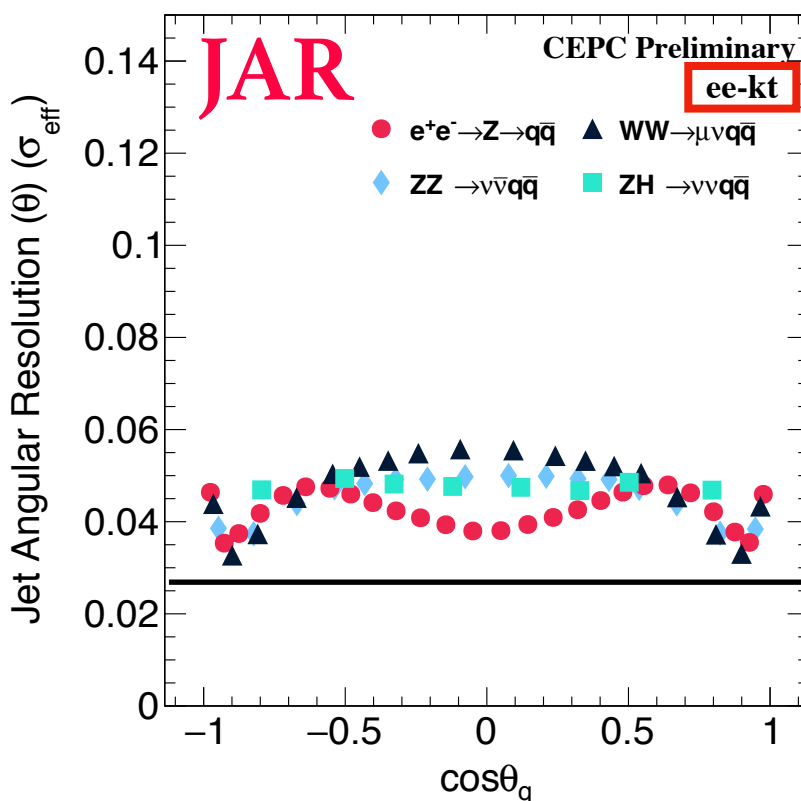


- “Thrust” is one kind of event-shape variables.
- The nature clustering idea for the **back-to-back di-jet topology**.
 1. Boost the system back to the rest frame.
 2. Find the thrust axis which has highest momentum efflux.
 3. Divide system into 2 hemispheres with the thrust axis, and each of them is identified as a jet.
- Applicable to all of **2-jet final-states** at CEPC.
 (2-jet final-states could be identified with *efficiency*×*purity* = **88.4%**.)

BM3: JER & JAR (ee- k_t – Thrust)



JERs are improved **20%** w.r.t ee- k_t



JARs are improved **20%** w.r.t ee- k_t

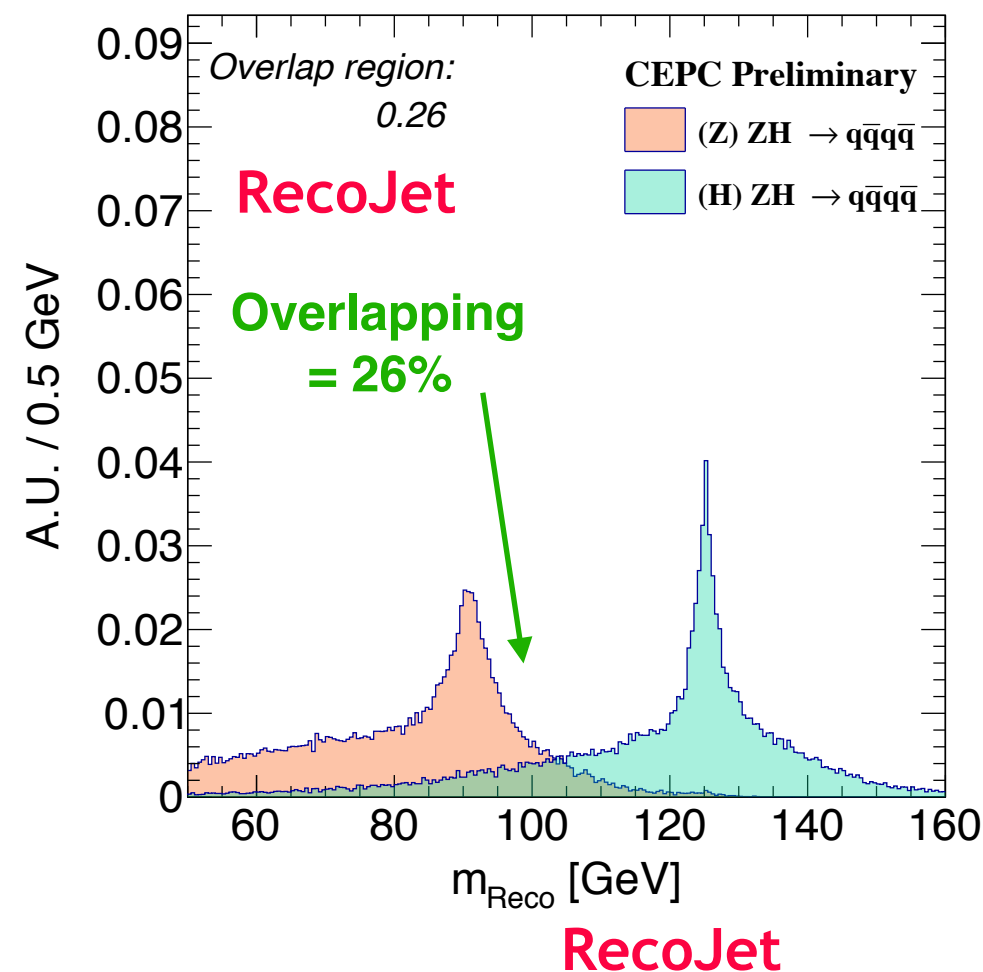
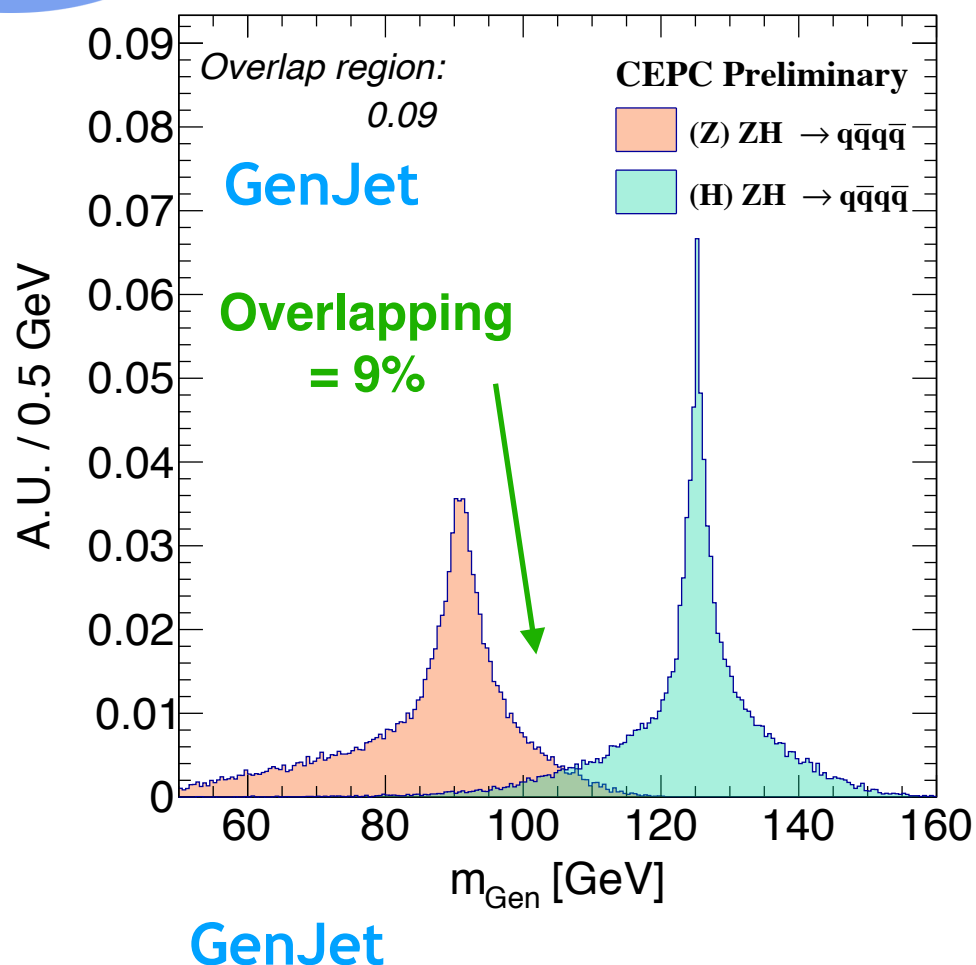
■ Improvement may come from boosting the system back to the rest frame.

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BM4: WW, ZZ, ZH to 4-jet Separation



| Sample \ Assignment(%) | WW | ZZ | ZH |
|------------------------|-------|-------|--------------|
| WW | 63.24 | 18.95 | 17.81 |
| ZZ | 16.09 | 57.89 | 26.02 |
| ZH | 9.99 | 13.84 | 76.17 |

| Sample \ Assignment(%) | WW | ZZ | ZH |
|------------------------|-------|-------|--------------|
| WW | 64.98 | 19.07 | 15.94 |
| ZZ | 26.51 | 50.54 | 22.96 |
| ZH | 20.29 | 22.93 | 56.77 |

■ χ^2 method is employed.

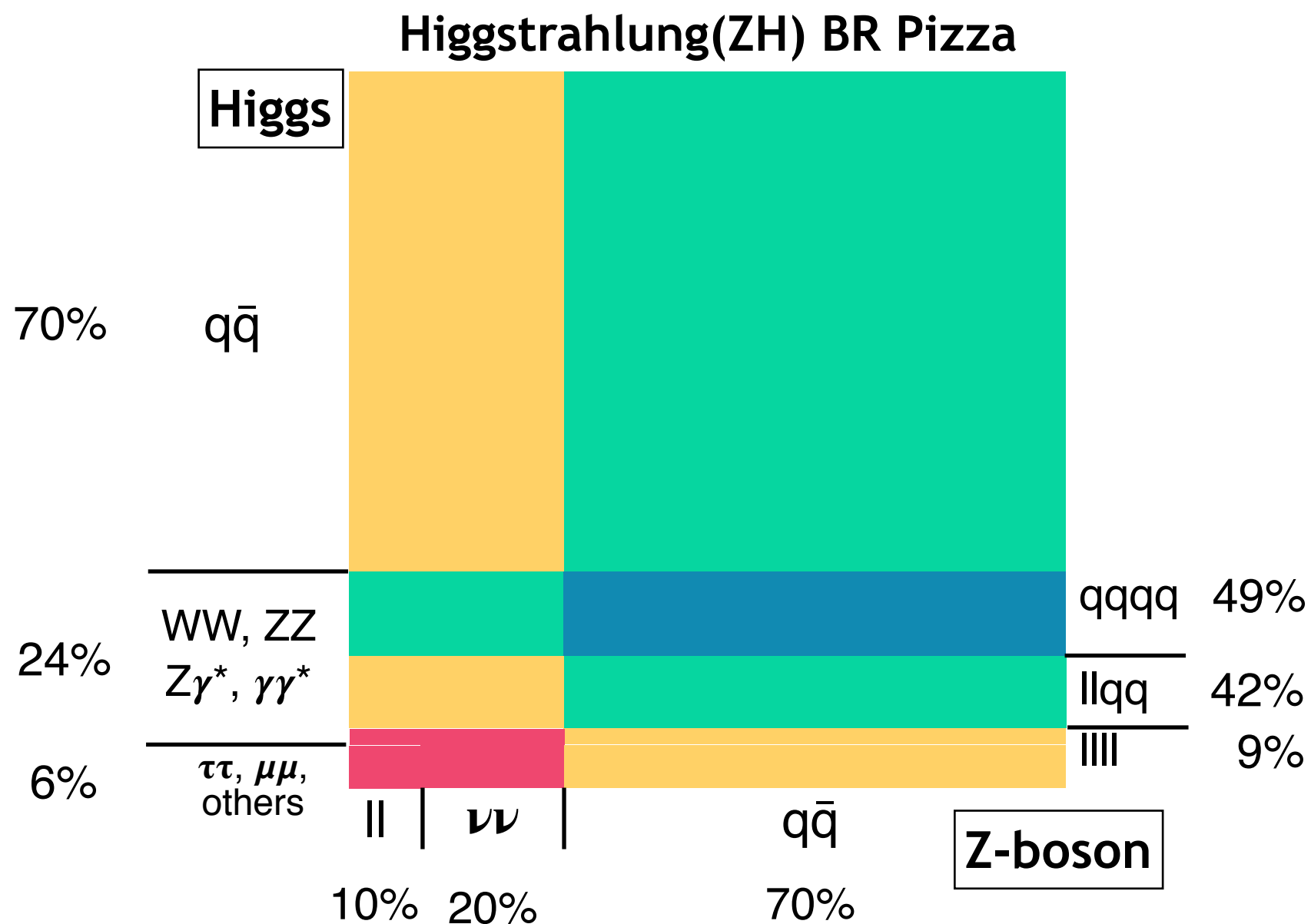
■ The *Efficiency x Purity* of ZH identification is expected **18%** in the 5 ab^{-1} data.

■ The statistical uncertainty of ZH to full hadronic final-state could achieve **0.25%** after considering the WW and ZZ as bkg.

$$\chi^2 = \frac{|(m_{ij} - m_{\text{boson}})|^2 + |(m_{ij} - m_{\text{boson}})|^2}{\sigma^2}$$

■ Jets are crucial for the CEPC Higgs physics

- **97%** of ZH events involve jets
- 1/3 of ZH events only come from single Z or Higgs boson.
- 2/3 of ZH events have more than one boson (e.g. $ZH \rightarrow q\bar{q}q\bar{q}$) - need **color singlet identification algorithm**.



| # of jets | Probability | |
|-----------|-------------|-----|
| 0 | 2.44% | 1/3 |
| 2 | 29.73% | |
| 4 | 59.58% | 2/3 |
| 6 | 8.23% | |

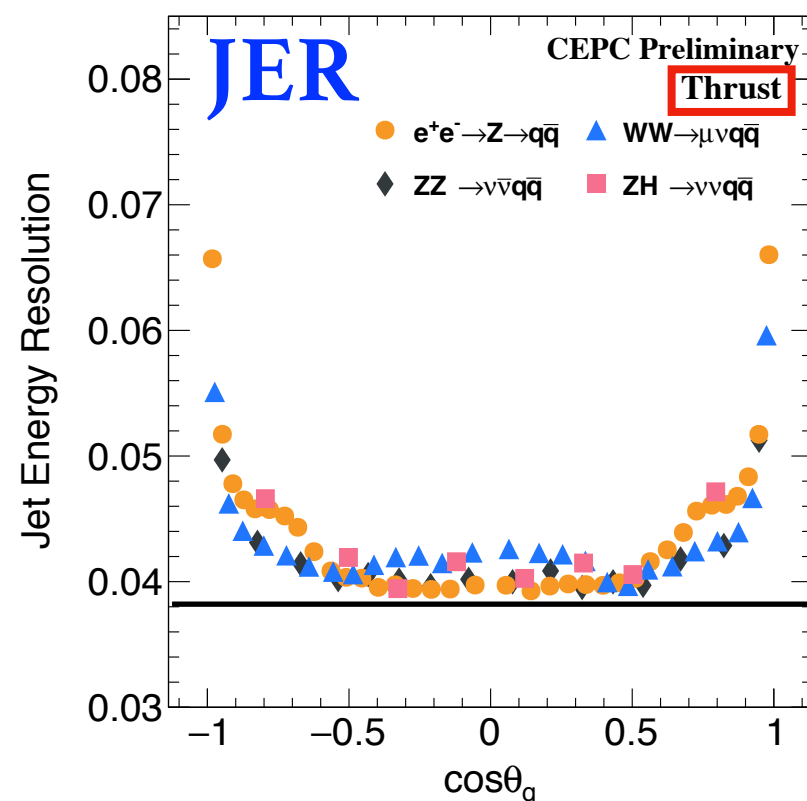
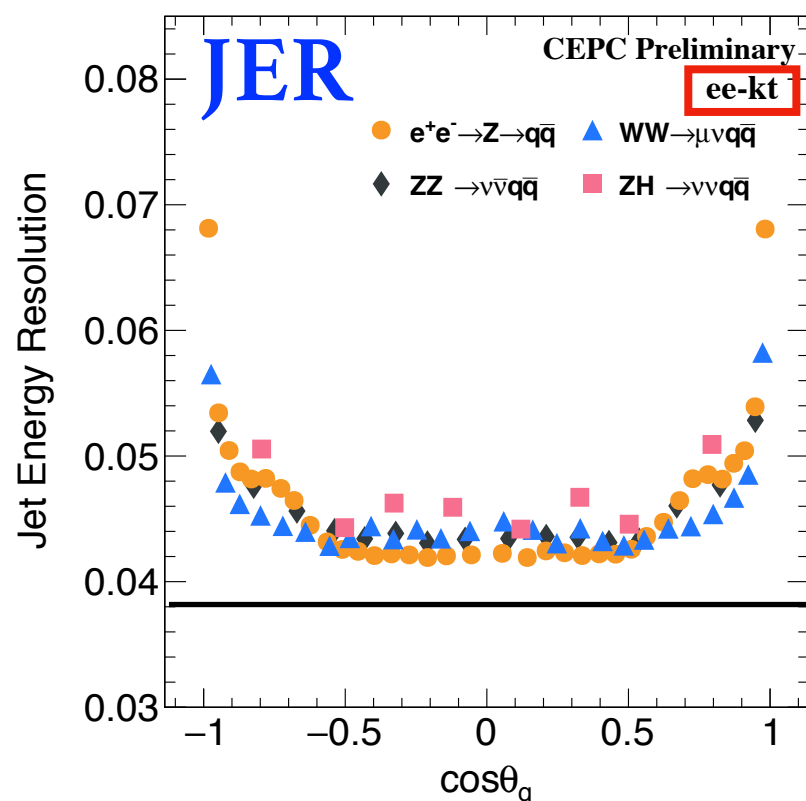
~ 97% with Jets

- I. **BMR < 4% is critical. Achieved at the CEPC baseline (3.8%)**
 - * W, Z, Higgs boson can be efficiently separated at both semi-leptonic & full hadronic final-state.
 - * Exploit Z-boson di-jet recoil mass to distinguish the ZH from ZZ process (main background).
- II. Jet energy resolution ~ **3-5%** & Jet angular resolution ~ **1%**.
- III. 2-jet final-states could be identified with *efficiency*×*purity* = **88.4%**.
 - * Clustering by dedicated the jet clustering algorithm, **thrust based algorithm**.
 - * Thrust based algorithm is recommended for 2-jet final-states because it brings the JER and JAR **20%** improvement.
- IV. Need a better color-singlet identification algorithm for full hadronic final-state.
 - * The statistical uncertainty of ZH to full hadronic final-state is expected to be **0.25%** currently when considering the WW and ZZ as background.

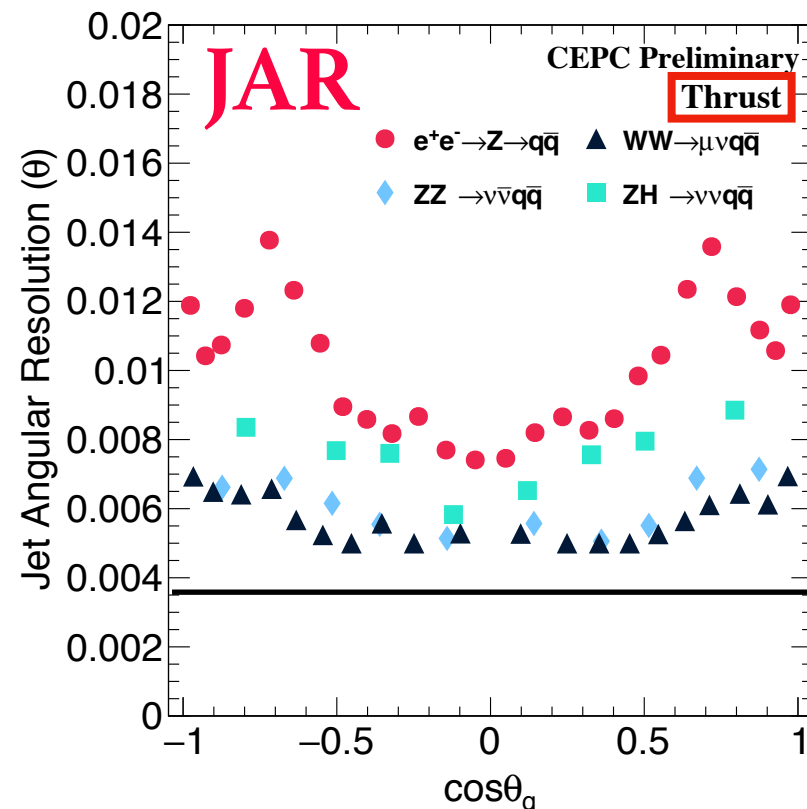
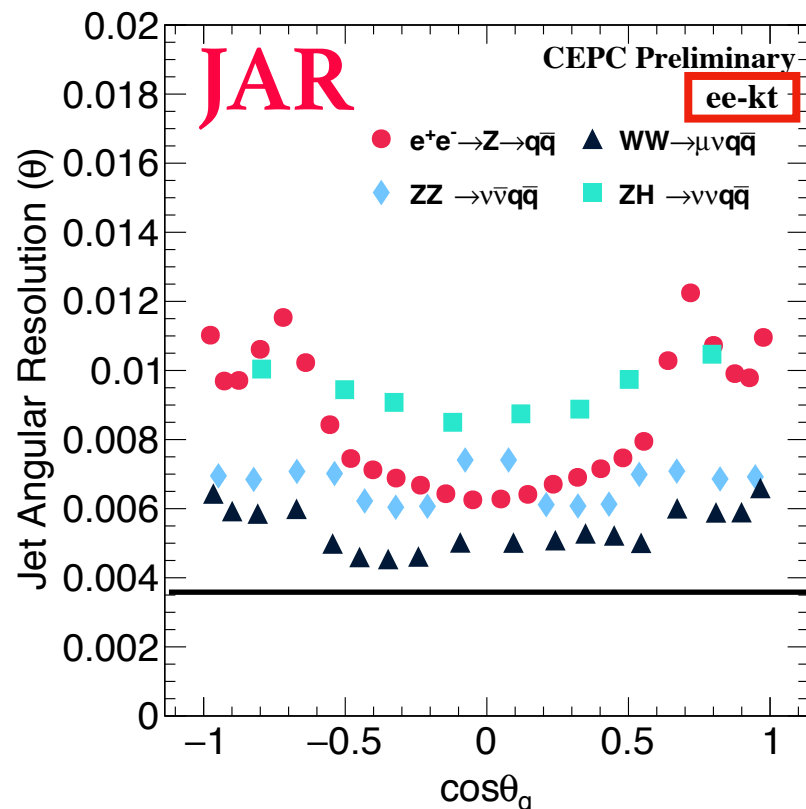
Thank for your attention



BM3: JER & JAR (ee- k_t – Thrust)



JERs are improved **20%** w.r.t ee- k_t



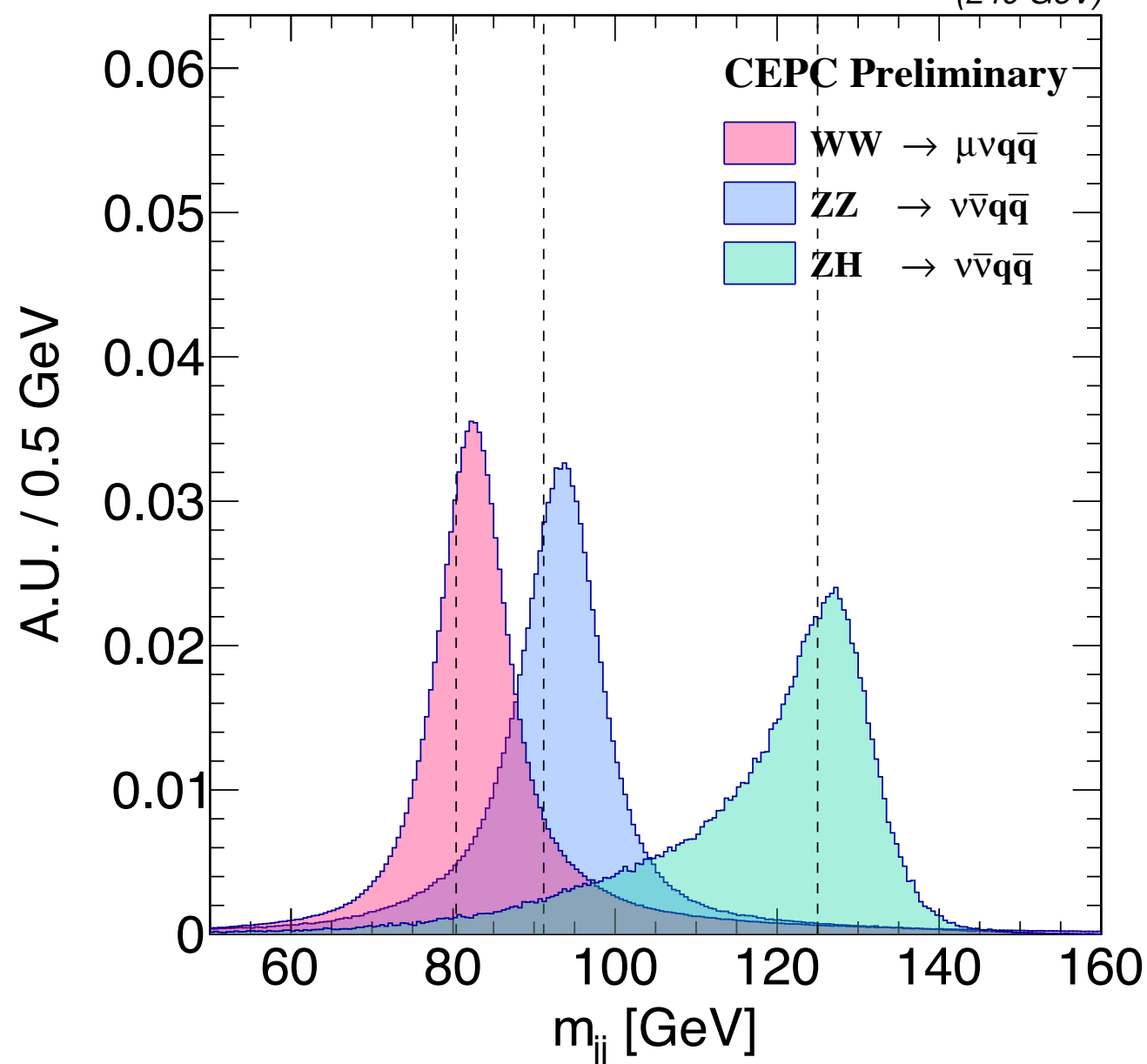
JARs are improved **20%** w.r.t ee- k_t

■ Improvement maybe came from boosting the system back to the rest frame with the neutrons' information.

Jet Energy Calibration

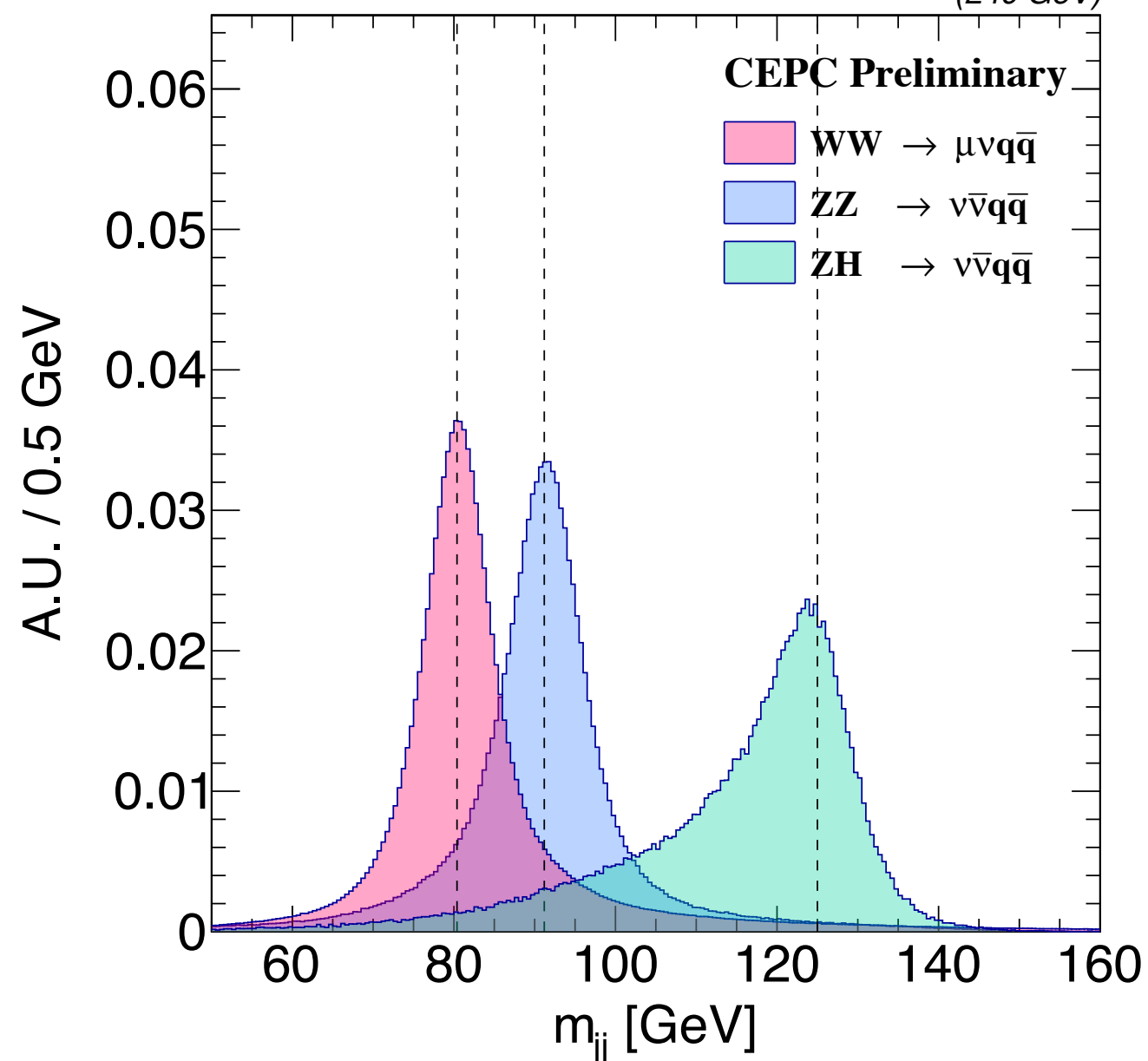
Before Calibration

(240 GeV)



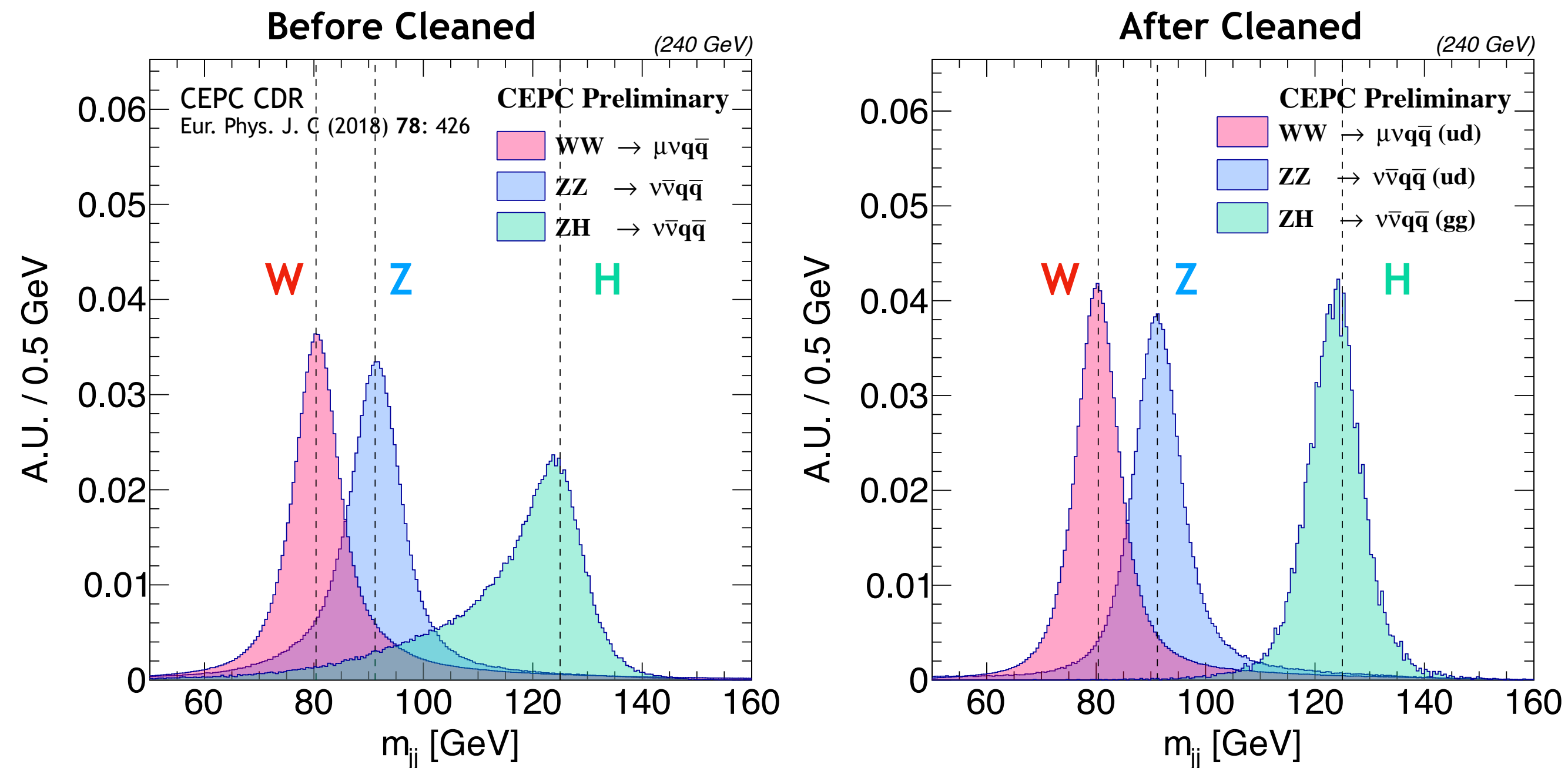
After Calibration

(240 GeV)



- Since the double-counting effect, jet energy would be overestimated.
- According to MC true energy and $\cos\theta$ distribution, JES can be used to calibrate the dijet invariant mass back to the value we put into simulation.
- After calibration, boson mass resolution is improved about **1%**.

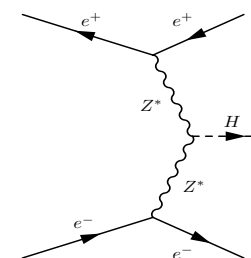
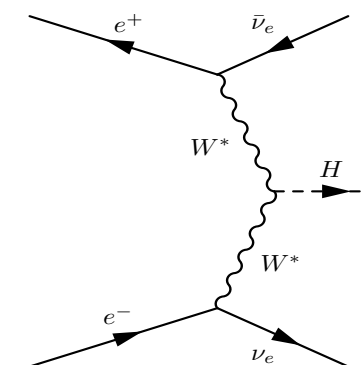
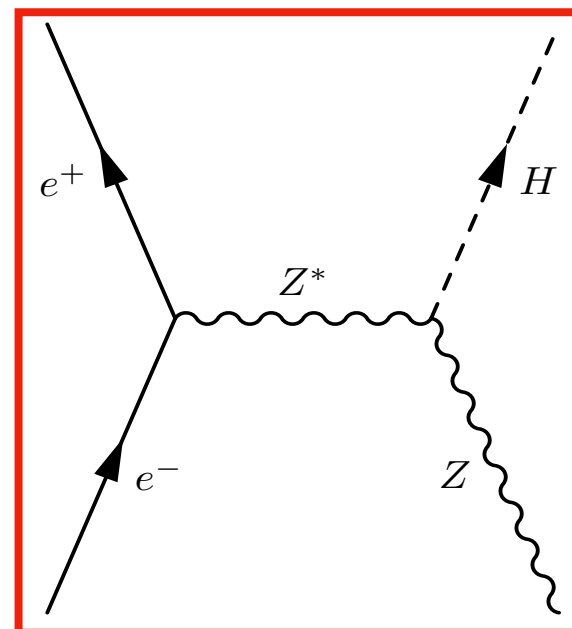
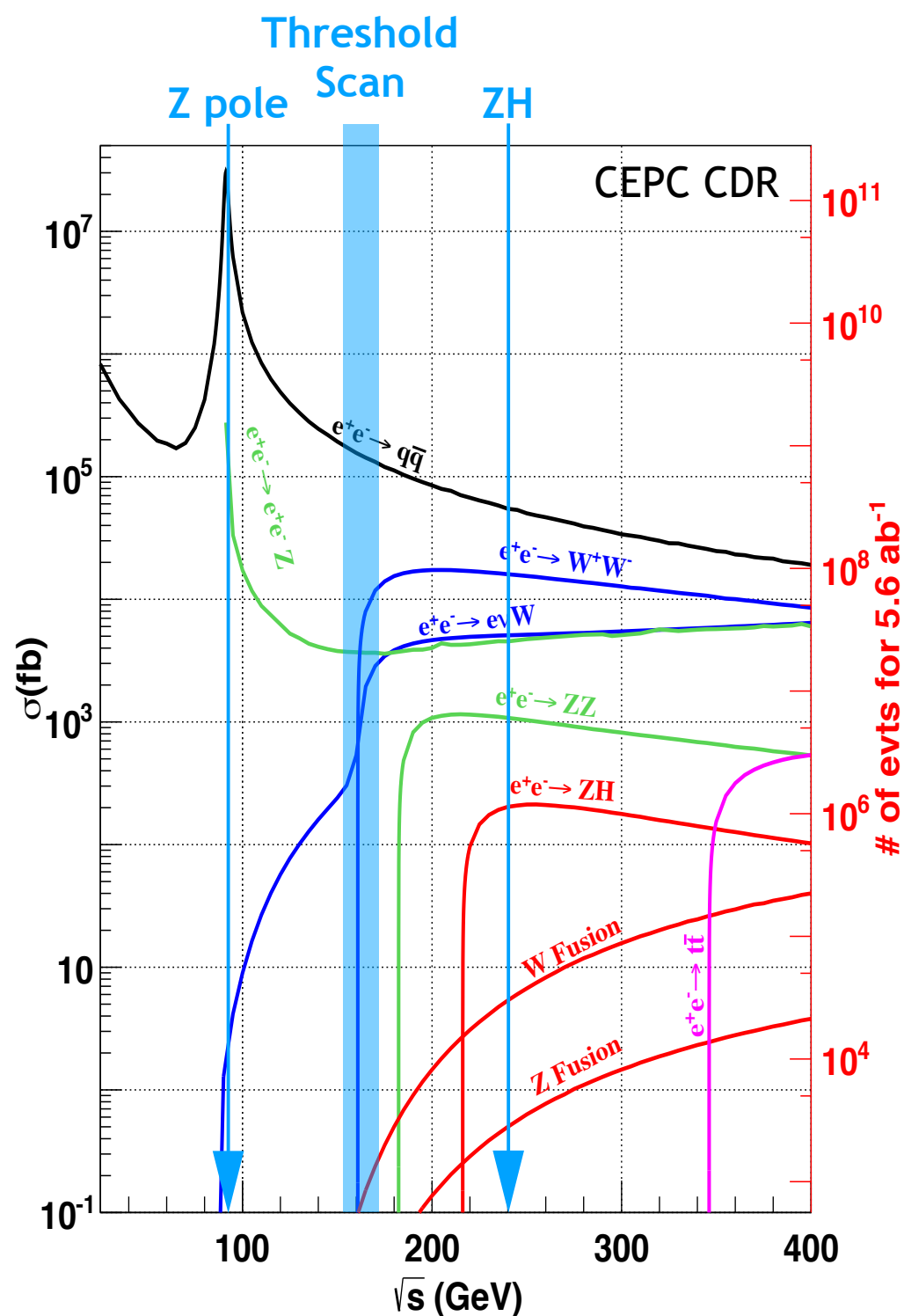
BM1: Massive Boson Mass Resolution



- **W-, Z-, and Higgs-boson masses in dijet final state can be well separated at CEPC.**
- After cleaned, Z- and W-boson could be separated $\approx 2\sigma$, and the Higgs **Boson Mass Resolution = 3.8%** achieving the CEPC baseline.

Cleaned: Select the light flavor jet event with low energy ISR, low energy neutrino inside jet, and within $|\cos\theta| < 0.85$.

Higgs Production at CEPC



| Process | Cross section(fb) | Events in 5.6 ab^{-1} |
|--|-------------------|--------------------------------|
| $e^+e^- \rightarrow ZH$ | 196.2 | 1.10×10^6 |
| $e^+e^- \rightarrow \nu_e \bar{\nu}_e H$ | 6.19 | 3.47×10^4 |
| $e^+e^- \rightarrow e^+e^- H$ | 0.28 | 1.57×10^3 |
| Total | 203.7 | 1.14×10^6 |

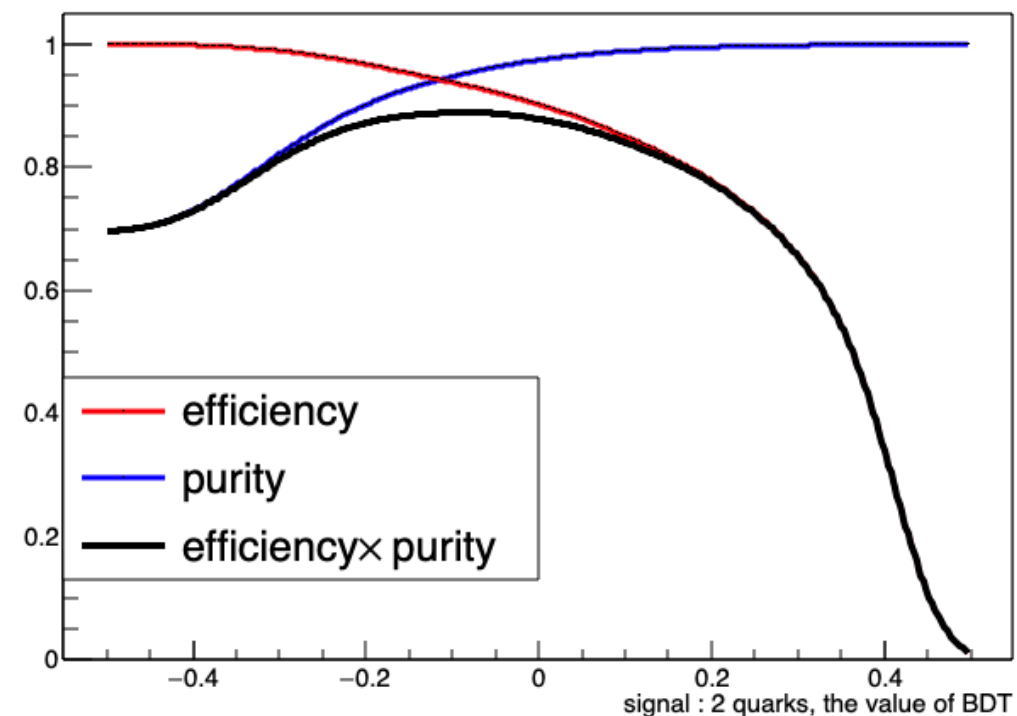
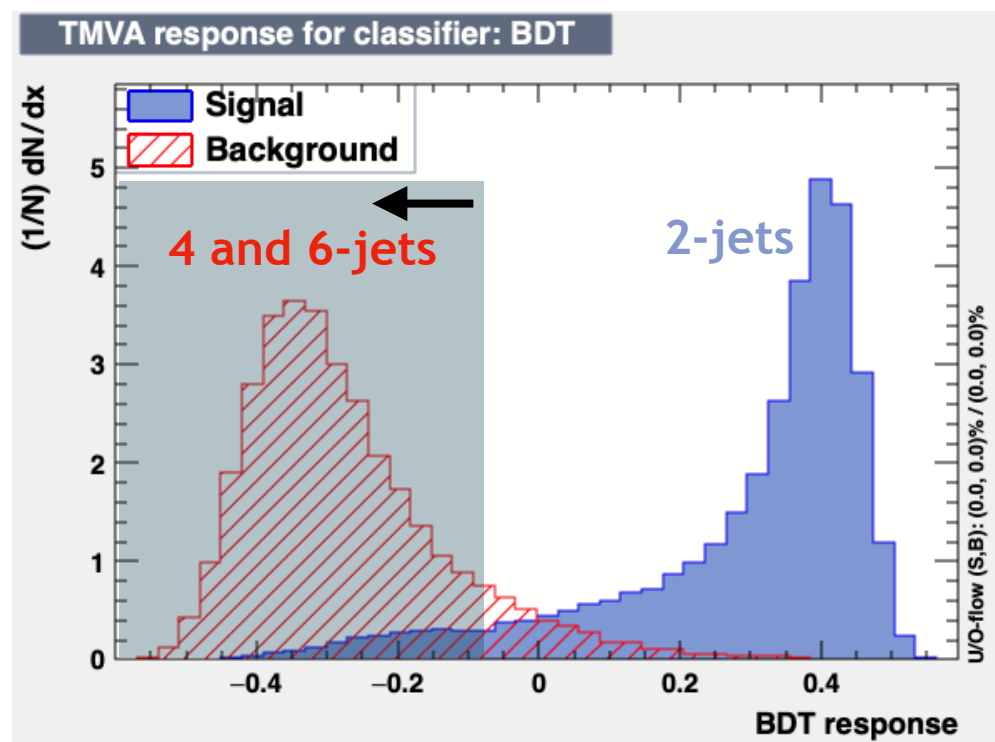
$$S : B = 1 : (100 \sim 1000)$$

- Observables: Higgs mass, CP, $\sigma(ZH)$, event rate ($\sigma(ZH, \nu\nu H) \cdot \text{Br}(H \rightarrow X)$), Diff. distributions
 → Absolute Higgs width, branching ratio, couplings



BM2: Preliminary Number of Jet Identification

Yong-Feng Zhu



Samples:

$e^+e^- \rightarrow q\bar{q}$ (2 jets)
 $ZZ \rightarrow q\bar{q}q\bar{q}$ (4 jets)
 $W^+W^- \rightarrow q\bar{q}q\bar{q}$ (4 jets)
 $ZH \rightarrow q\bar{q}q\bar{q}$ (4 jets)
 $ZH \rightarrow q\bar{q}H \rightarrow qq\bar{q}\bar{q}qq$ (6 jets)

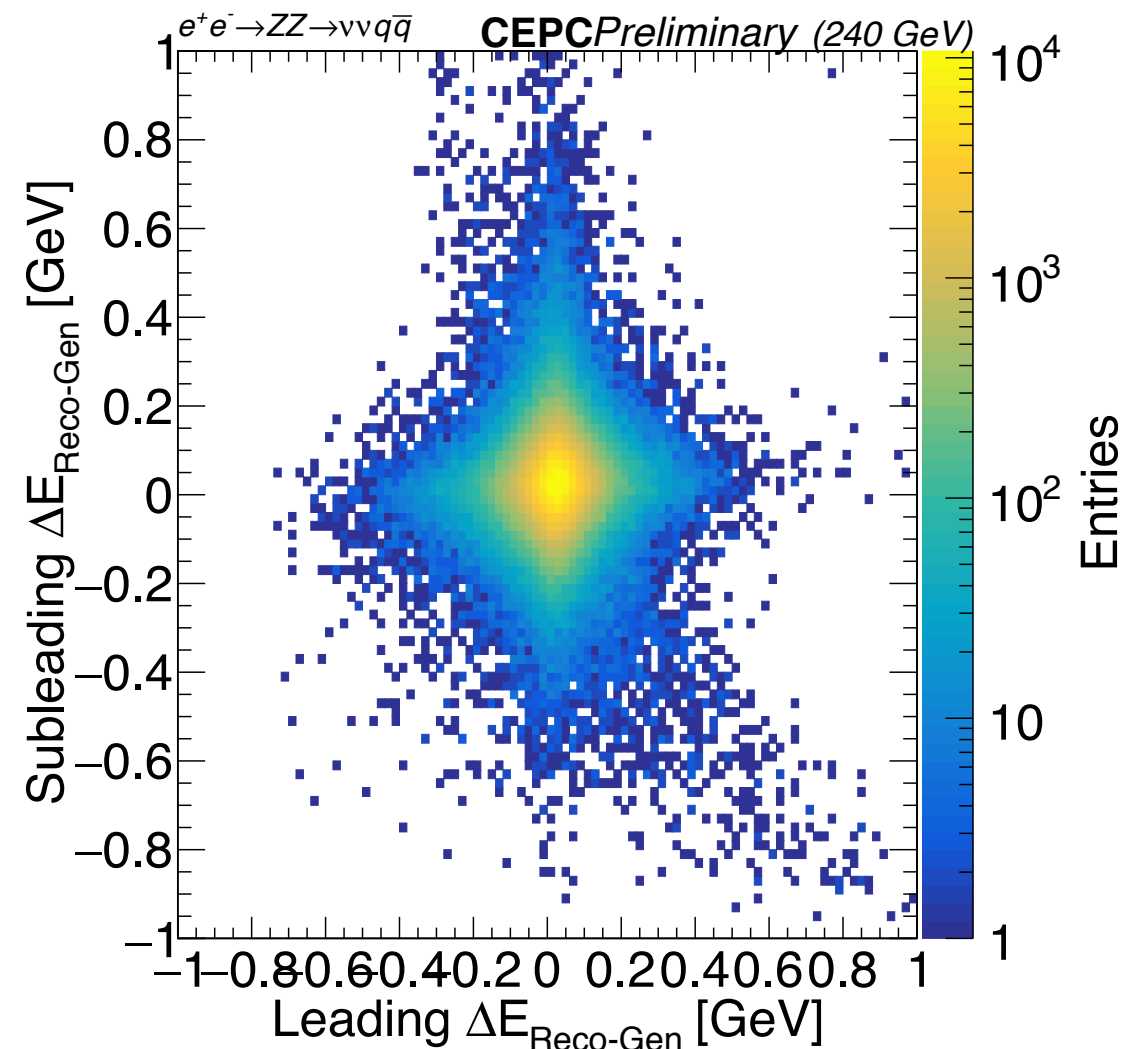
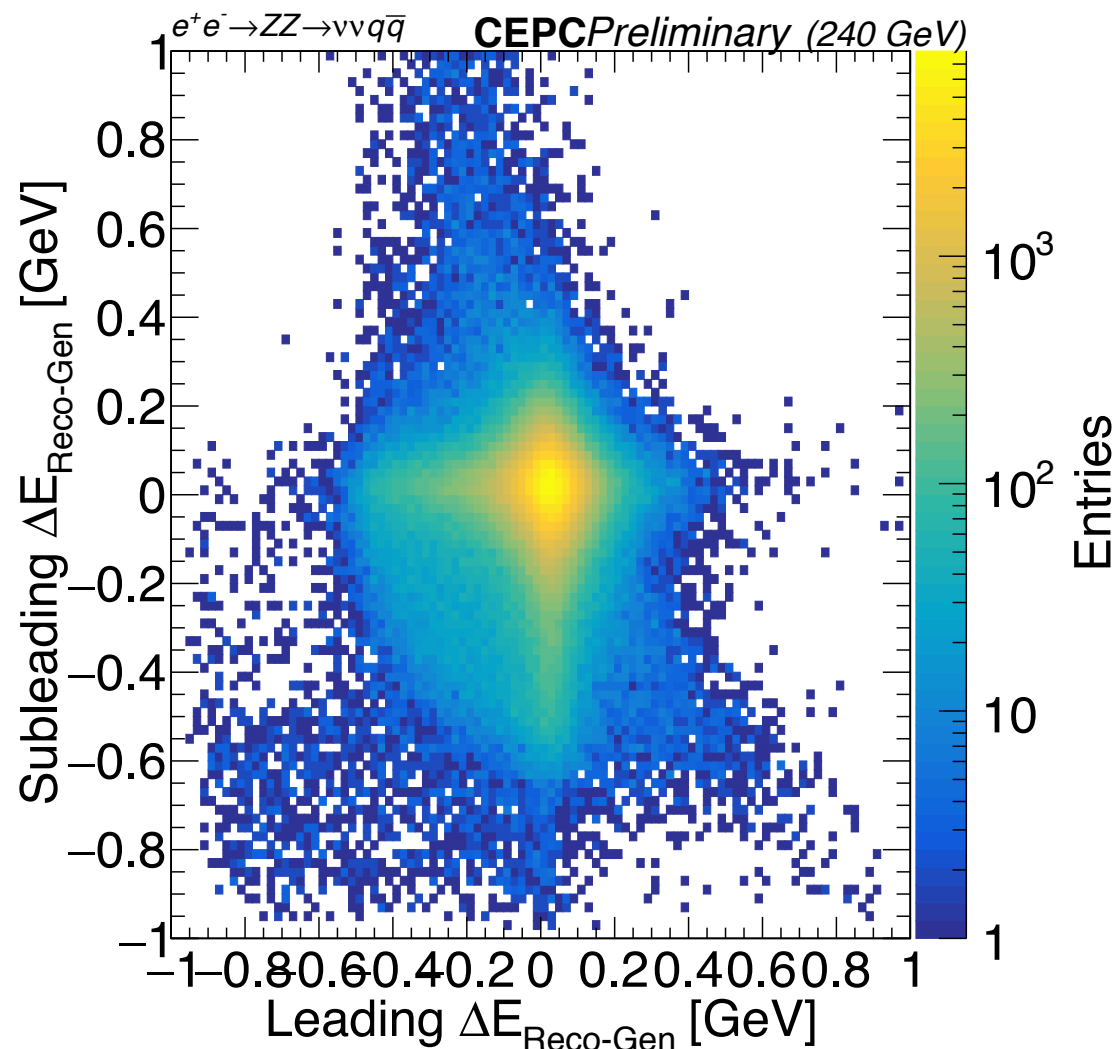
| Signal | <i>Efficiency \times Purity</i> |
|--------|--|
| 2 jets | 88.4% |
| 6 jets | 1.8% |

20 event-shape variables are combined with the multi-variate analysis (MVA) to separate 2, 4, and 6 jets final-states.

BM3: Thrust Jet Clustering Method

ee-kt

Thrust

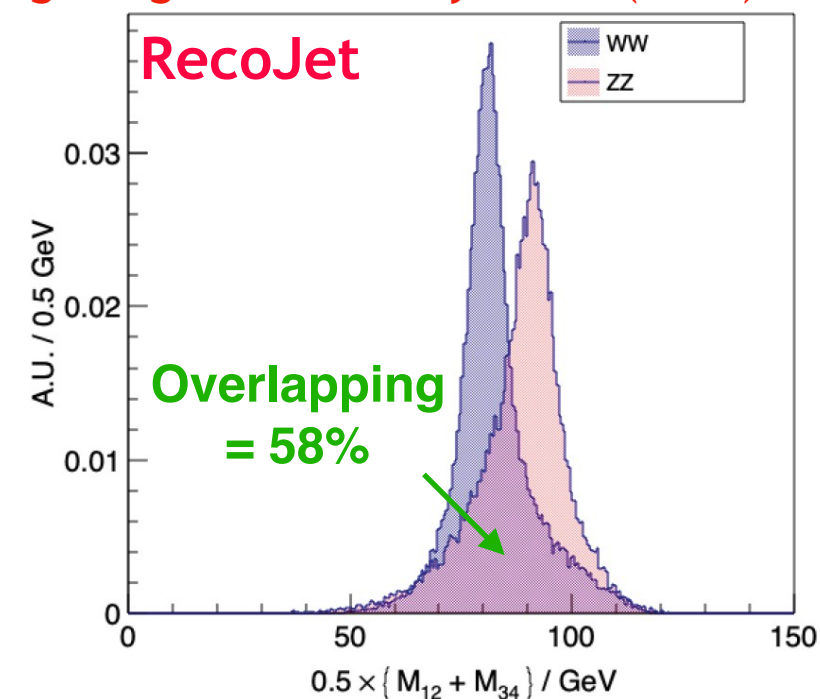
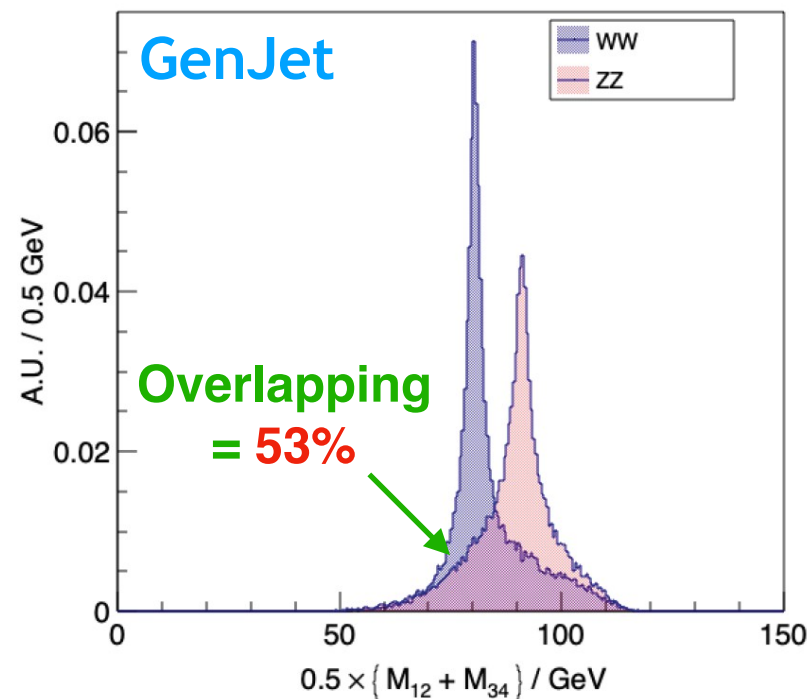
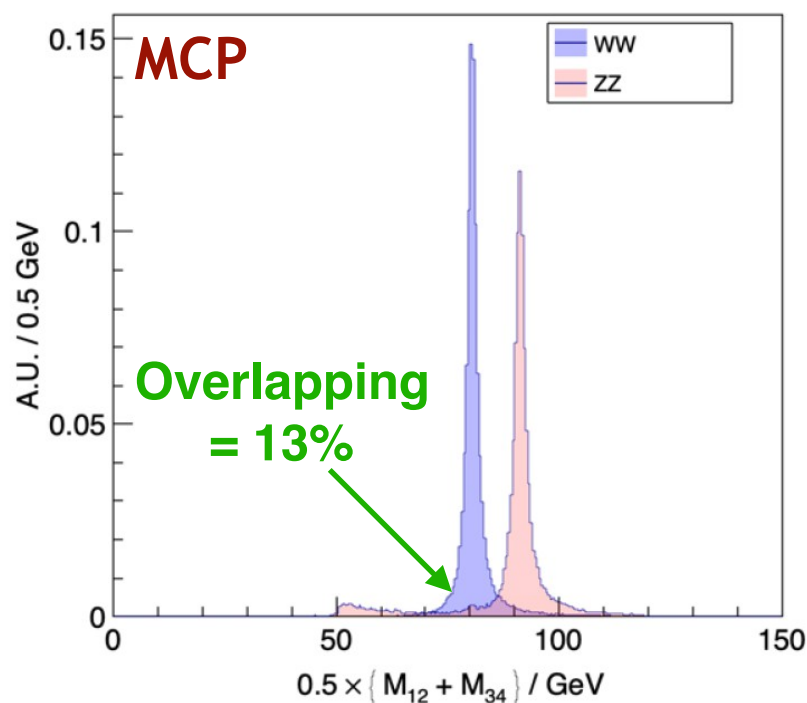


- Identify the 2 jets final-state event with (Efficiency x Purity) = **88.4%**, the thrust jet clustering method could be employed.
- After “cleaned” selection, the thrust method has **significant tail suppressed**
→ expected to have improvement on jet energy and angular response.

Cleaned: Select the light flavor jet event with low energy ISR, low energy neutrino inside jet, and within $|\cos\theta| < 0.85$.

BM4: WW & ZZ to 4 Jets Separation

Yong-Feng Zhu—Eur. Phys. J. C (2019) 79:274



■ Low energy jet (20-120 GeV)

■ Typical multiplicity could be 10^2 .

■ GenJet and RecoJet are clustered by ee-kt and paired according to χ^2 .

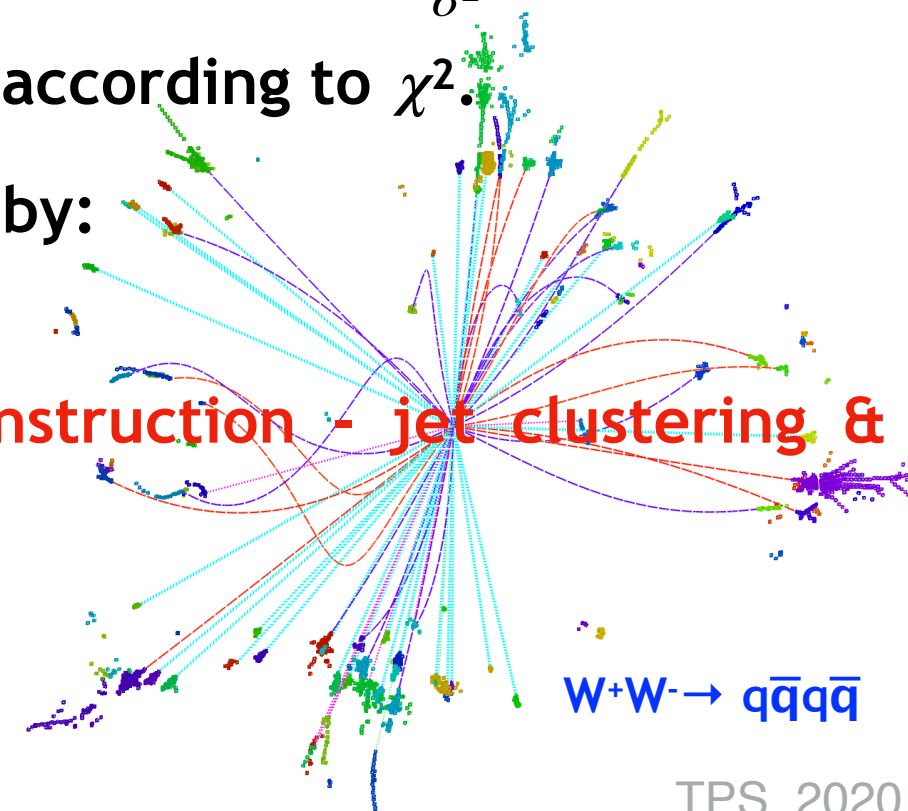
■ WW & ZZ to 4 jets final-state separation is determined by:

1. (13%) Intrinsic boson mass/width (10 GeV)
2. (53%) Wrong jet pairing for color singlet reconstruction - jet clustering & pairing.
3. (58%) Detector response

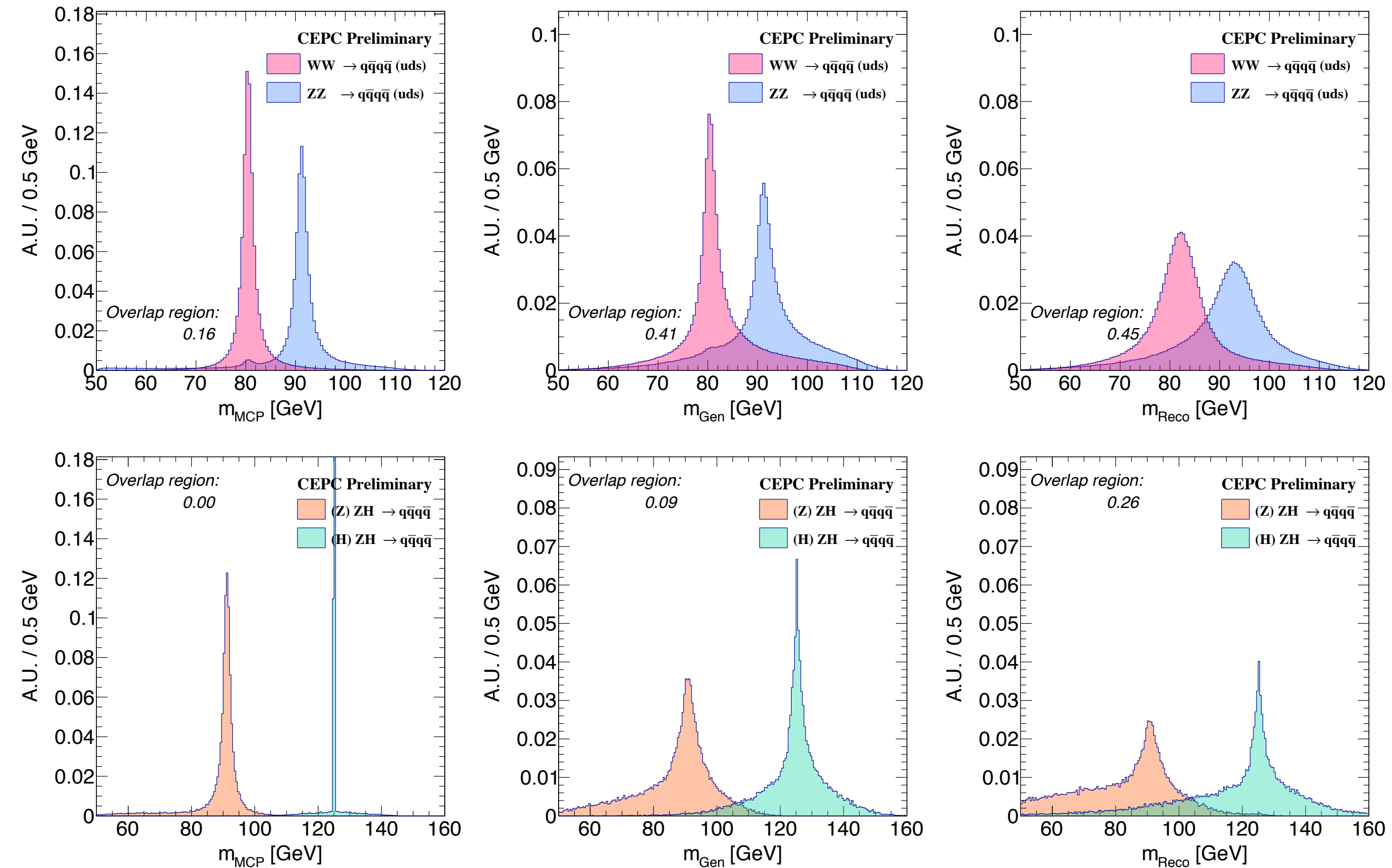
40%

5%

$$\chi^2 = \frac{|(m_{ij} - m_{boson})|^2 + |(m_{ij} - m_{boson})|^2}{\sigma^2}$$

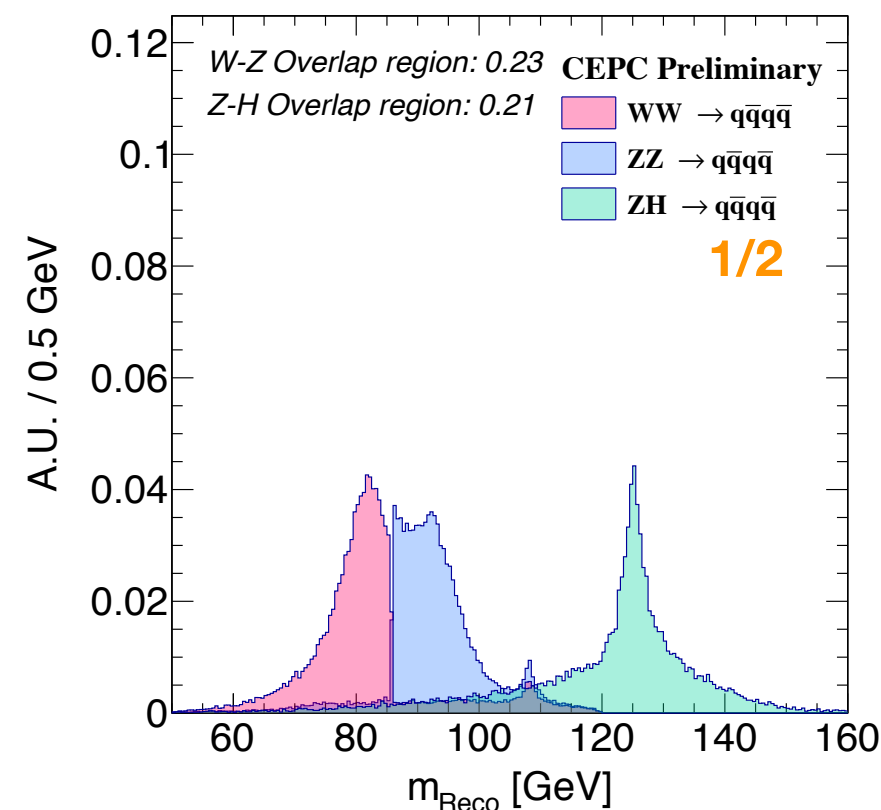
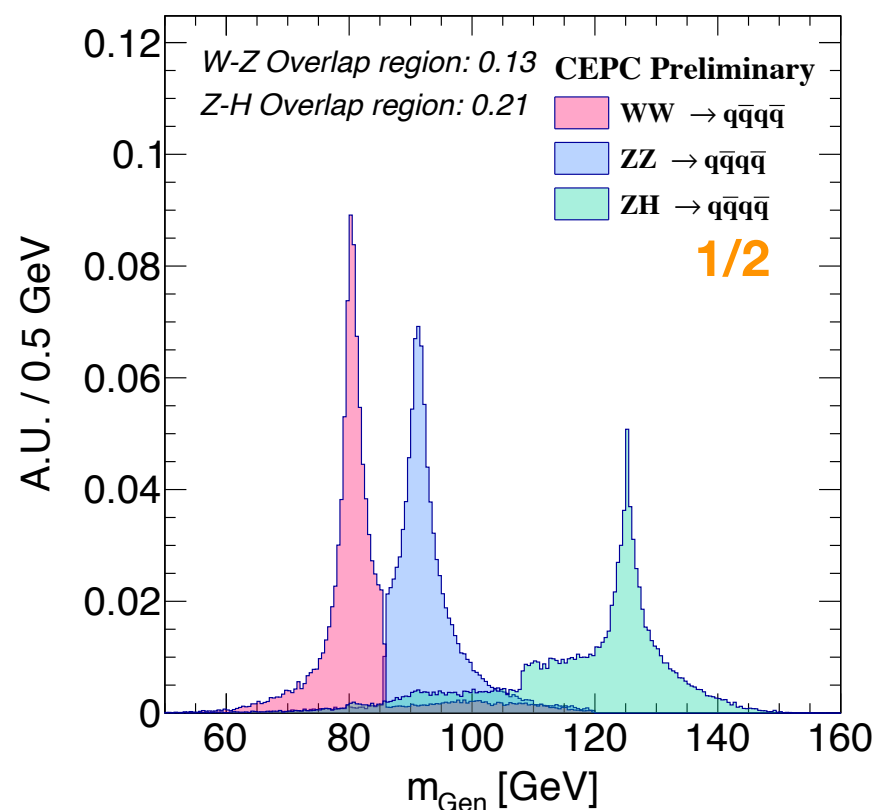
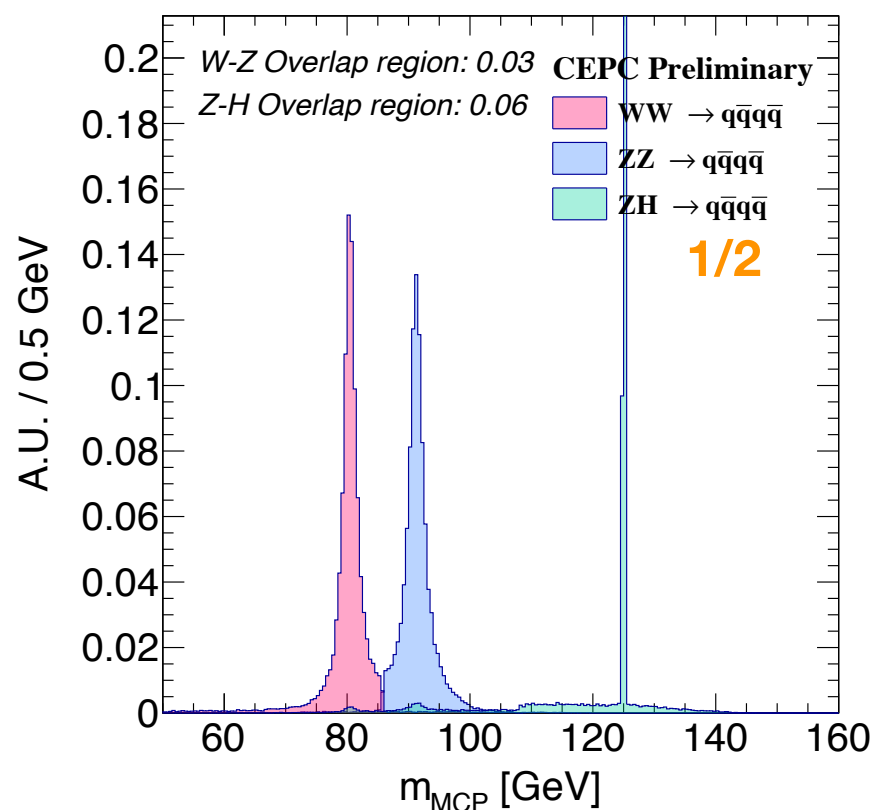
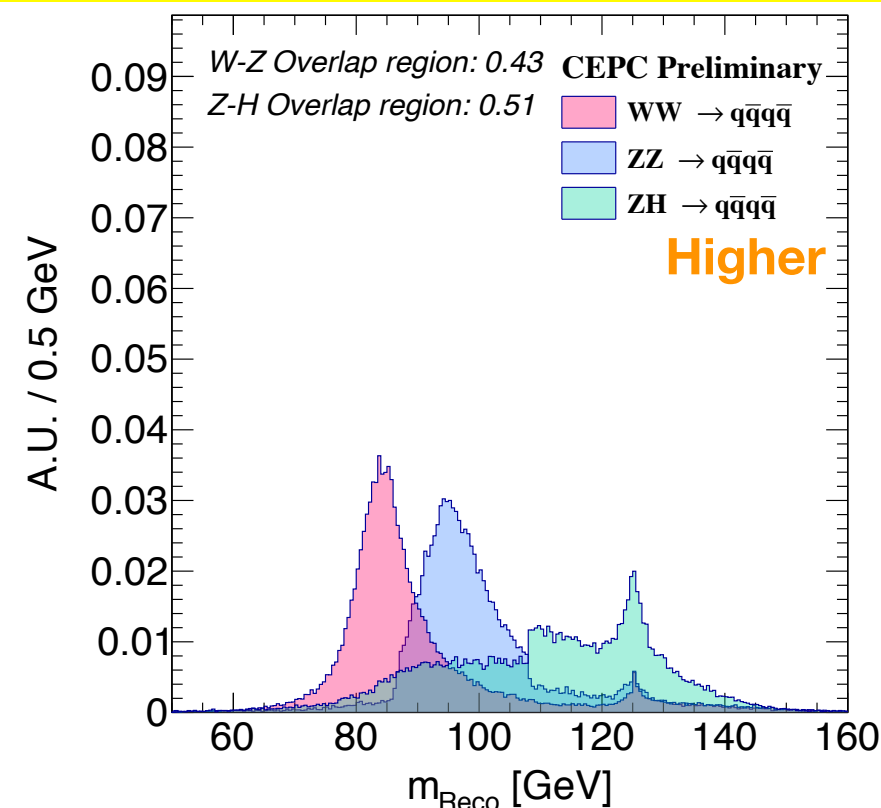
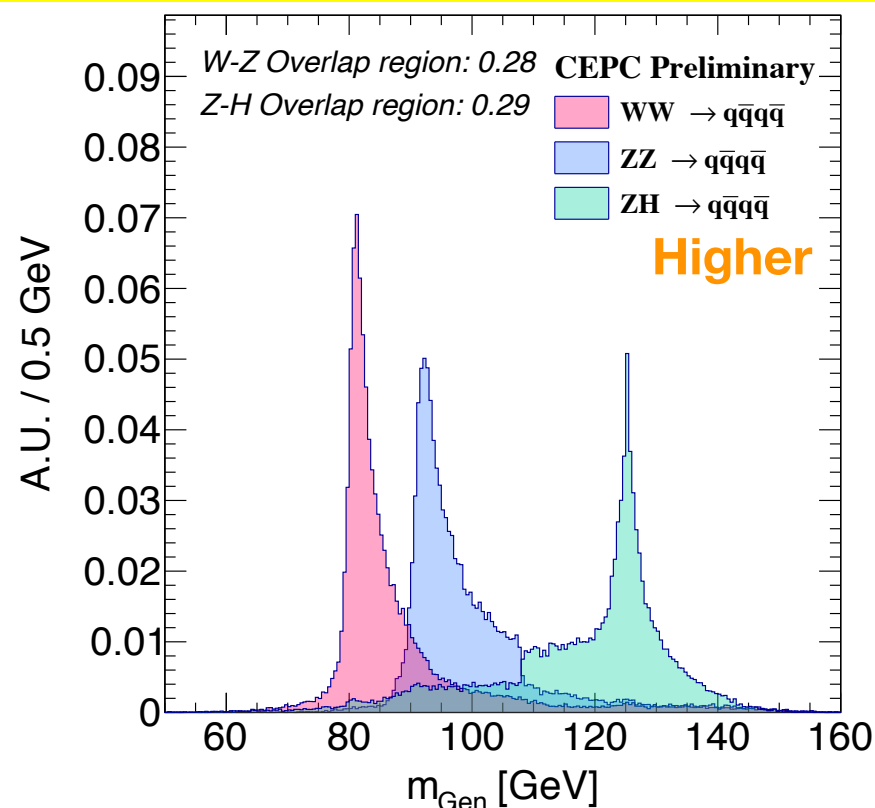
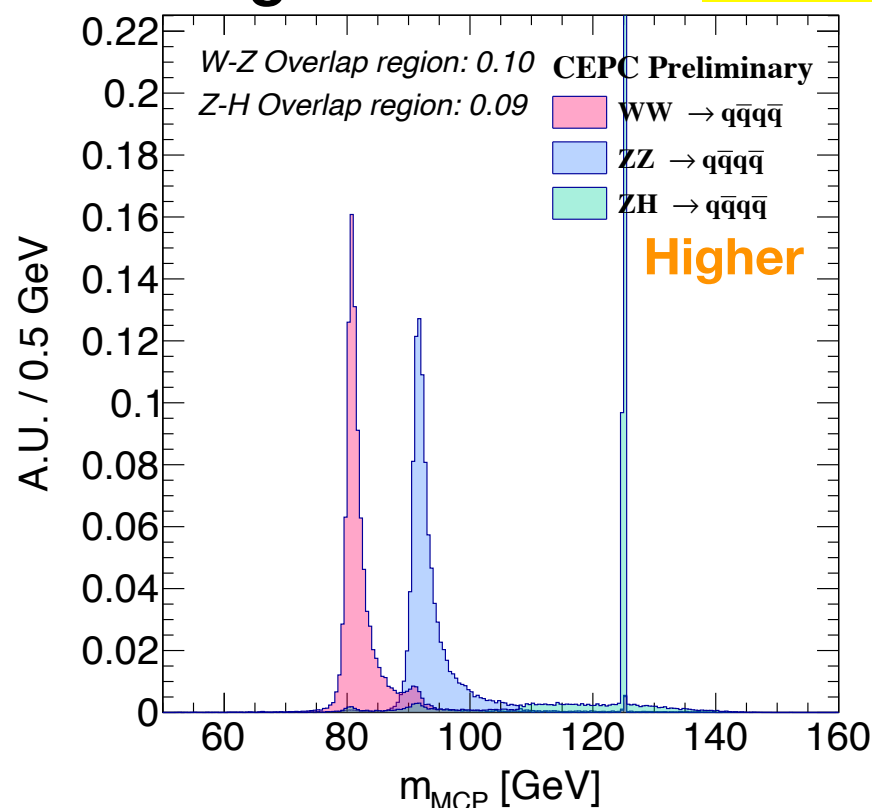


WW, ZZ, and ZH Full Hadronic



Mixing Signal & BKG

WW, ZZ, ZH Full Hadronic Separation



First Row: After reconstructed m_1 , m_2 , higher one would be chosen

Second Row: After reconstructed m_1 , m_2 , and then $(m_1 + m_2) / 2$. (Higgs still chosen the higher one)

BM4:ZH Full Hadronic Identification

- According to the final results, the following estimation could be declared:
The identified efficiency of ZH signal is 60% with background, 20% ZZ and 10% WW.
The cross section of ZZ is 5 times amount than ZH, 10 times from WW.

| | Efficiency | XS | | | |
|----|------------|----|---|-----|------------------------------------|
| WW | 10% | 10 | → | 100 | Purity → 60/200 = 30% |
| ZZ | 20% | 5 | → | 100 | |
| ZH | 60% | 1 | → | 60 | |

Efficiency x Purity

$$60\% \times 30\% = 18\%$$

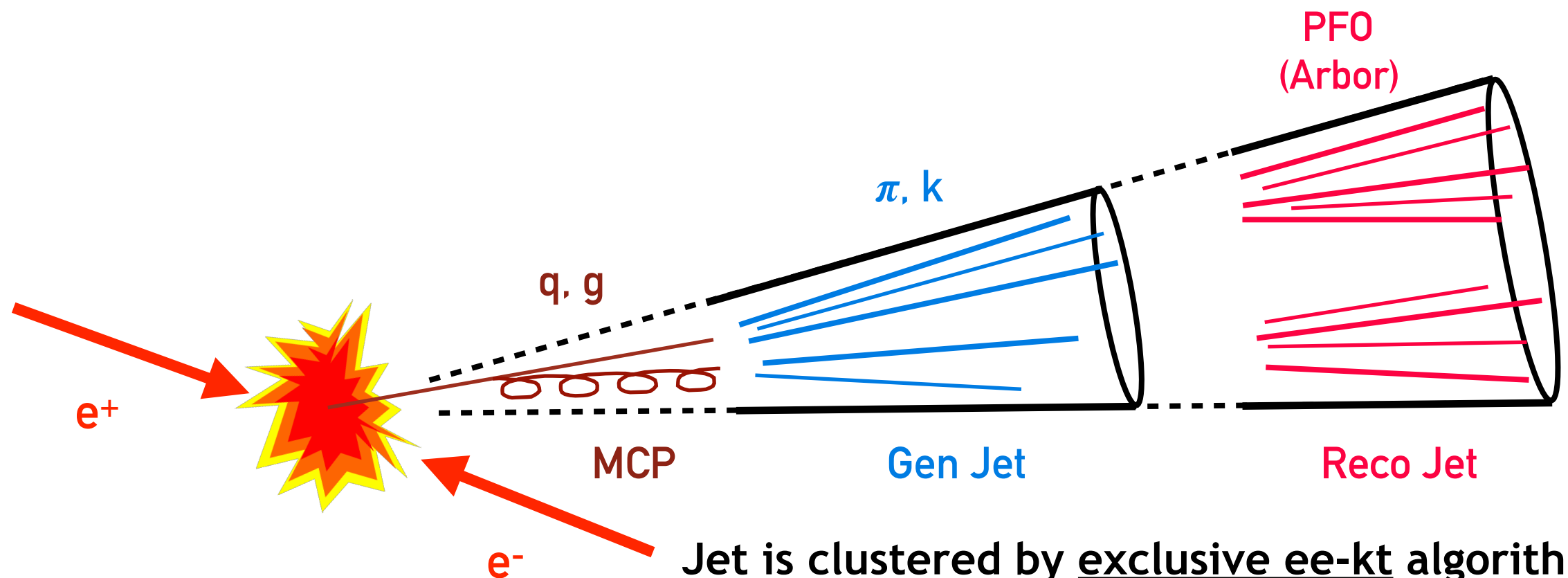


of ZH = 500,000 in the 5 ab⁻¹

500,000 x 18% = 150,000 could be identified

$$1 / \text{sqrt}(150,000) = 0.25\%$$

- **MCP** represents initial parton of MC quark. The original state of quark.
- **GenJets** are grouped all MC particles except neutrinos with $c\tau > 1$ cm through exclusive ee-kt jet clustering algorithm.
- **RecoJets** are grouped with the particle flow objects by exclusive ee-kt jet clustering algorithm.

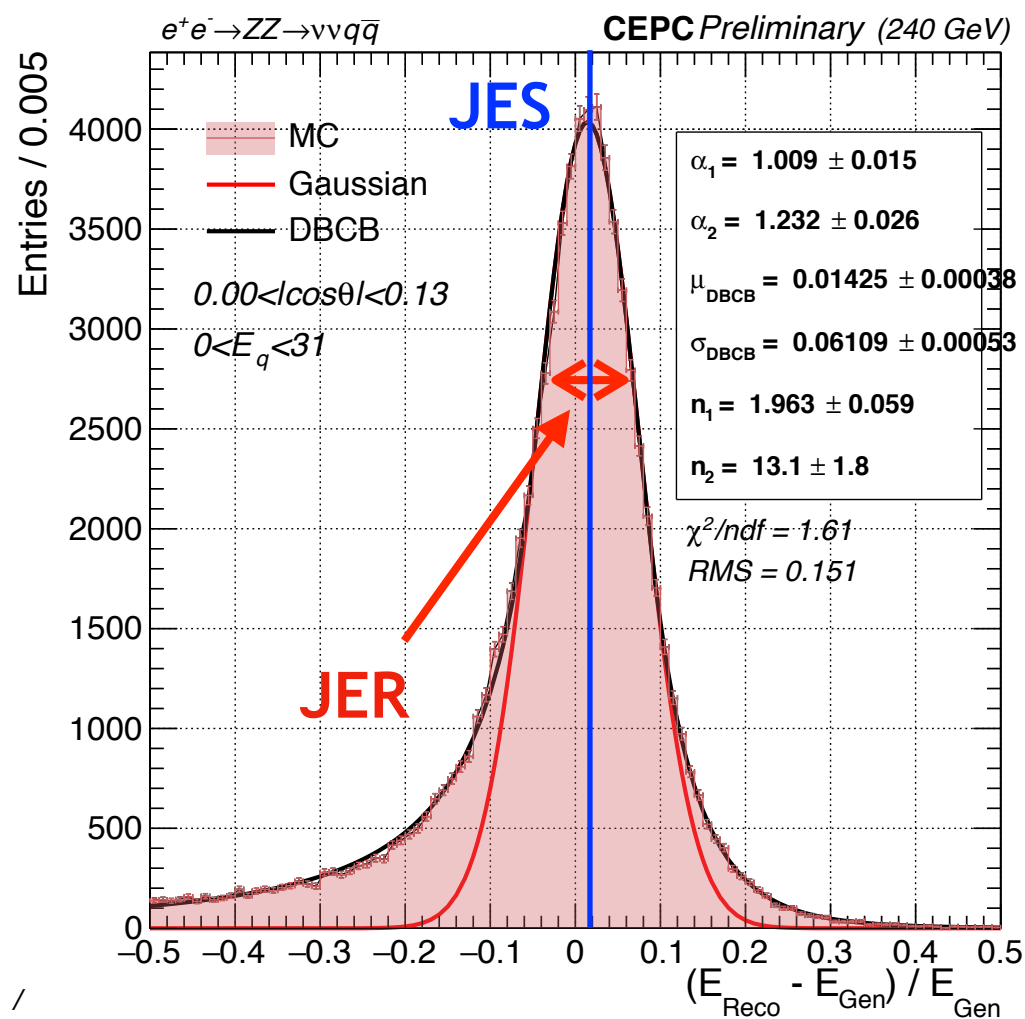


Quantify the Performance

- Double-sided crystal ball(DBCB) function is used to extract energy and angular resolution and scale.

Jet Energy Scale (JES)

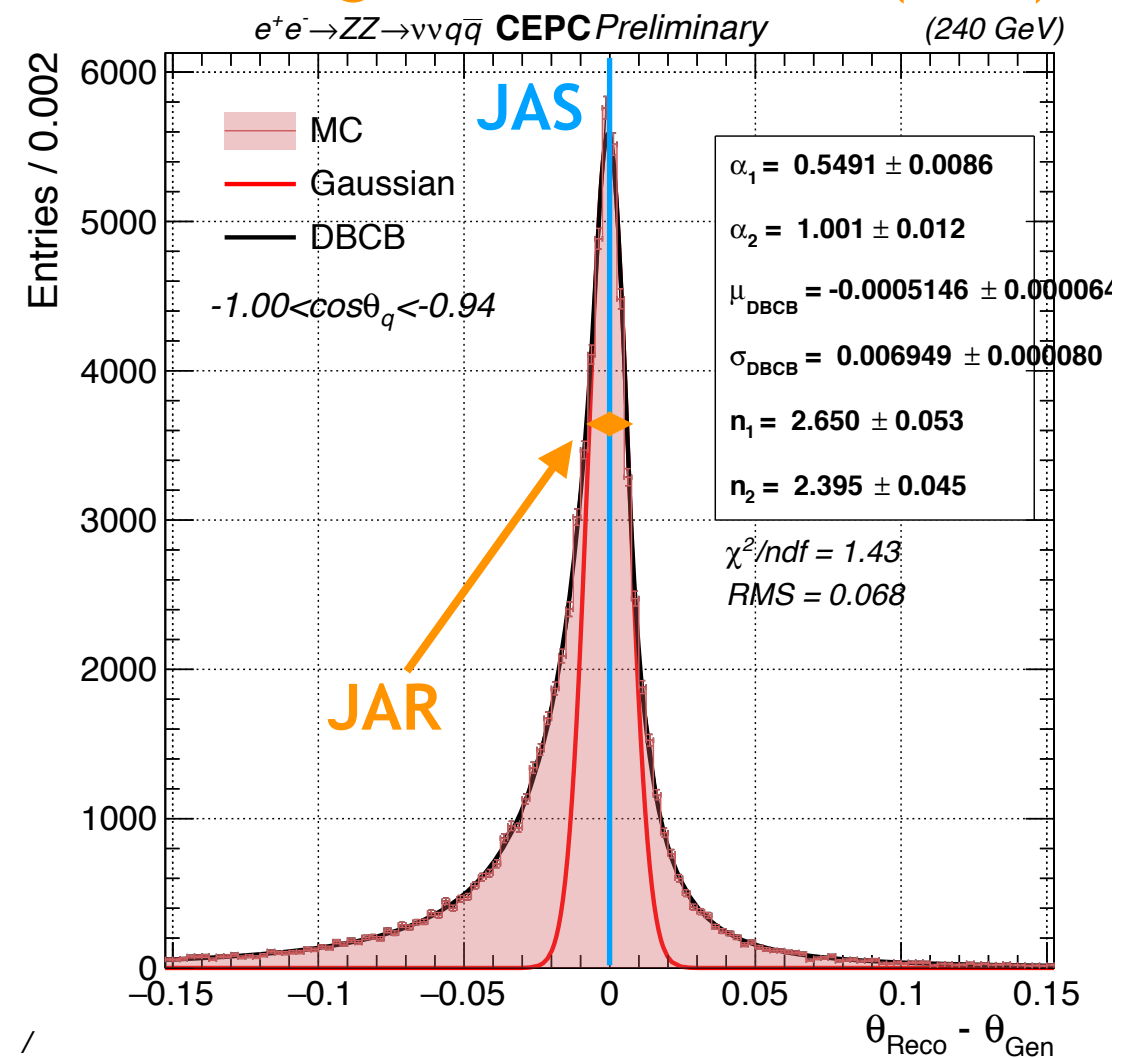
Jet Energy Resolution (JER)



Relative difference :
$$\frac{E_{\text{Reco}} - E_{\text{Gen}}}{E_{\text{Gen}}}$$

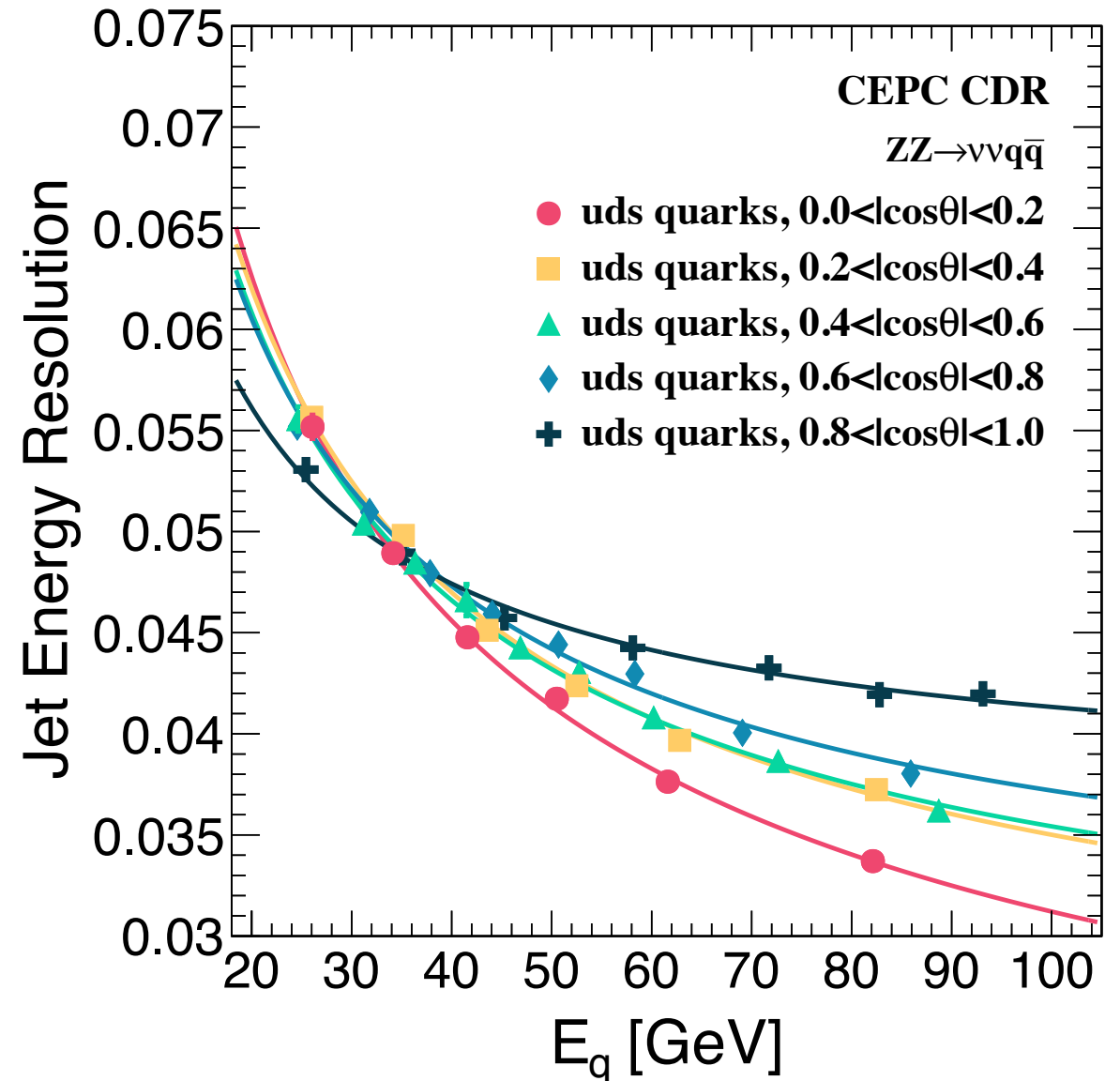
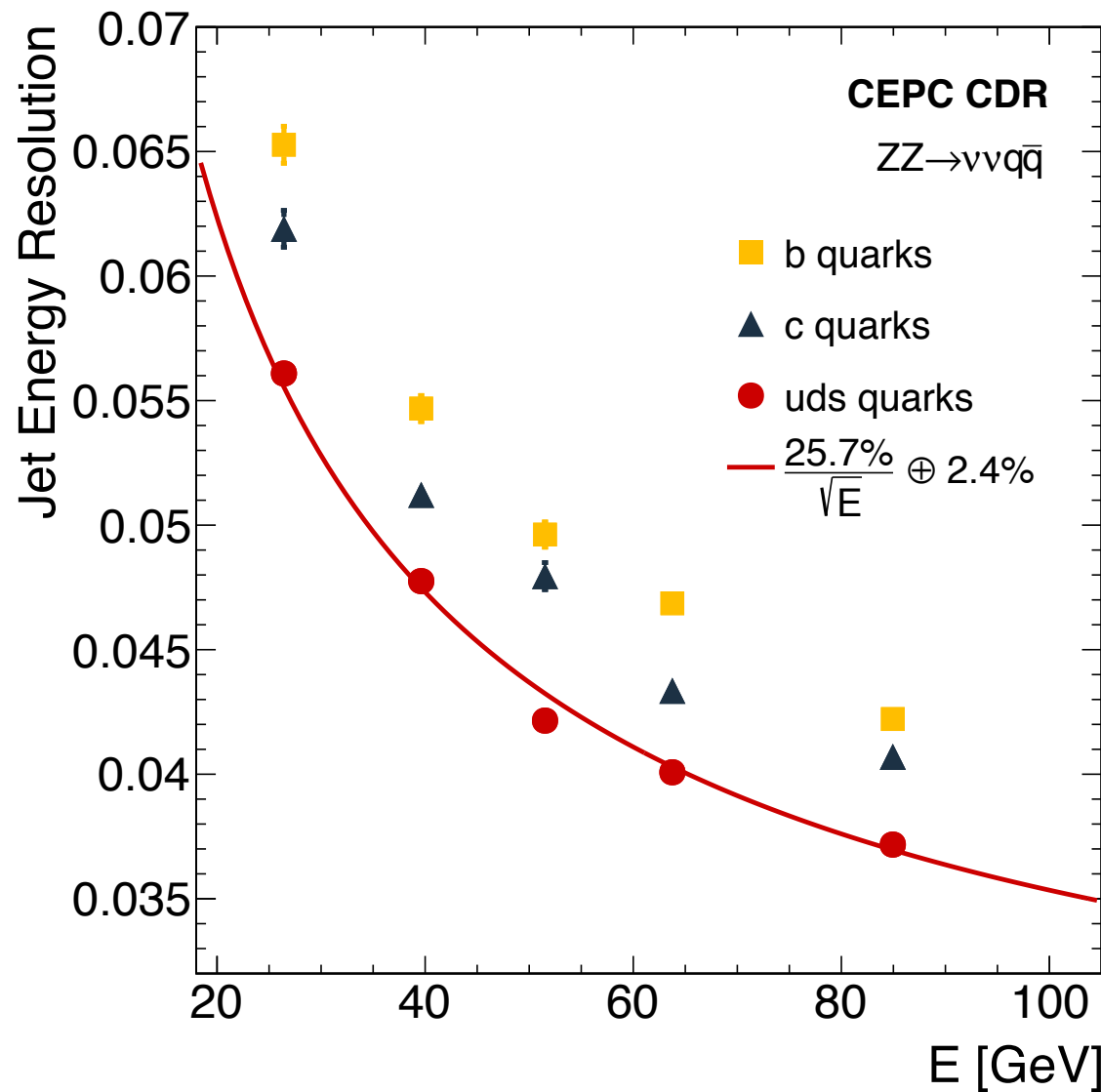
Jet Angular Scale (JAS)

Jet Angular Resolution (JAR)

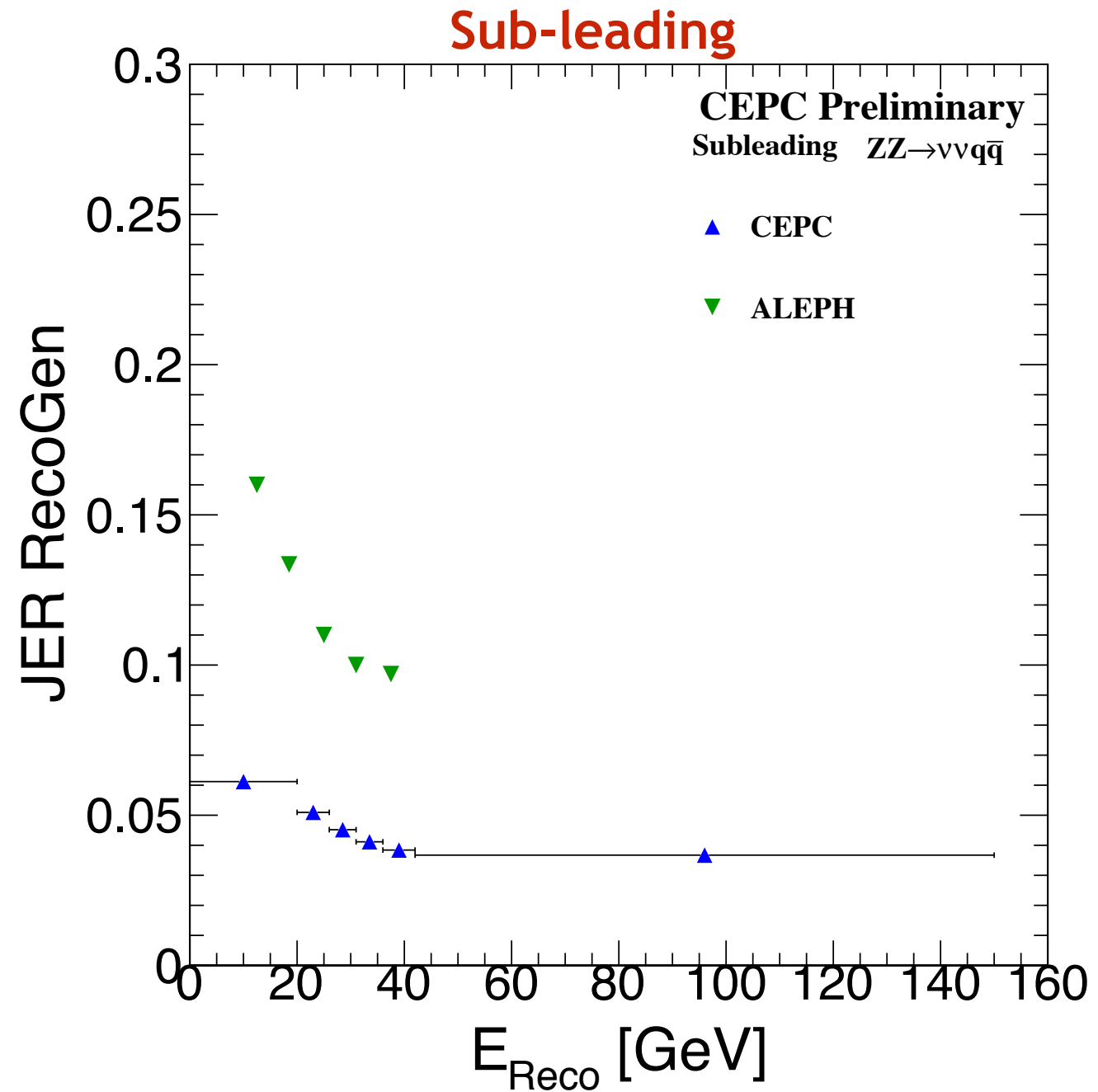
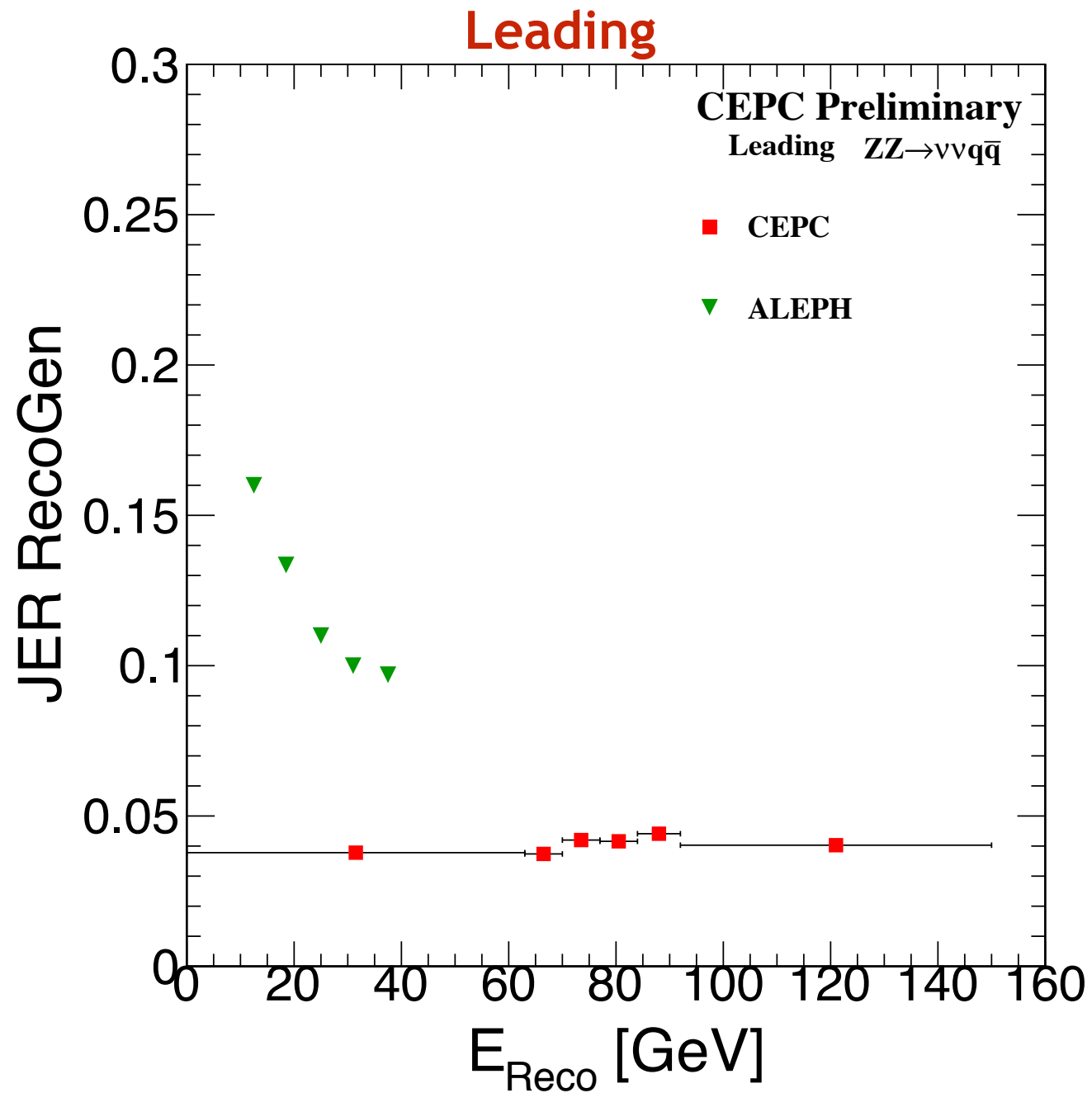


Difference :
$$\theta_{\text{Reco}} - \theta_{\text{Gen}}$$

BM3: JER (Reco-Gen)

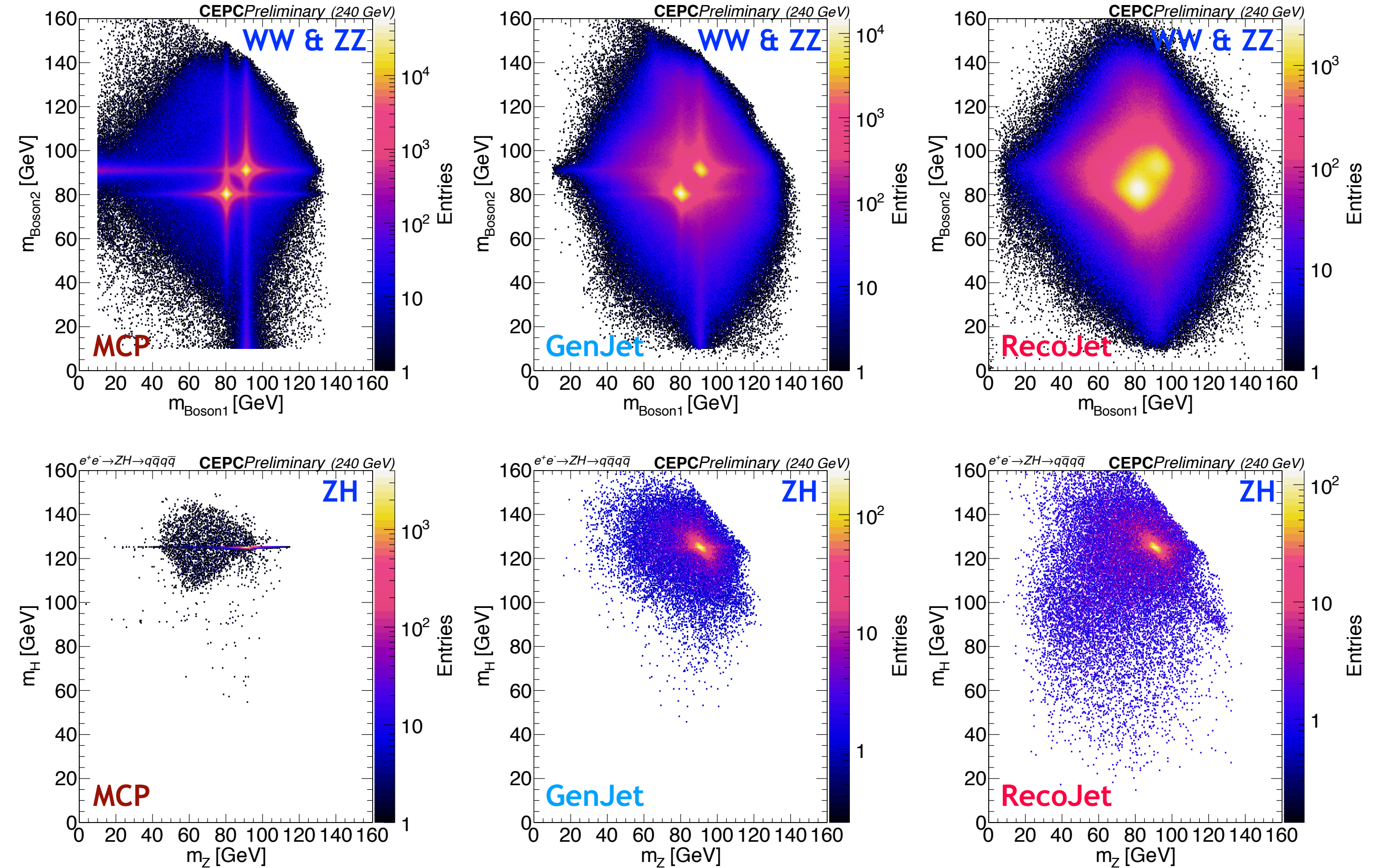


- JER also depends on jet flavors; the semi-leptonic decay from c- and b-quarks.
- For light-flavor jets with high energy and within central region of barrel, JER could reach **3%**.



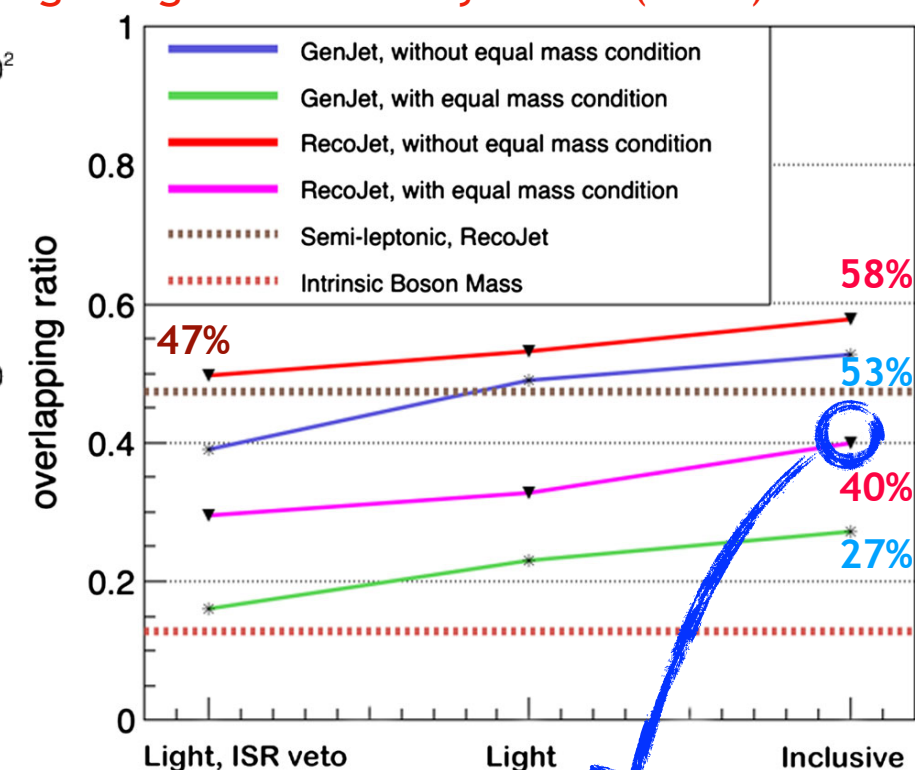
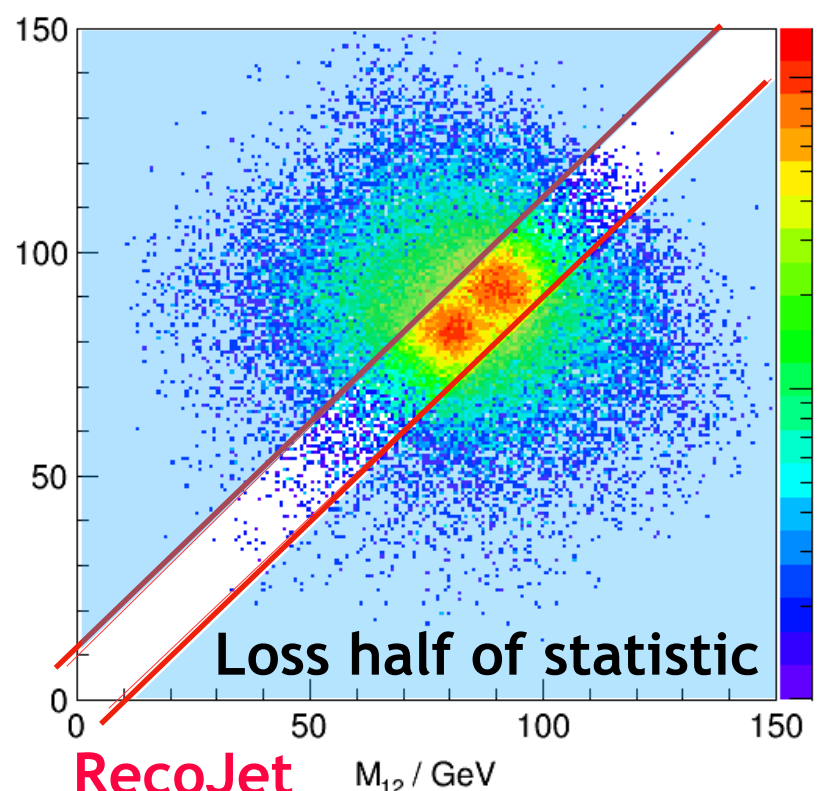
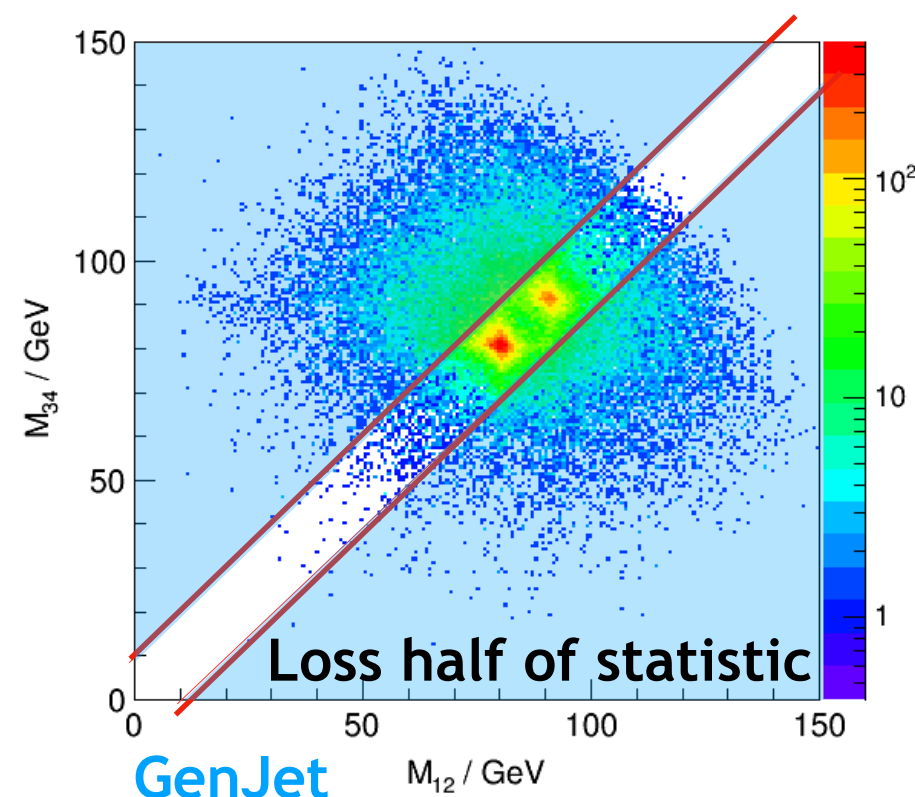
■ Our JER is better than ALEPH.

WW & ZZ Full Hadronic



BM4: WW & ZZ to 4 Jets Separation

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■ Equal mass requirement: $|M_{12} - M_{34}| < 10 \text{ GeV}$

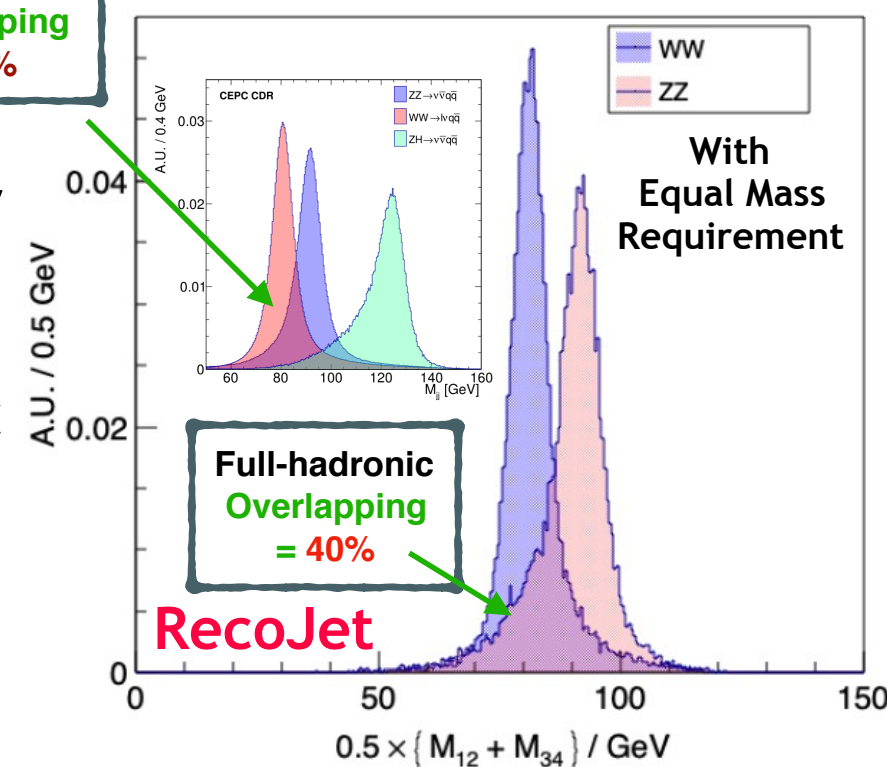
- Cost half of the statistic.
- Overlapping can be reduced from **58%/53%** to **40%/27%** for the **RecoJet/GenJet**.

■ CEPC baseline could separate WW & ZZ with full hadronic final-state.

■ Improve from the naive jet clustering & pairing and control the ISR photon in the event.

■ ZH full hadronic final-state analysis is on the way.

Semi-leptonic
Overlapping
= 47%



■ Jets are crucial for the CEPC Higgs physics

- 97% of ZH events evolve jets
- 1/3 only come from single Z or Higgs boson.
- 2/3 has more than one boson (e.g. $ZH \rightarrow q\bar{q}q\bar{q}$) - need color singlet identification algorithm.

I. **BMR < 4% is critical. Achieved at the CEPC baseline (3.8%)**

- * W, Z, Higgs boson can be efficiently separated at both semi-leptonic & full hadronic.
- * By Z-boson di-jet recoil mass to distinguish the ZH from ZZ process.

II. **2 jets final-state could be identified with $efficiency \times purity = 88.4\%$.**

- * Could be clustered by dedicated jet clustering algorithm, thrust.

III. **Single Jet — JER ~ 3-5% & JAR ~ 1%.**

- * Thrust clustering method is recommended for two jets final-state. It could improve the JER 20%, 40% on tail (RMS), and JAR 20%.

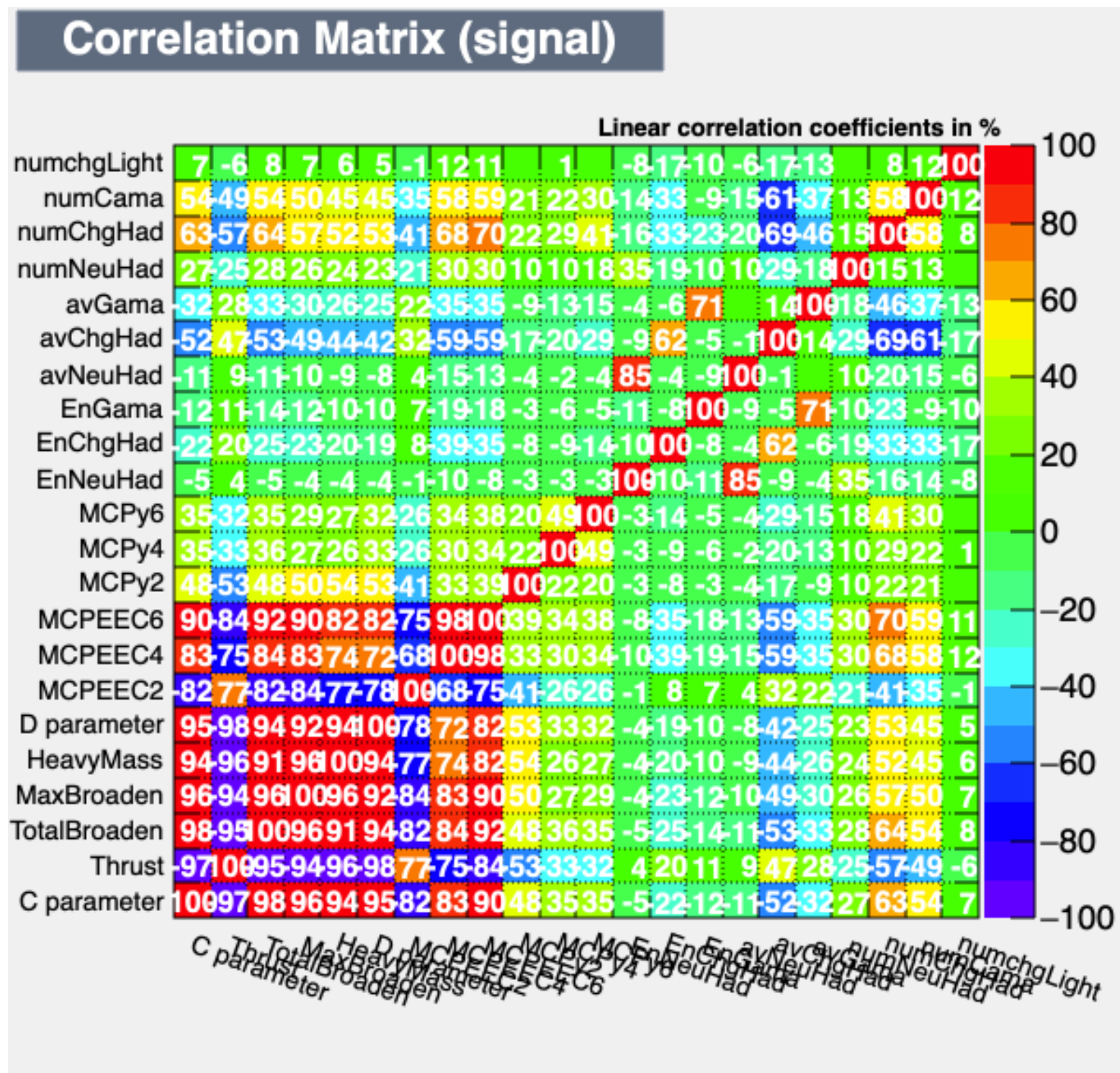
IV. **Need a better color singlet identification algorithm.**

- * Wrong jet pairing is the dominant effect to induce overlapping in full hadronic WW-ZZ separation.
- * Equal mass requirements: Reduce the overlapping to be better than semi-leptonic, but very costly.
- * Other physical impact is significant: ISR photon etc.
- * The statistical uncertainty of ZH to full hadronic final-state could be achieved 0.25% after considering the WW and ZZ as bkg.

BM2: Number of Jet Identification

20 Variables

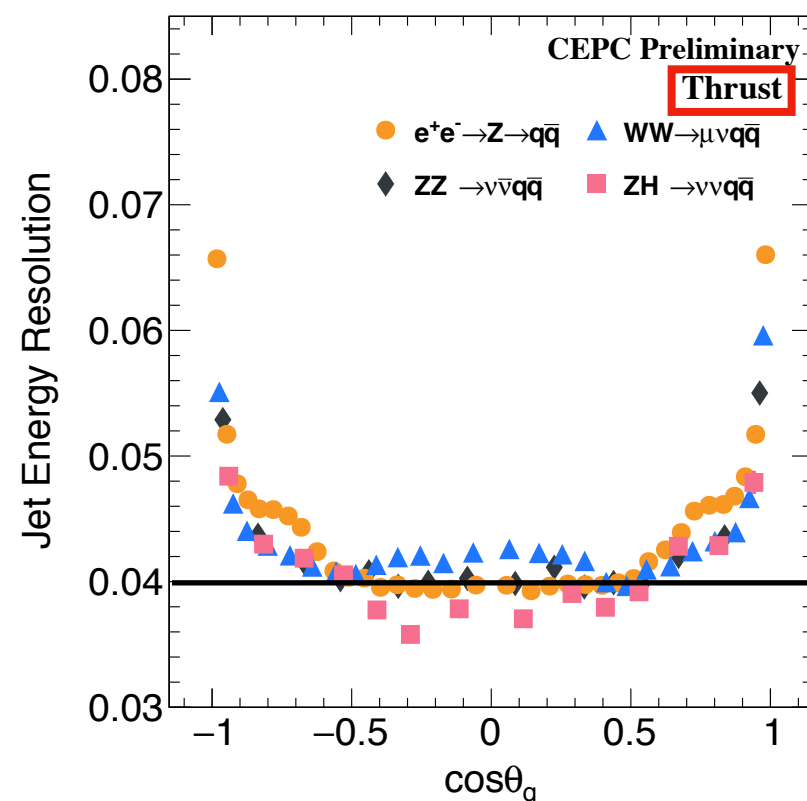
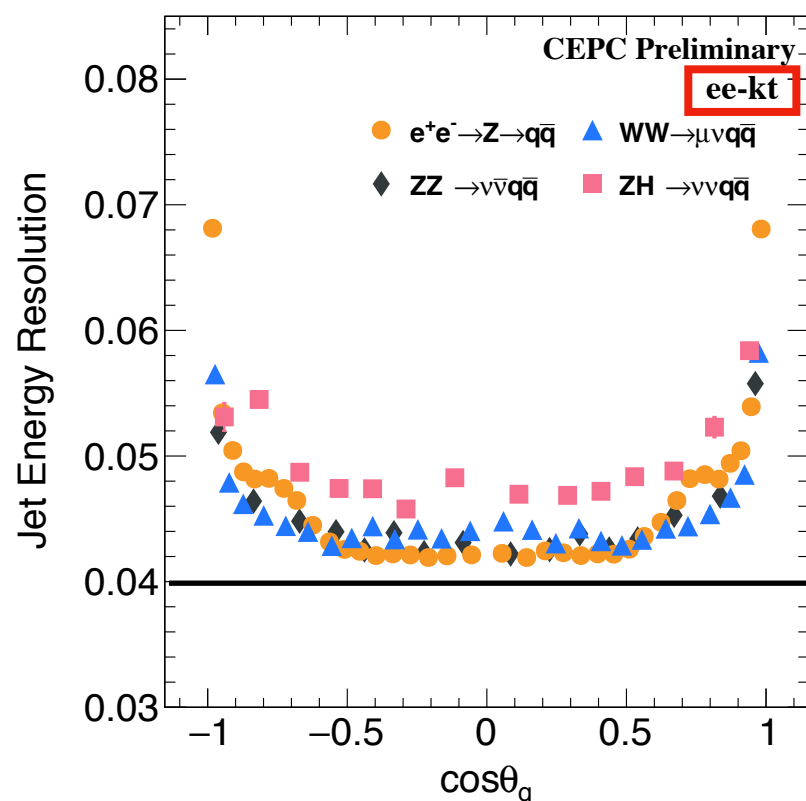
| | |
|----------------------------------|--------------------------|
| # of charge lepton | EEC 6 |
| # of γ | EEC 4 |
| # of charge hadron | EEC 2 |
| # of neutro hadron | C parameter |
| \bar{E}_γ | D parameter |
| $\bar{E}_{\text{Charge hadron}}$ | Heavy Mass |
| $\bar{E}_{\text{Neutro hadron}}$ | Max Broaden |
| E_γ | Total Broaden |
| $E_{\text{Charge hadron}}$ | Thrust |
| $E_{\text{Neutro hadron}}$ | y_{23}, y_{45}, y_{67} |



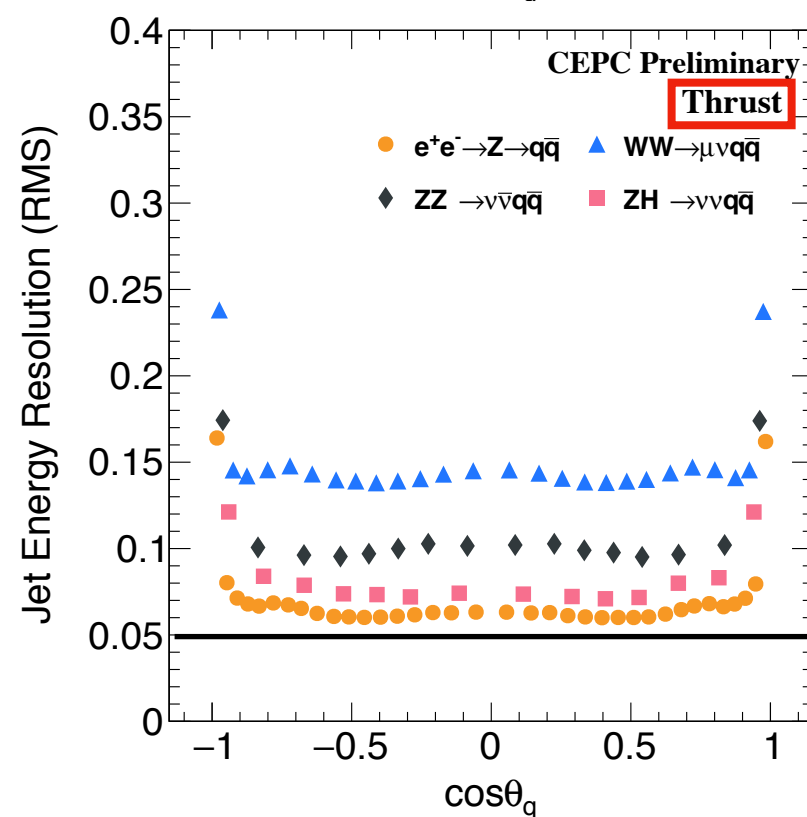
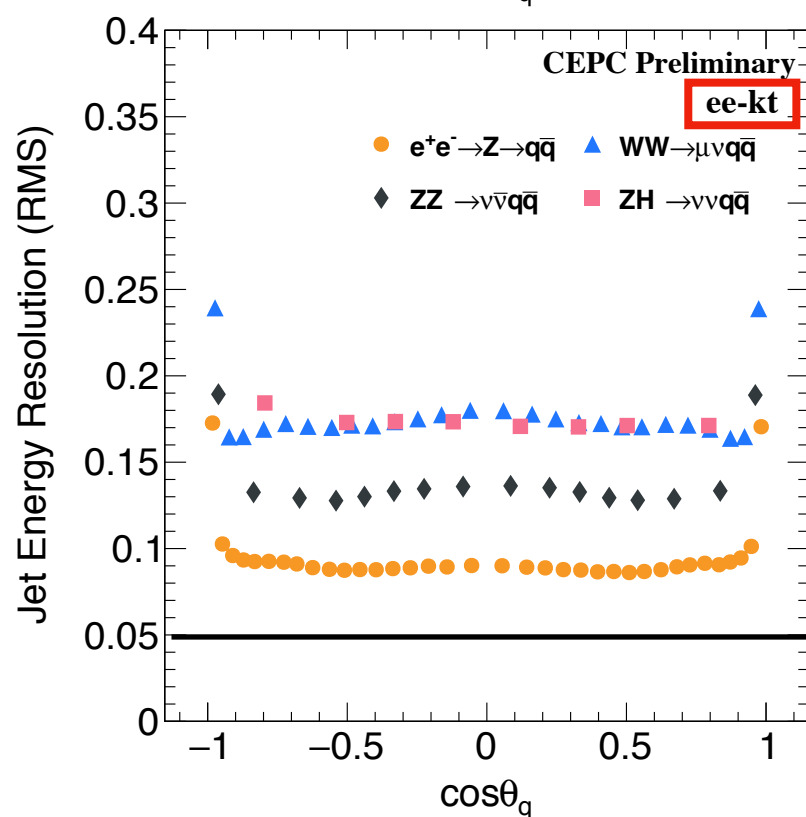
- Event-shape variables basic multi-variable analysis to separate 2, 4, and 6 jets final-state.

Yong-Feng Zhu

BM3: JER (ee- k_t —Thrust)



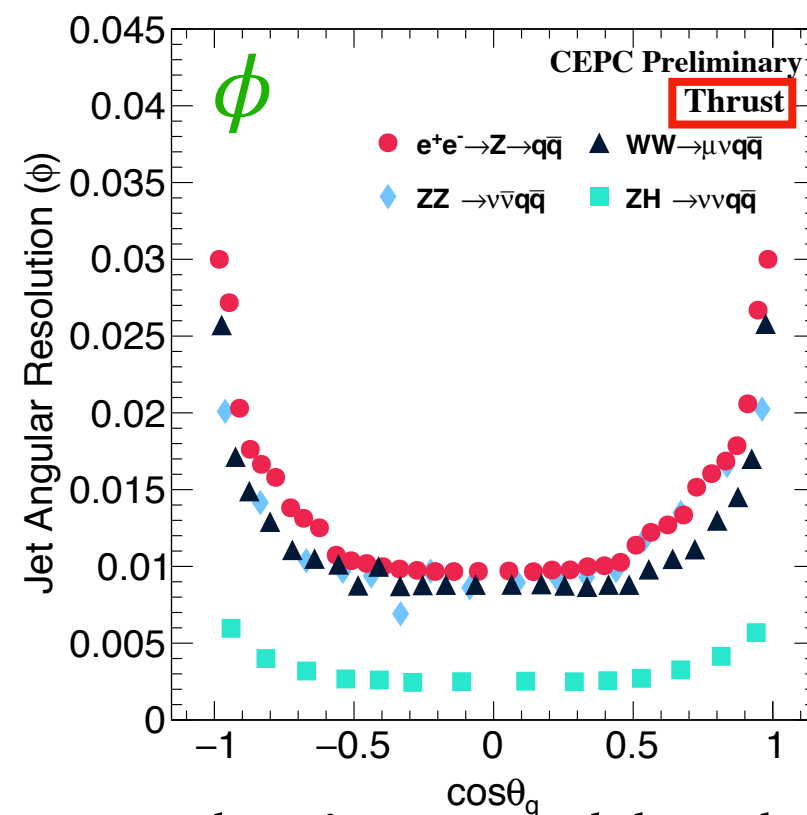
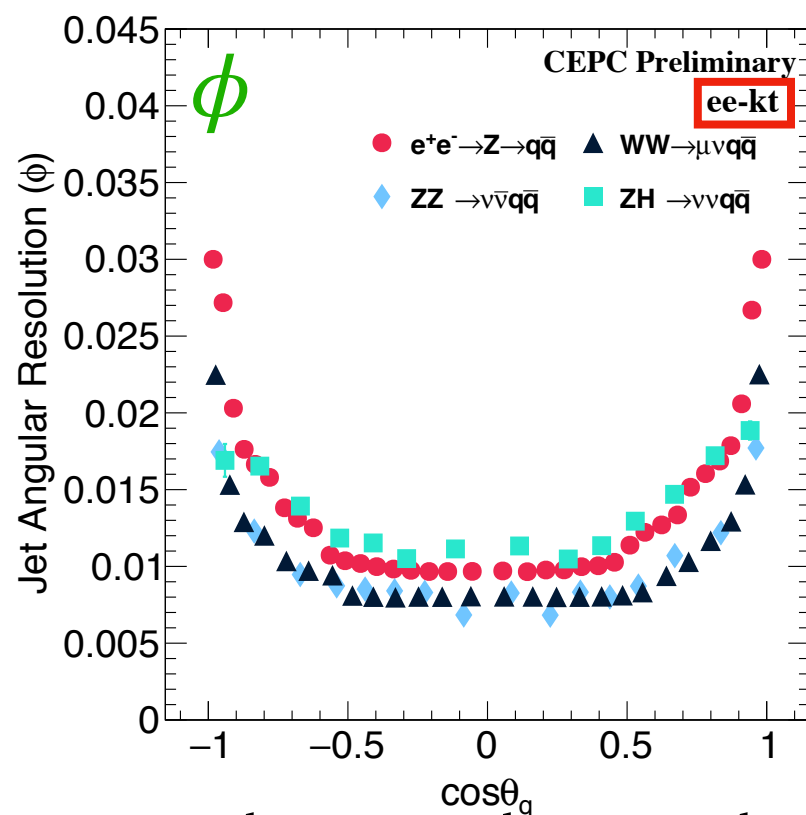
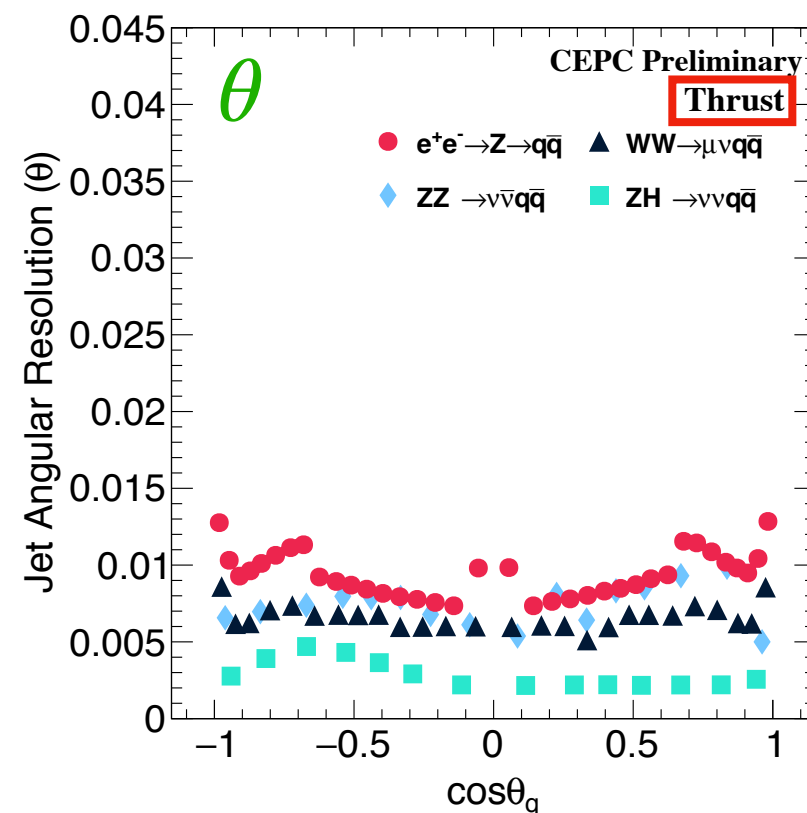
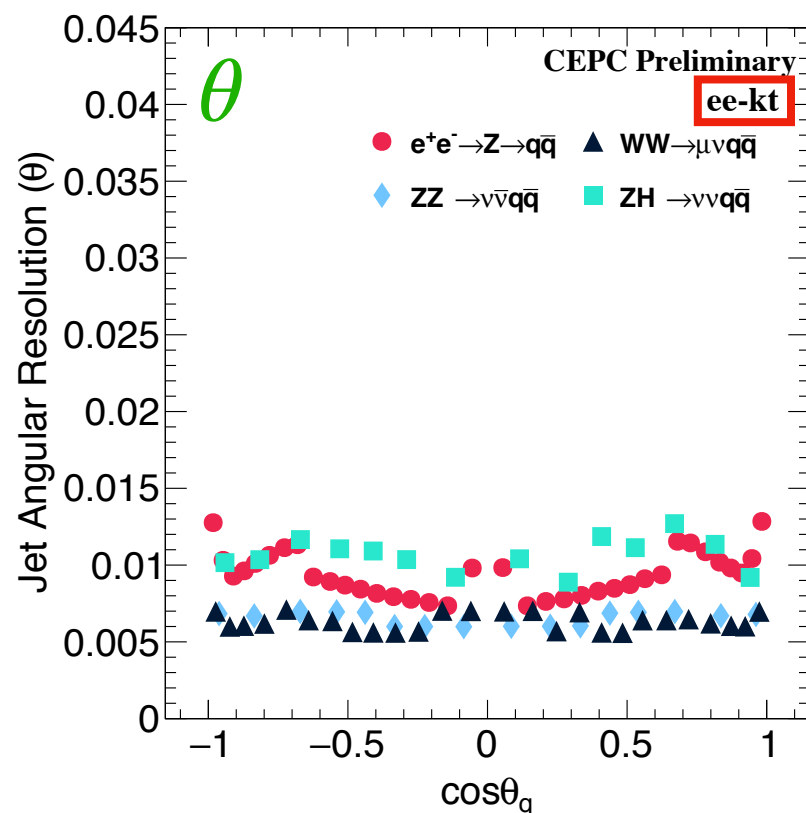
Improved **20%**
w.r.t ee- k_t



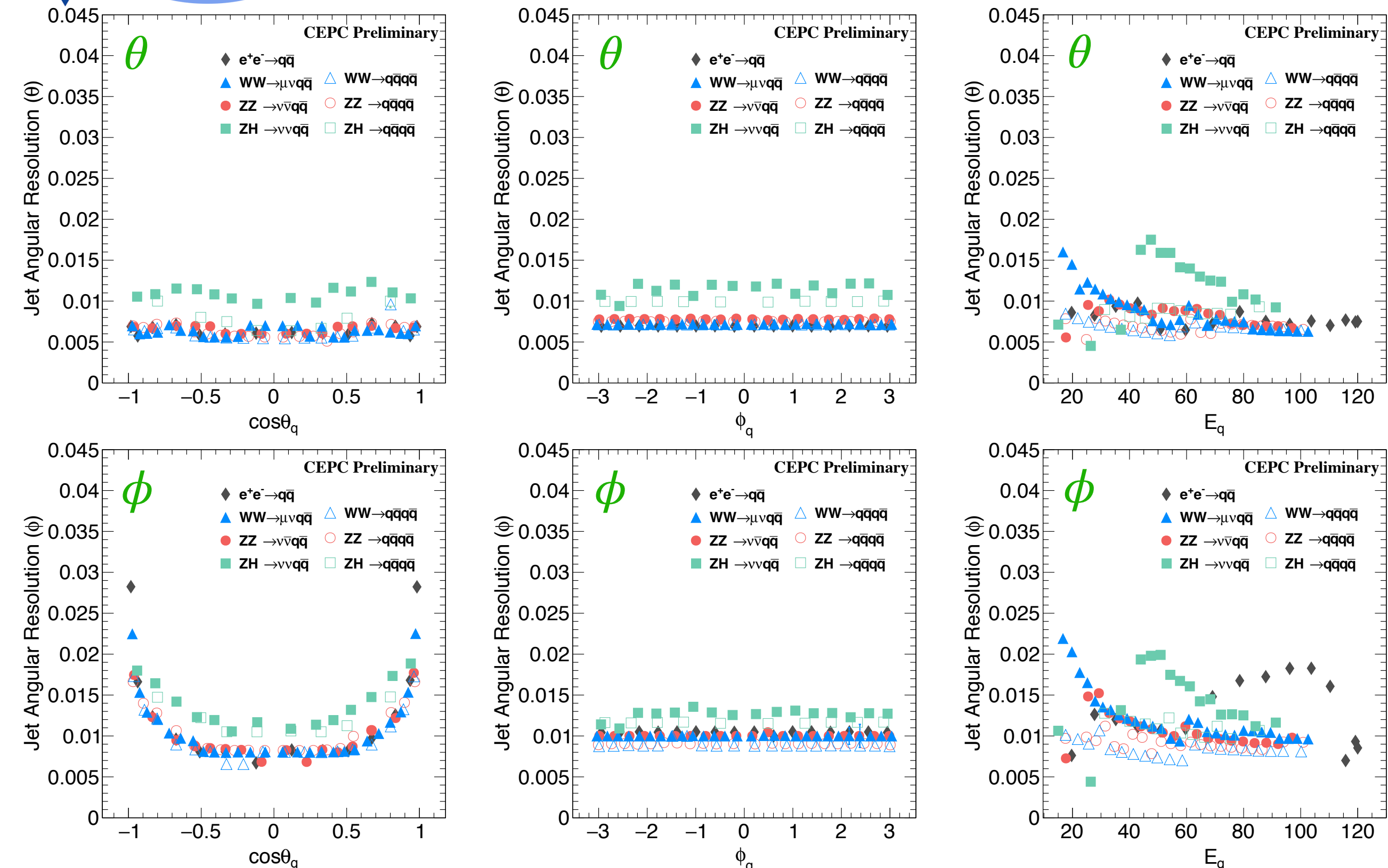
Improved **40%**
w.r.t ee- k_t

■ Improvement maybe came from boosting the system back to the rest frame with the neutrons' information.

BM3: JAR (ee- k_t —Thrust)



■ Both of jet θ and ϕ angular resolution are also improved by thrust method,
20%.



■ JAR is around **1%** in barrel region; JAS is **independent** of ϕ and energy.

■ The difference between 2 and 4 jets final-state is controlled within **1%** level.

Event-shape Variables

Heavy Jet Mass

$$M_1^2 = \frac{1}{(\sqrt{s})^2} \left(\sum_i^N P_i \right)^2$$

$$M_2^2 = \frac{1}{(\sqrt{s})^2} \left(\sum_i^N P_i \right)^2$$

Jet Broadening

$$B_1 = \frac{1}{2 \sum_{j=1}^N |P_j|} \sum_{i=1}^N |P_i \times n_T|, (P_i \times n_T) > 0$$

$$B_2 = \frac{1}{2 \sum_{j=1}^N |P_j|} \sum_{i=1}^N |P_i \times n_T|, (P_i \times n_T) < 0$$

Jet Transition variable, y_{23} , y_{45} , y_{67}

ee-kt jet clustering algorithm

$$d_{ij} = 2\min(E_i^2, E_j^2)(1 - \cos\theta_{ij})$$

C and D Parameter

$$L^{ab} = \frac{1}{\sum_{j=1}^N |P_j|} \sum_{i=1}^N \frac{P_i^a P_i^b}{|P_i|}$$

$$C = 3(\lambda_1\lambda_2 + \lambda_1\lambda_3 + \lambda_2\lambda_3)$$

$$D = 27\lambda_1\lambda_2\lambda_3$$

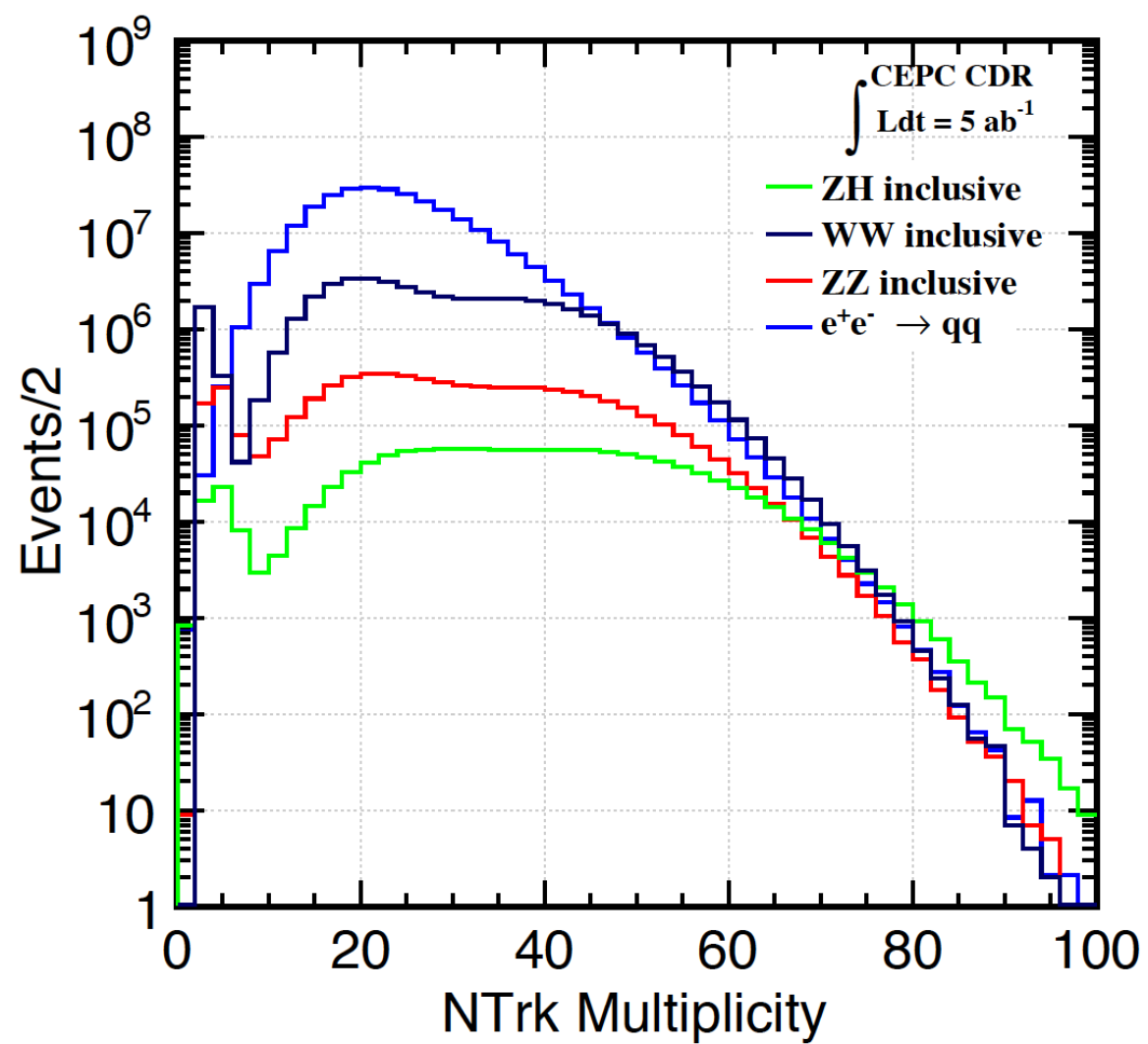
Energy-Energy Correlation

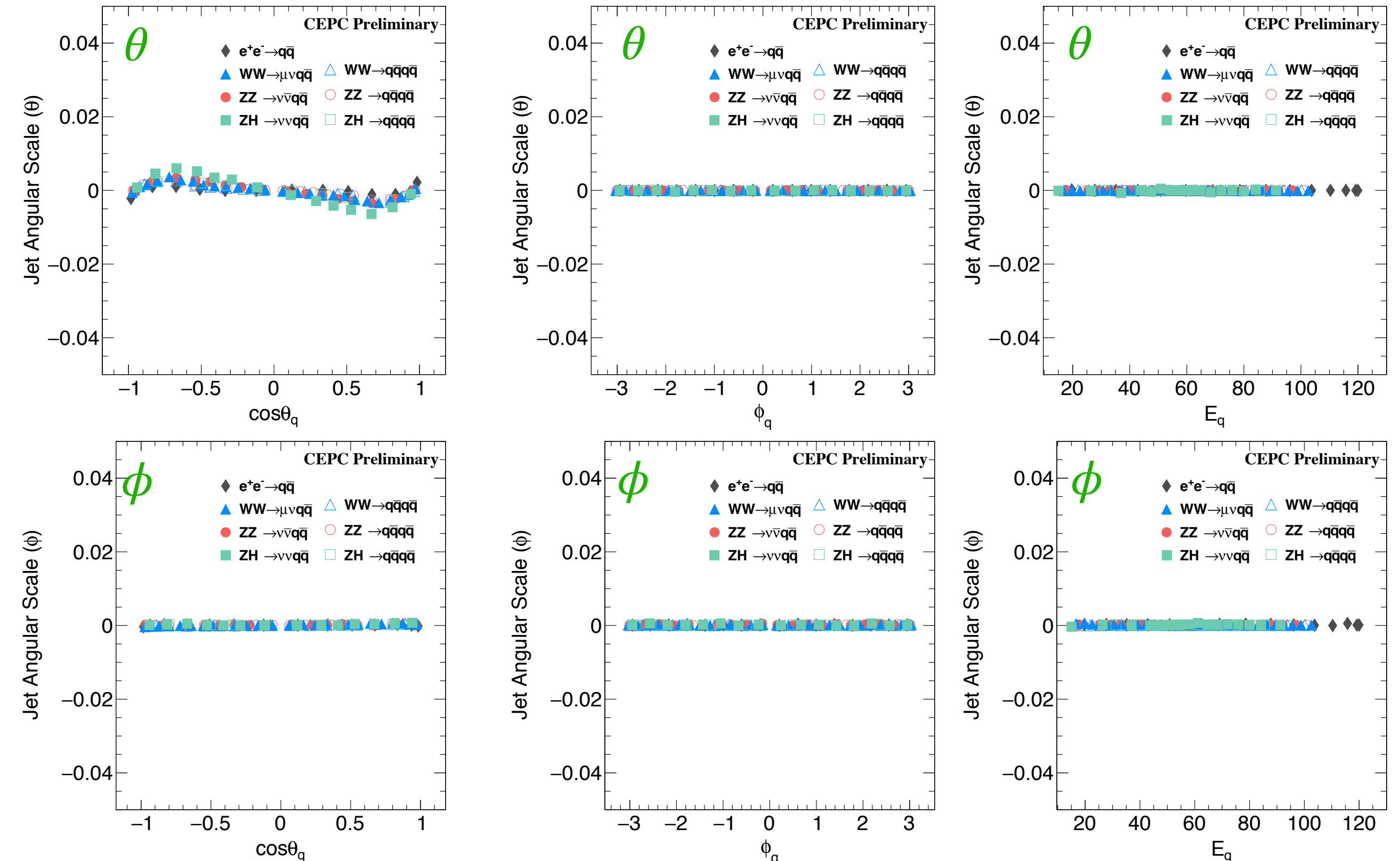
$$EEC = \frac{1}{\sigma_{tot}} \sum_{ij} \int d\sigma \frac{E_i E_j}{Q^2} \delta(\cos\chi - \cos\theta_{ij})$$

$$likelihood = \frac{\sum (P1_i) \times P2_i}{\sqrt{\sum (P1_i \times P2_i) \times \sum (P2_i \times P2_i)}}$$

Double-sided Crystal Ball

$$f(x|\alpha_1, \alpha_2, n_1, n_2, \bar{x}, \sigma) = \begin{cases} \left(\frac{n_1}{|\alpha_1|}\right)^{n_1} e^{-\frac{|\alpha_1|^2}{2}} \left(\frac{n_1}{|\alpha_1|} - |\alpha_1| - \frac{x - \bar{x}}{\sigma}\right)^{-n_1} & \frac{x - \bar{x}}{\sigma} < -\alpha_1 \\ e^{-\frac{1}{2}\left(\frac{x - \bar{x}}{\sigma}\right)^2} & -\alpha_1 < \frac{x - \bar{x}}{\sigma} < \alpha_2 \\ \left(\frac{n_2}{|\alpha_2|}\right)^{n_2} e^{-\frac{|\alpha_2|^2}{2}} \left(\frac{n_2}{|\alpha_2|} - |\alpha_2| - \frac{x + \bar{x}}{\sigma}\right)^{-n_2} & \alpha_2 < \frac{x - \bar{x}}{\sigma} \end{cases}$$

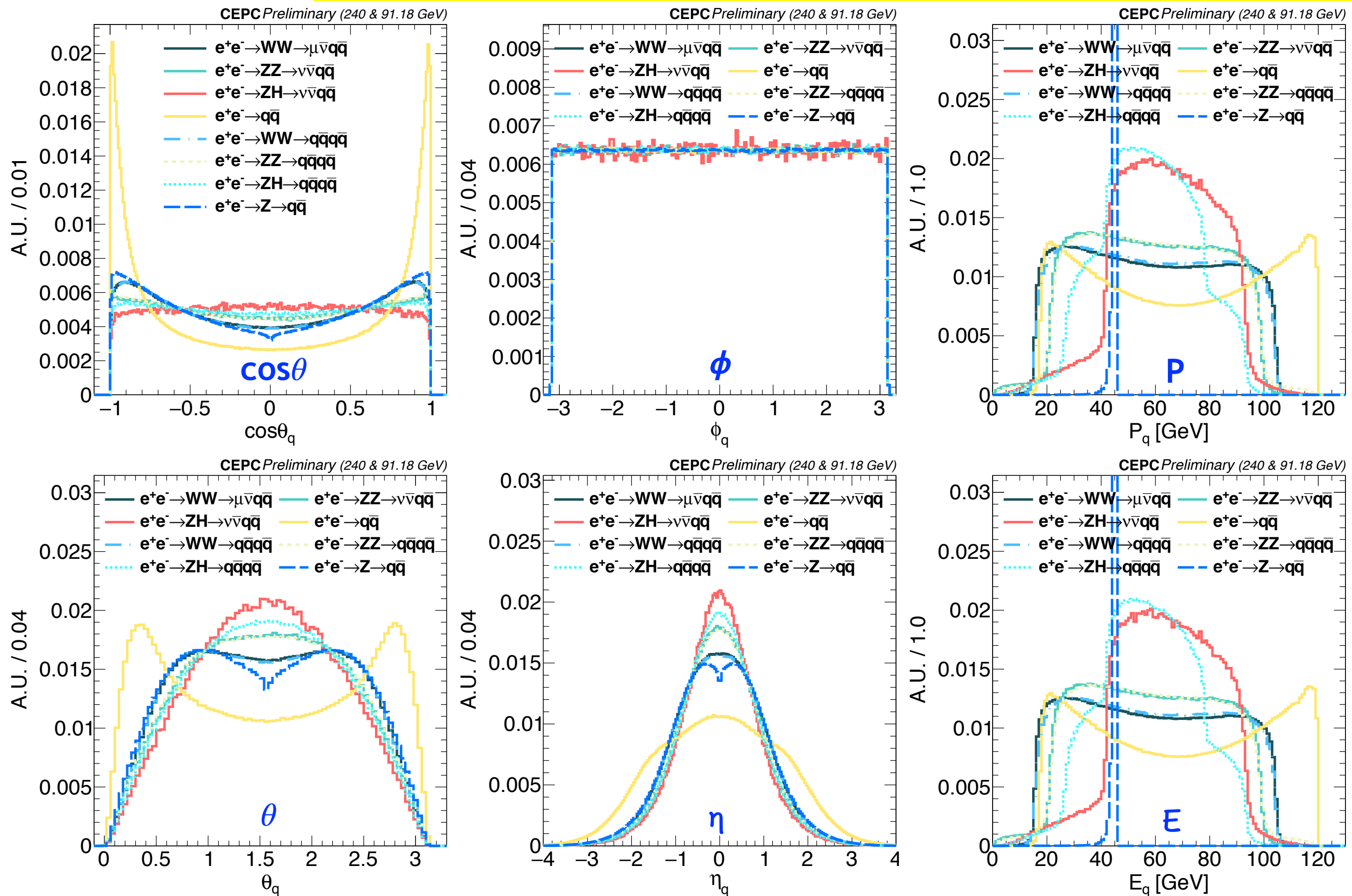




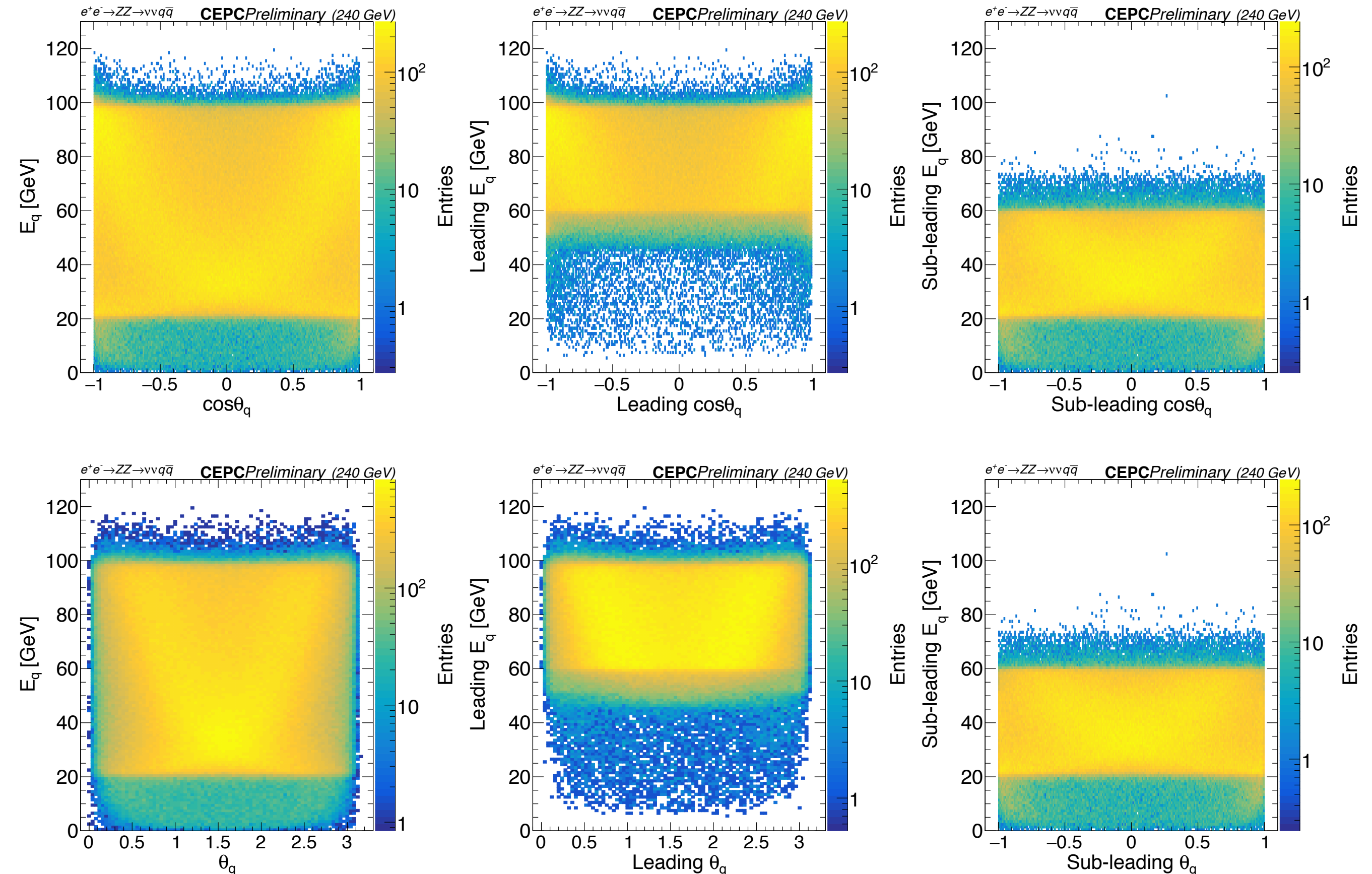
■ JAR is around **1%** in barrel region; JAS is **independent** of ϕ and energy.

■ The difference between 2 and 4 jets final-state is controlled within **1%** level.

Kinematic Summary Plots (Parton level)

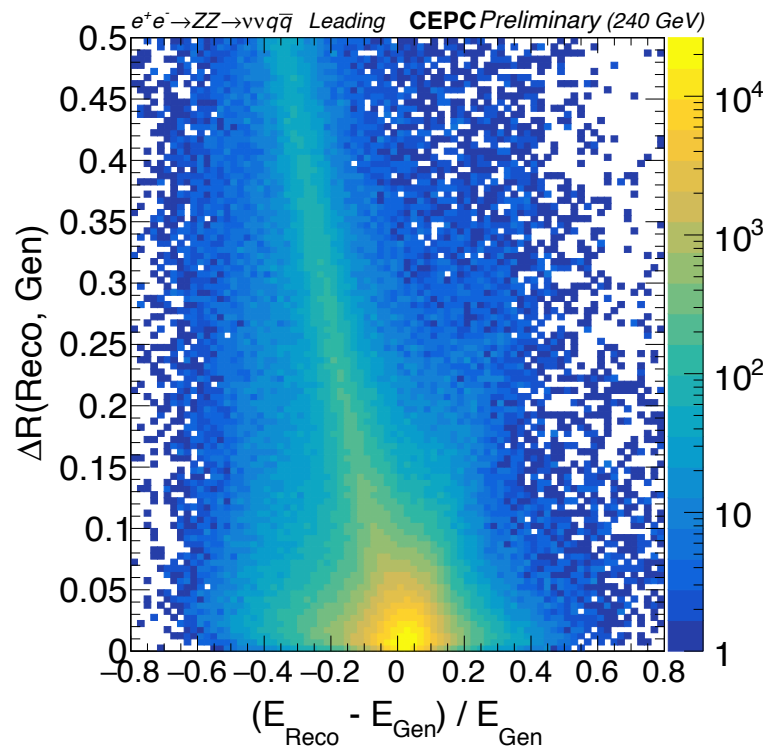


E as the function of the polar angle

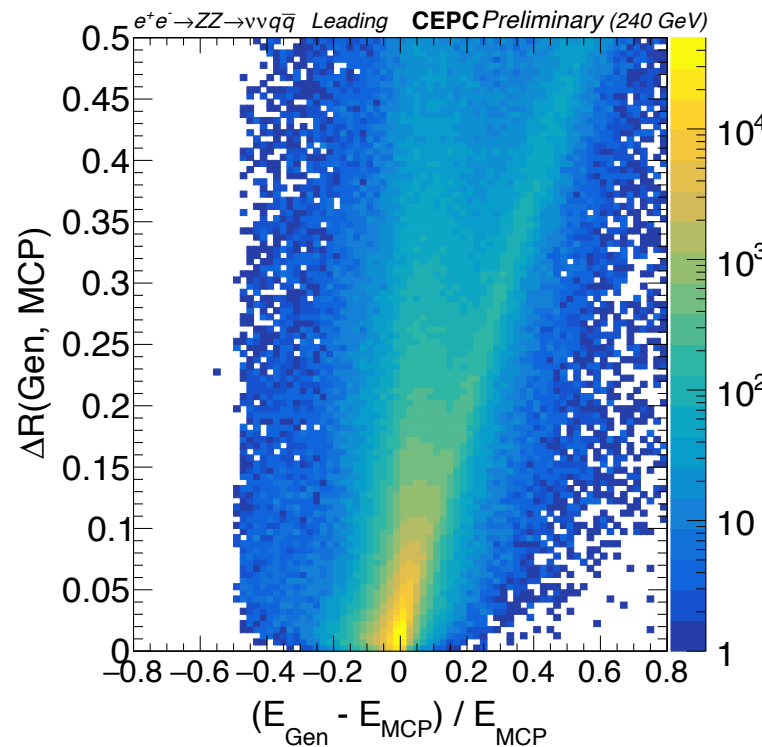


ΔR as the function of ΔE

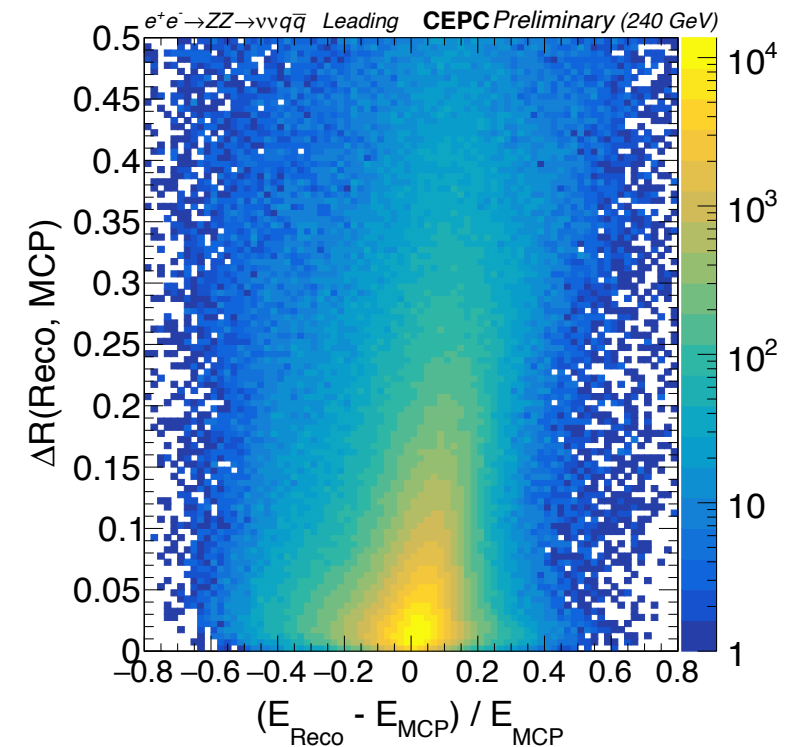
Leading, Gen-MCP



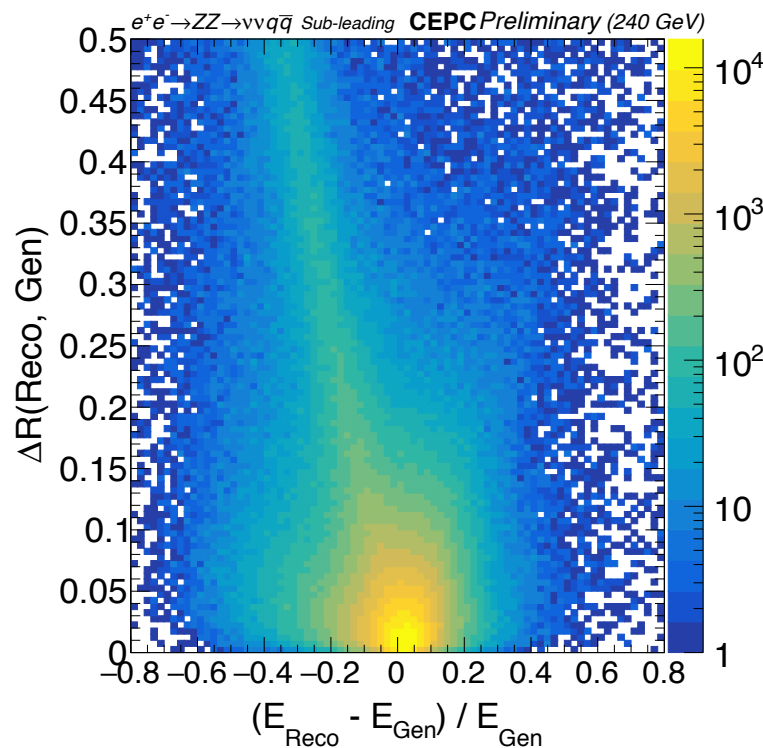
Leading, Reco-Gen



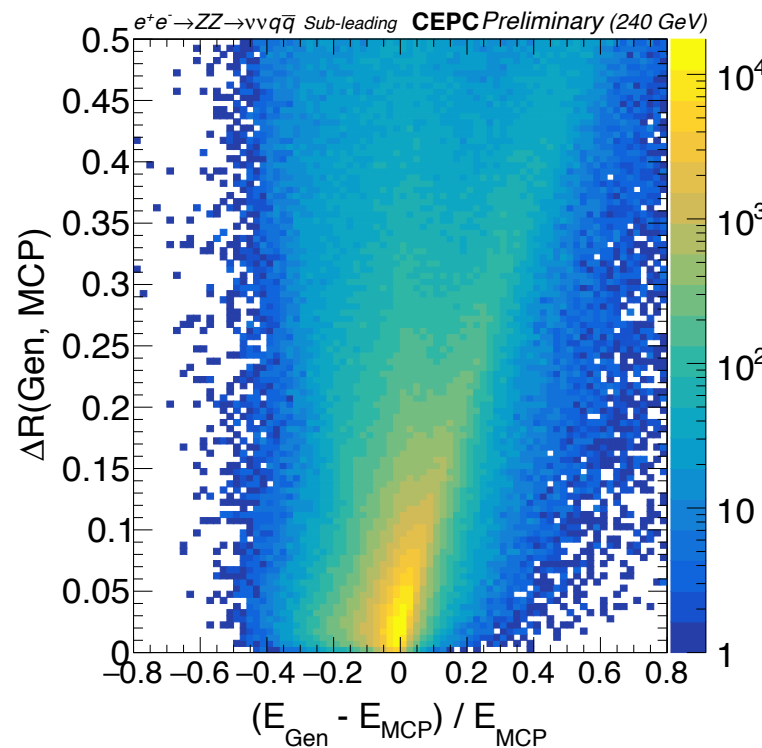
Leading, Reco-MCP



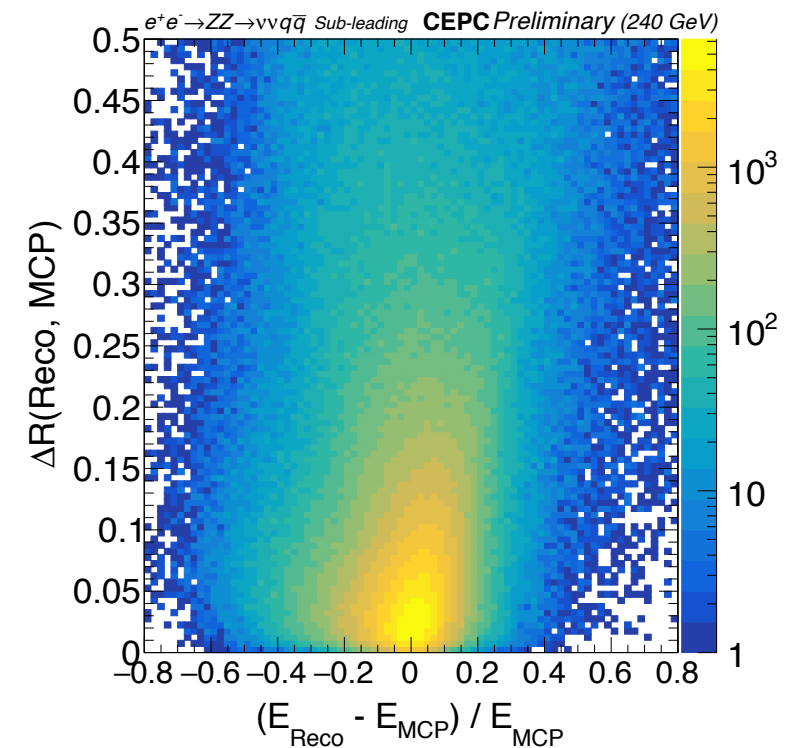
Sub-leading, Gen-MCP



Sub-leading, Reco-Gen

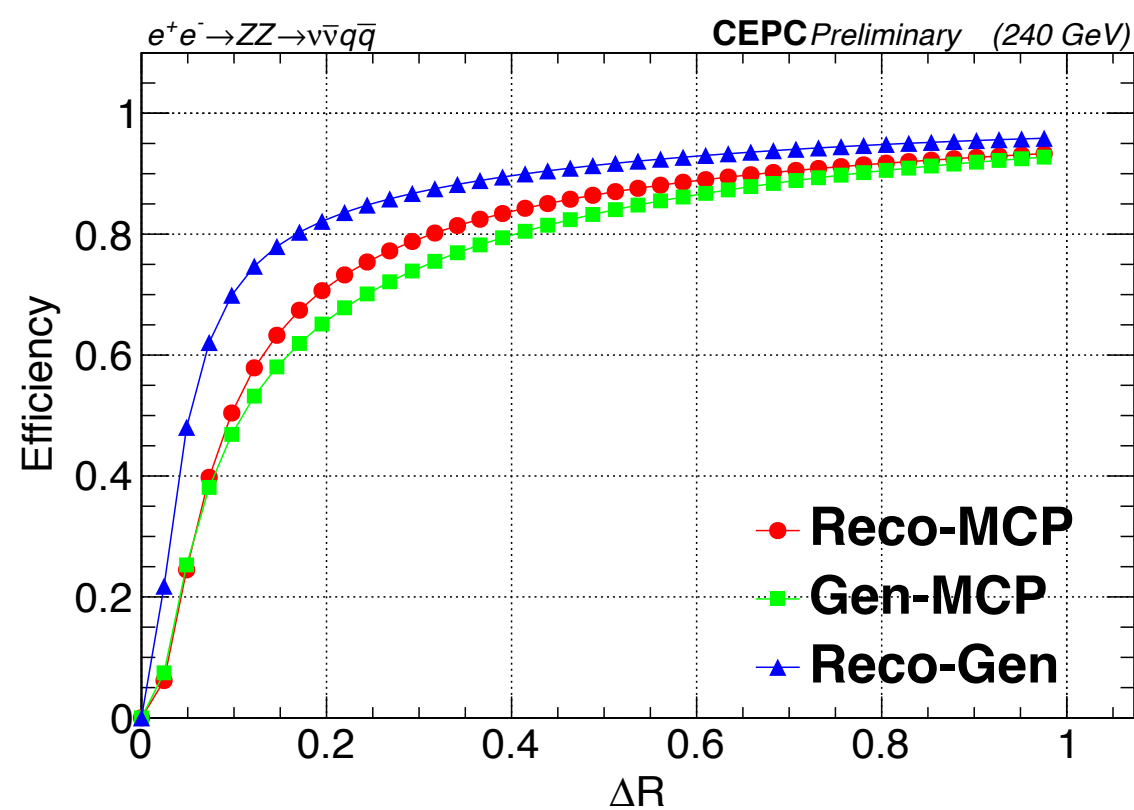
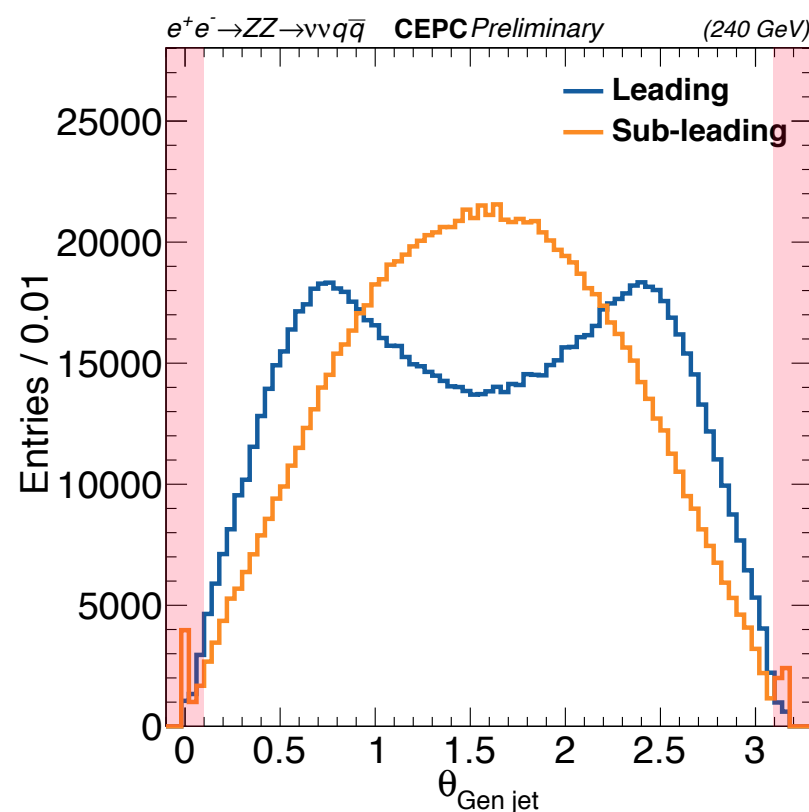


Sub-leading, Reco-MCP



The jet clustering brings a significant uncertainty.

| Items | (Reco-Gen) | (Gen-MCP) |
|--|------------|-----------|
| $\theta_{\text{Gen jet}} > 0.1 \ \& \ \theta_{\text{Gen jet}} < 3.1$ | ✓ | ✓ |
| $\Delta R(\text{Reco-MCP}) < 0.1$ | ✓ | ✗ |

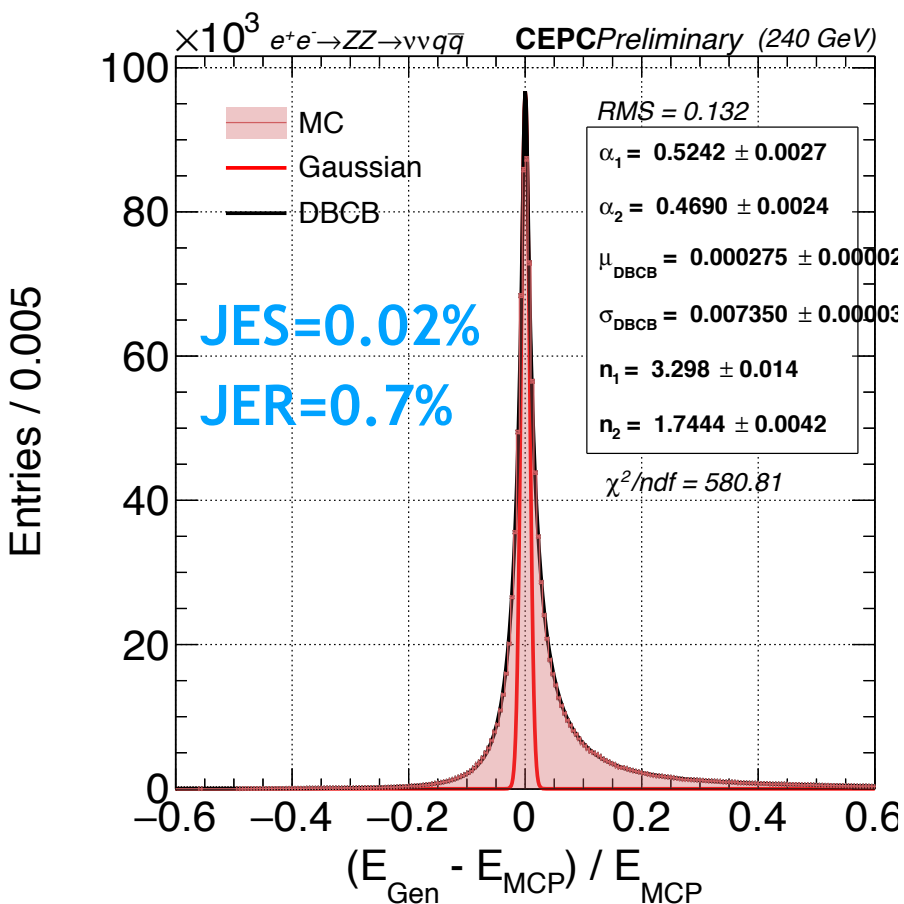


Efficiency=

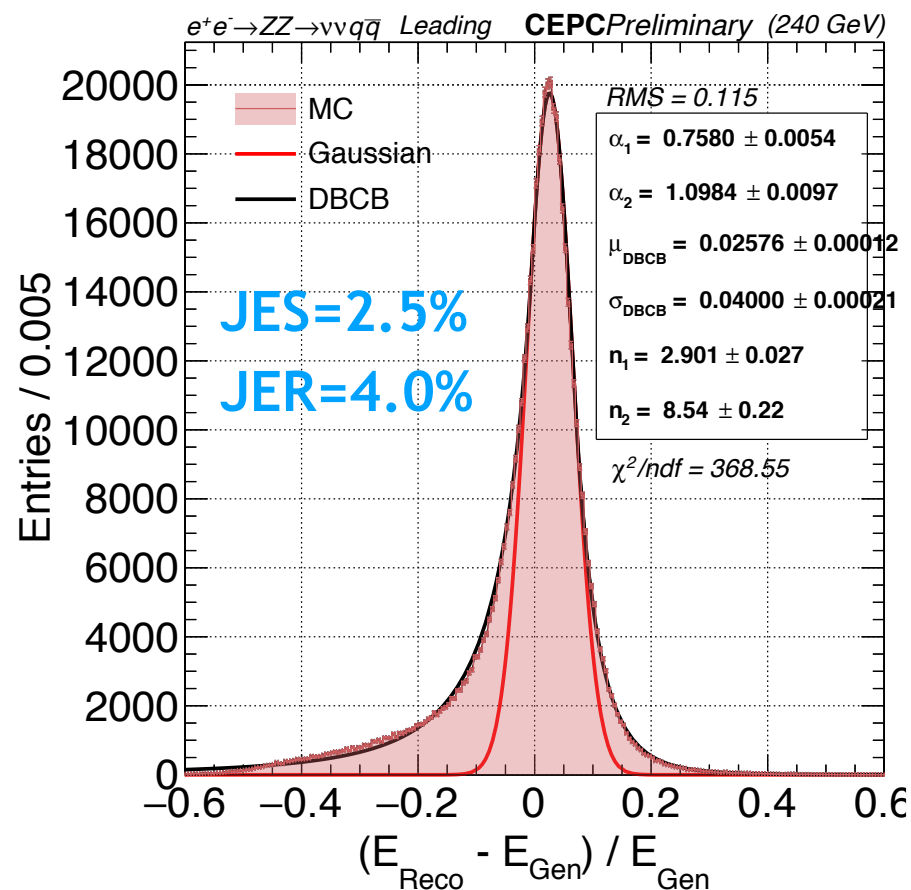
$$\frac{\text{\# of leftover event}}{\text{\# of total event}}$$

$$\Delta R = \sqrt{\Delta\phi^2 + \Delta\eta^2}$$

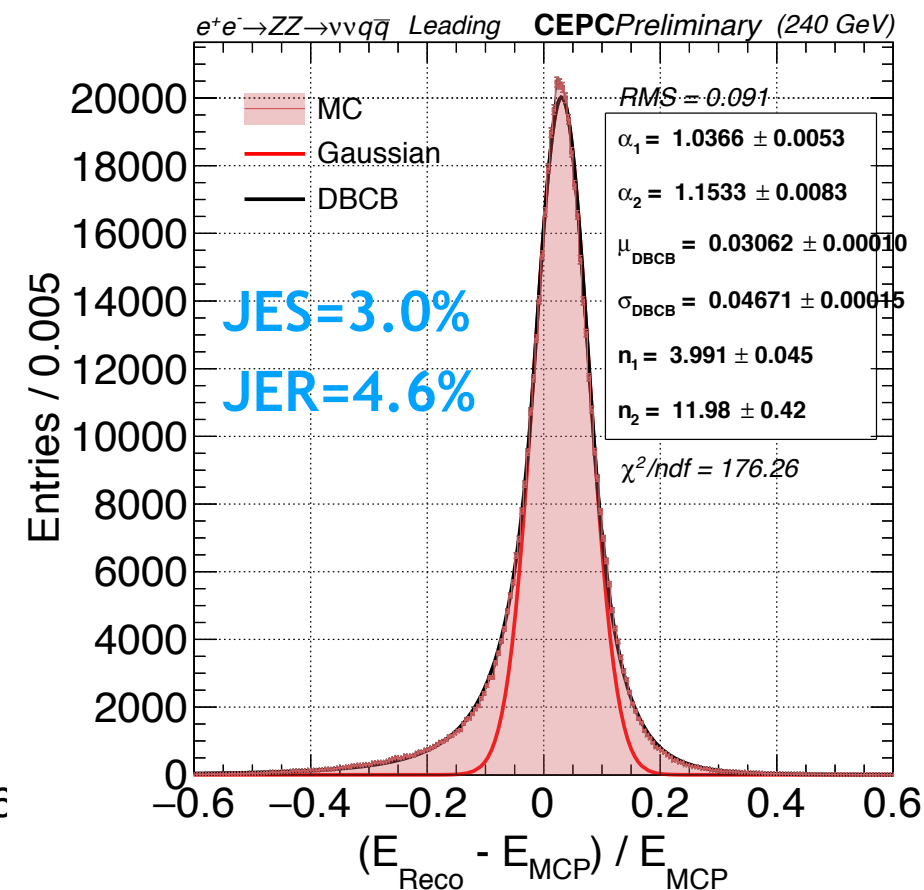
Gen-MCP



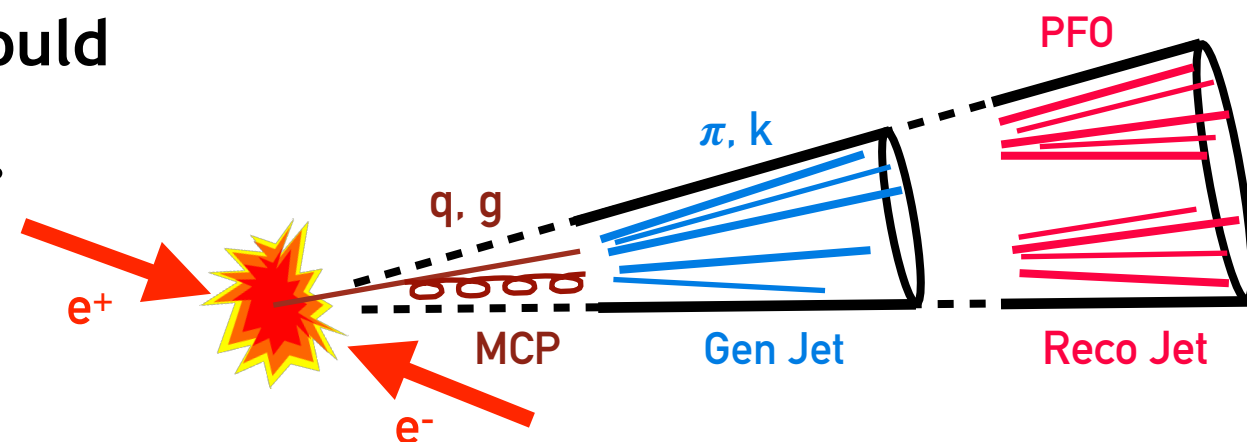
Reco-Gen



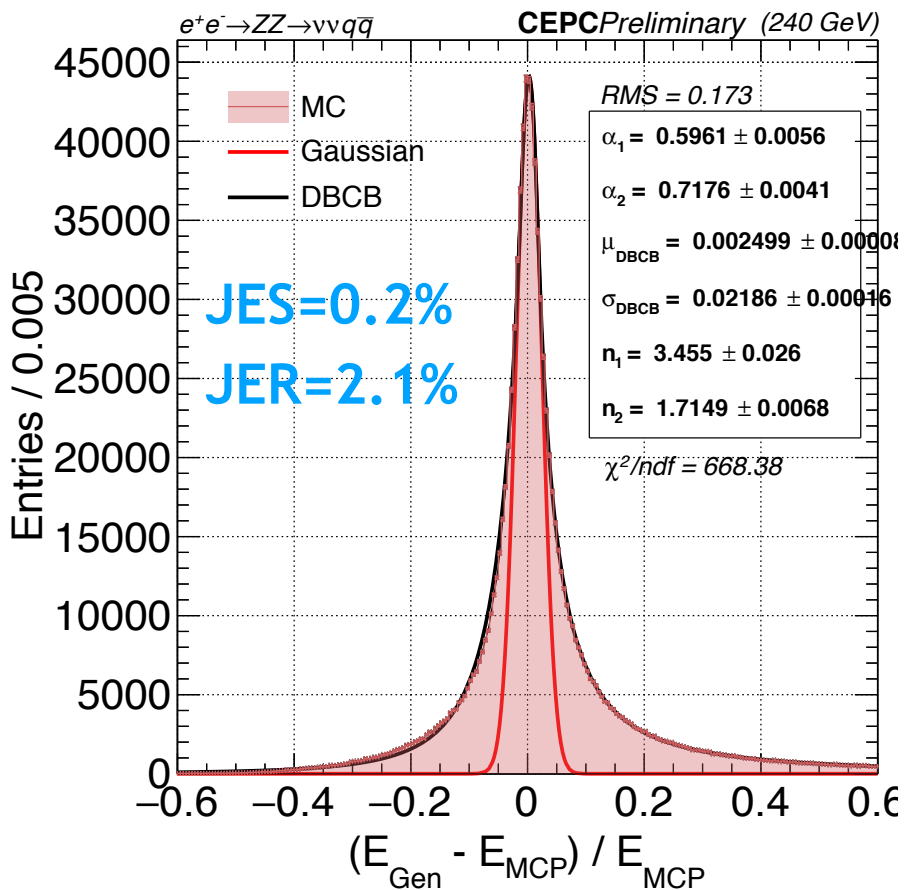
Reco-MCP



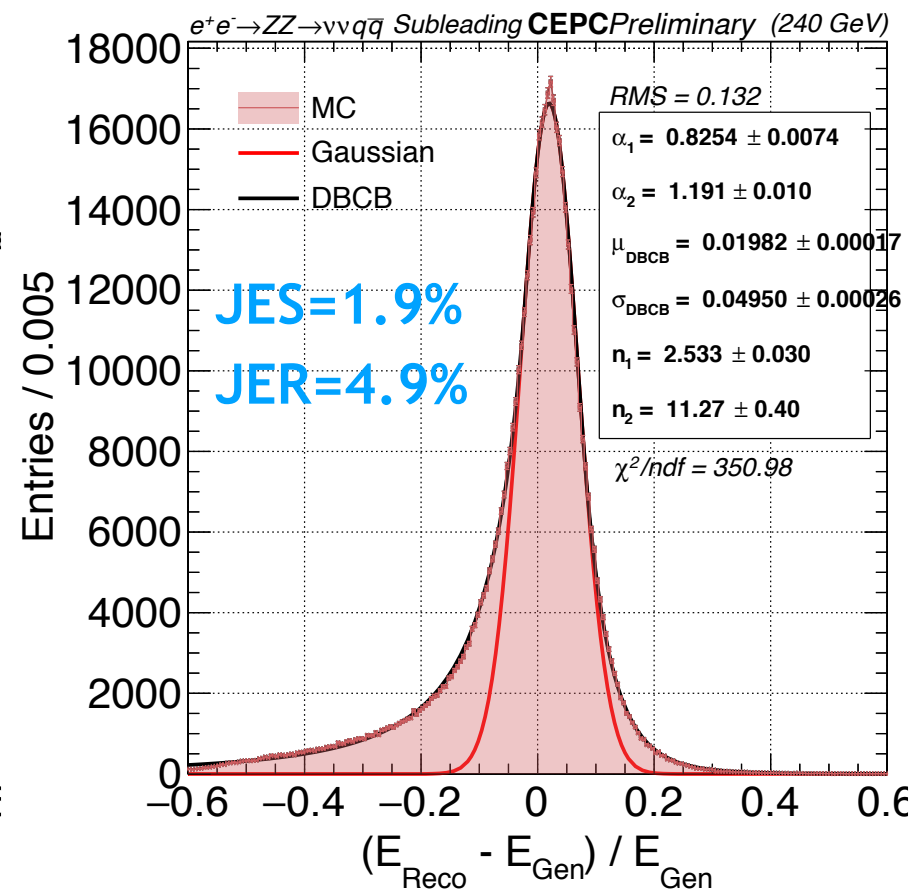
- JER/JES between Reco jet and MCP would combine the effects of two previous stages.



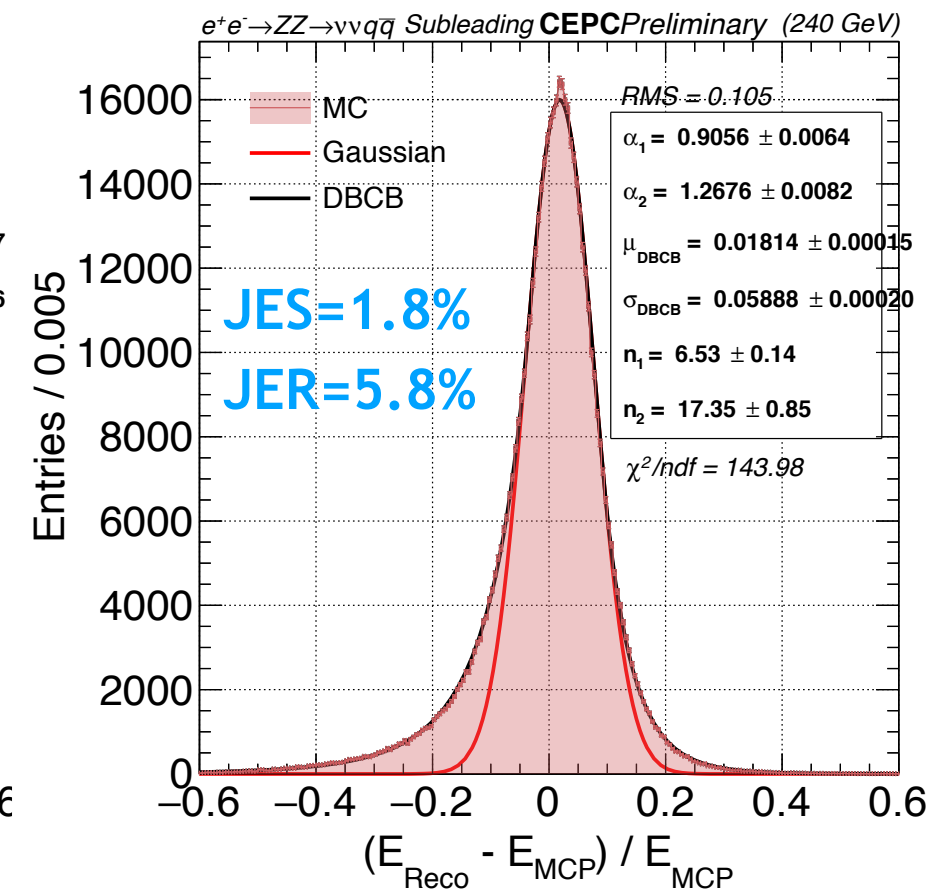
Gen-MCP



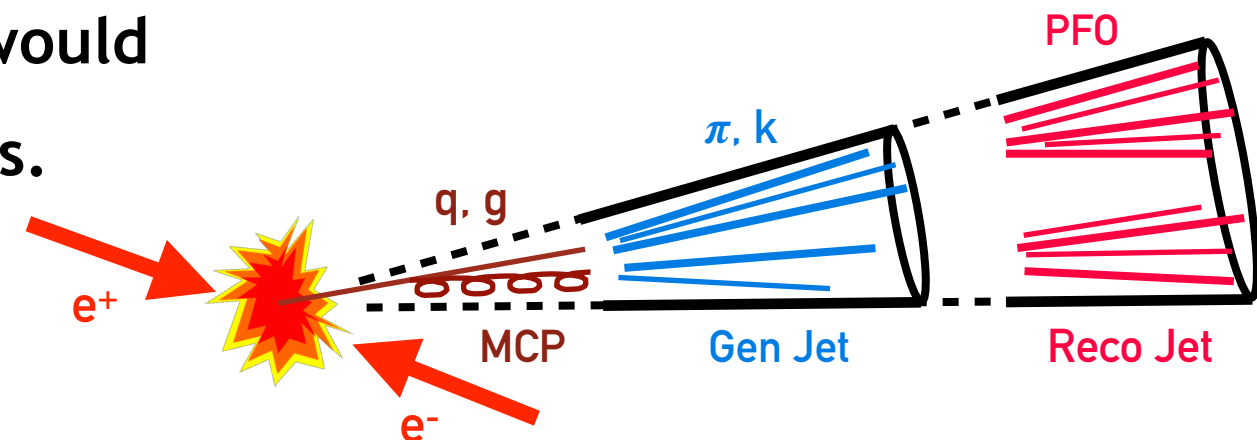
Reco-Gen

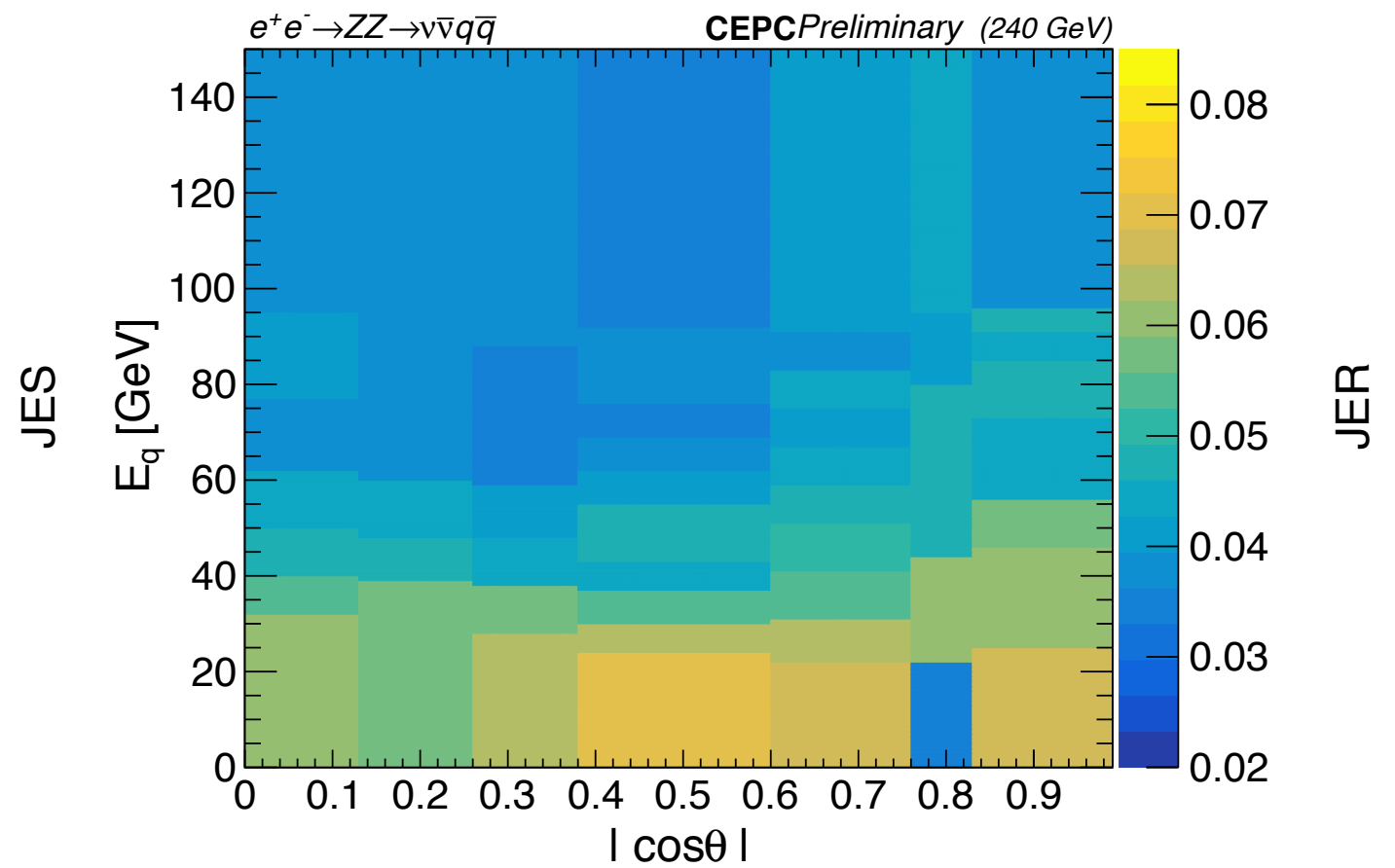
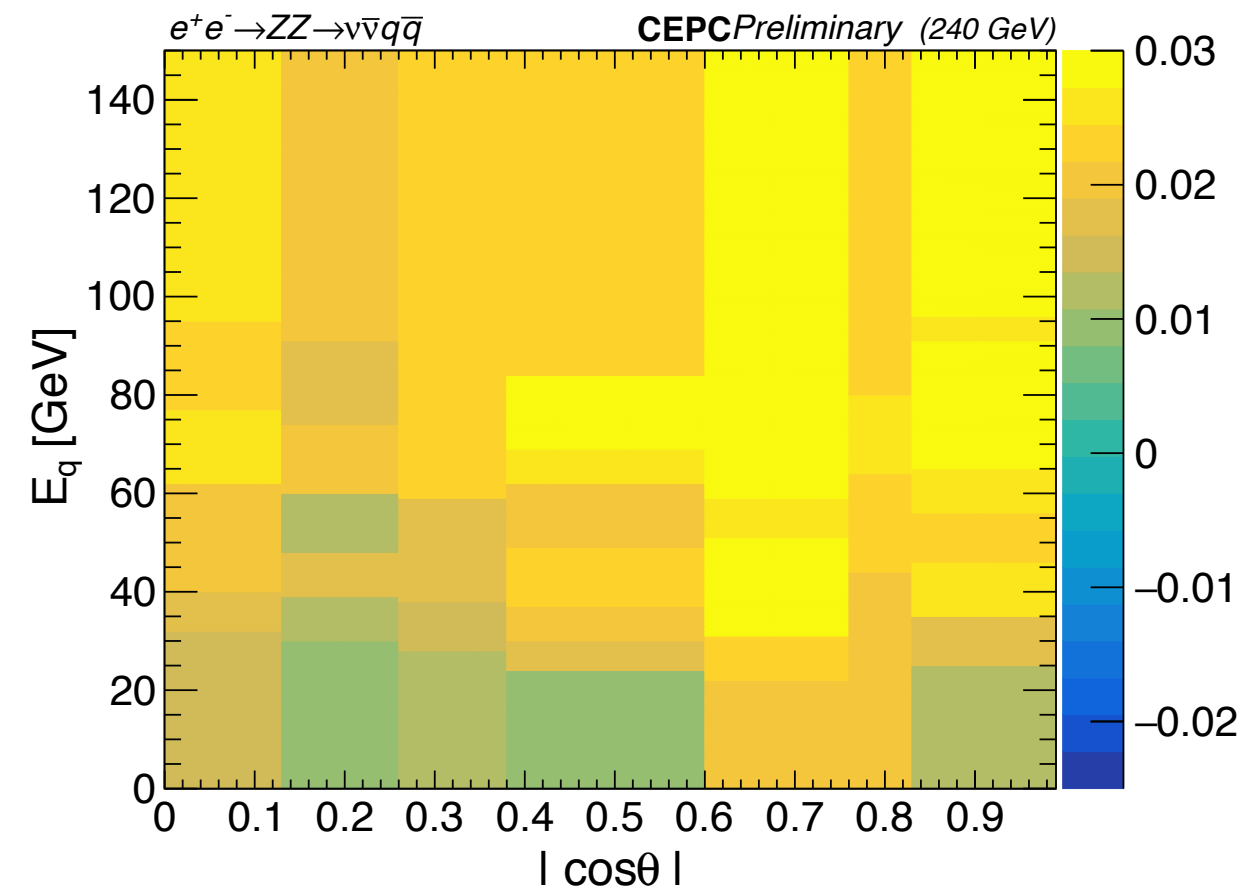


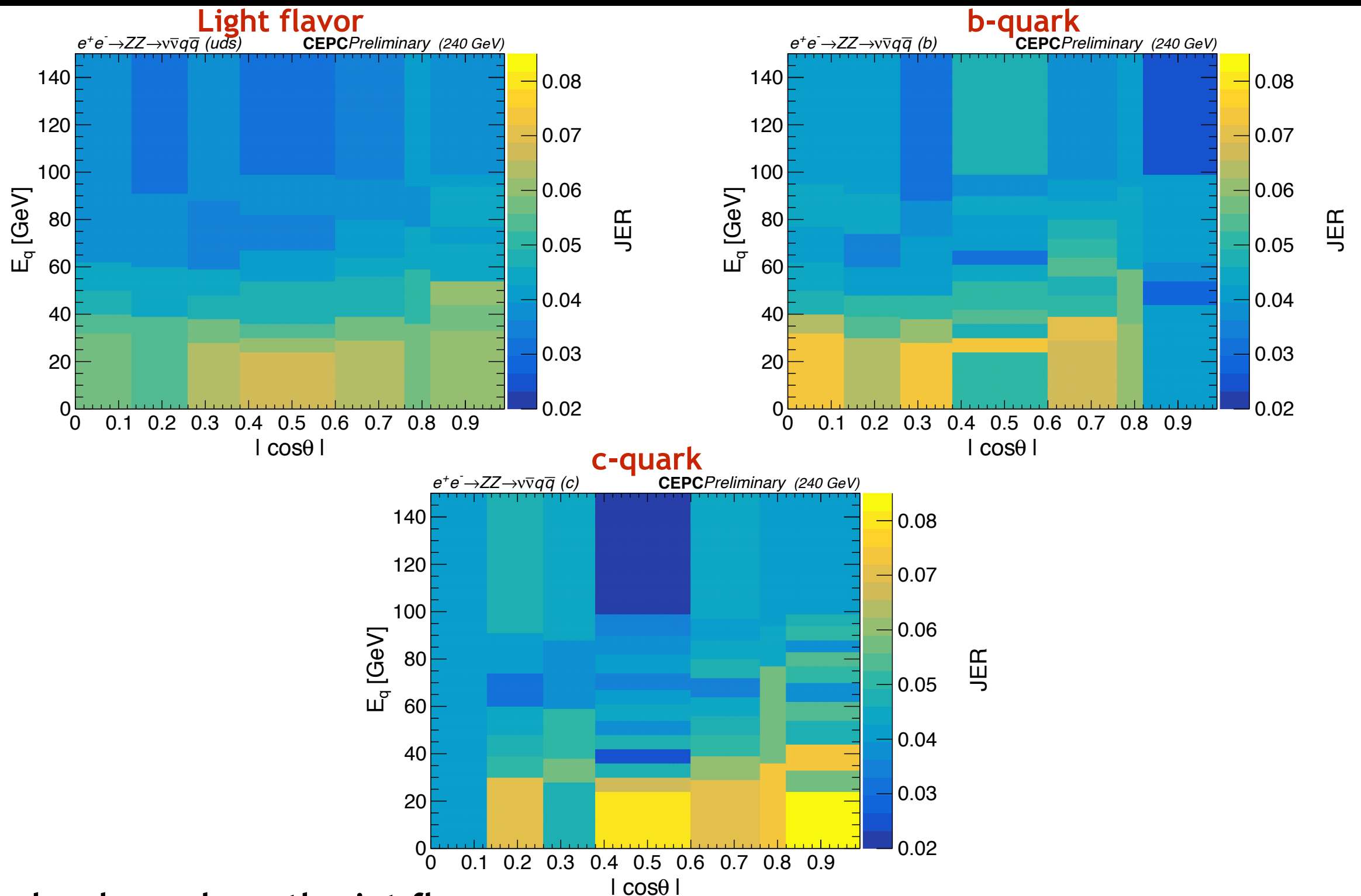
Reco-MCP



- JER/JES between Reco jet and MCP would combine the effects of two previous stages.

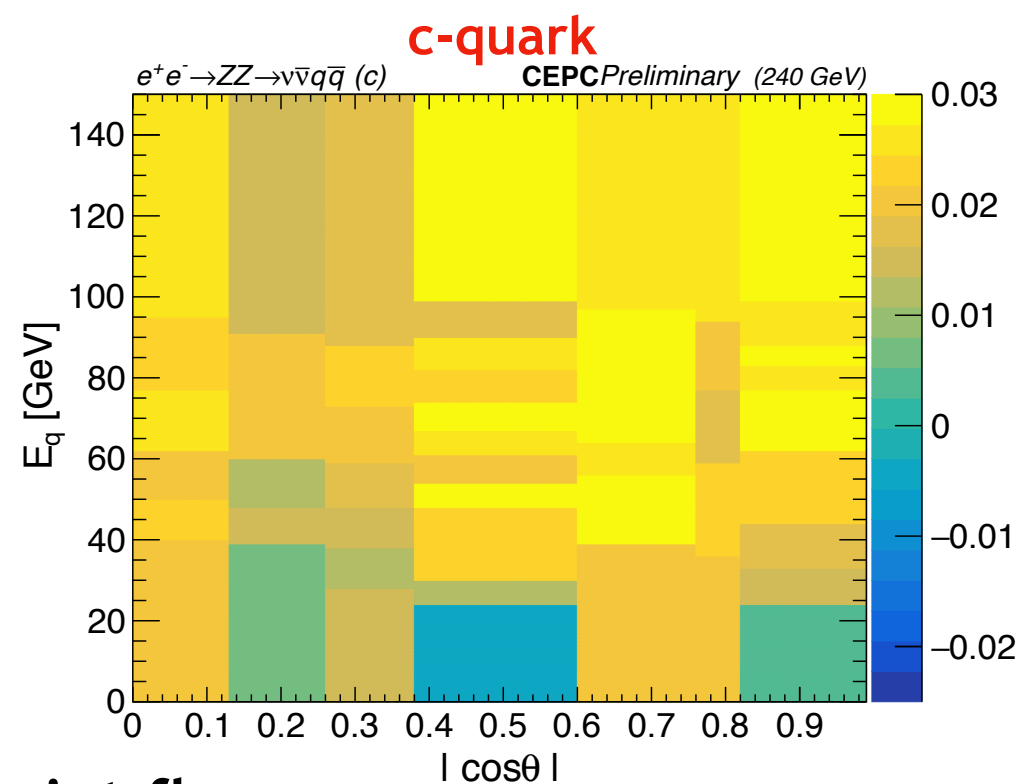
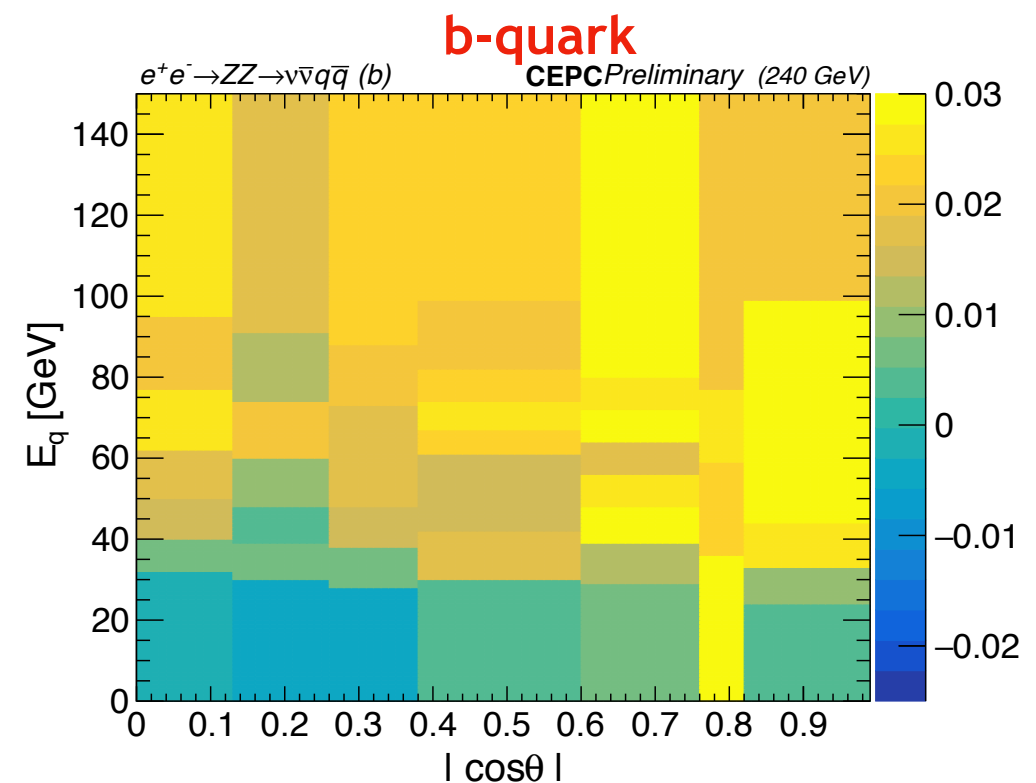
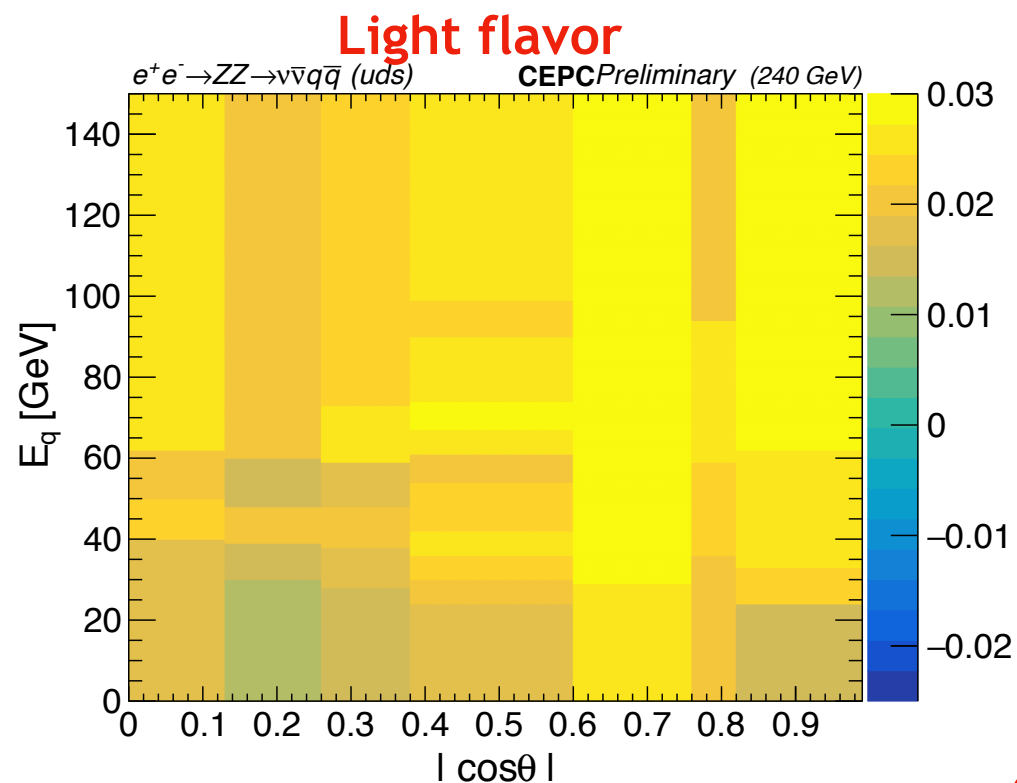






- JER also depends on the jet flavor.
- Higher jet energy and within central region of barrel, JER has impressive performance.

JES in Phase Space



- JES also depends on the jet flavor.
- Light flavor jet has higher energy deviation.